

Incremental timing analysis of synchronous programs

Partha S Roop

Joint work with Hugh Wang



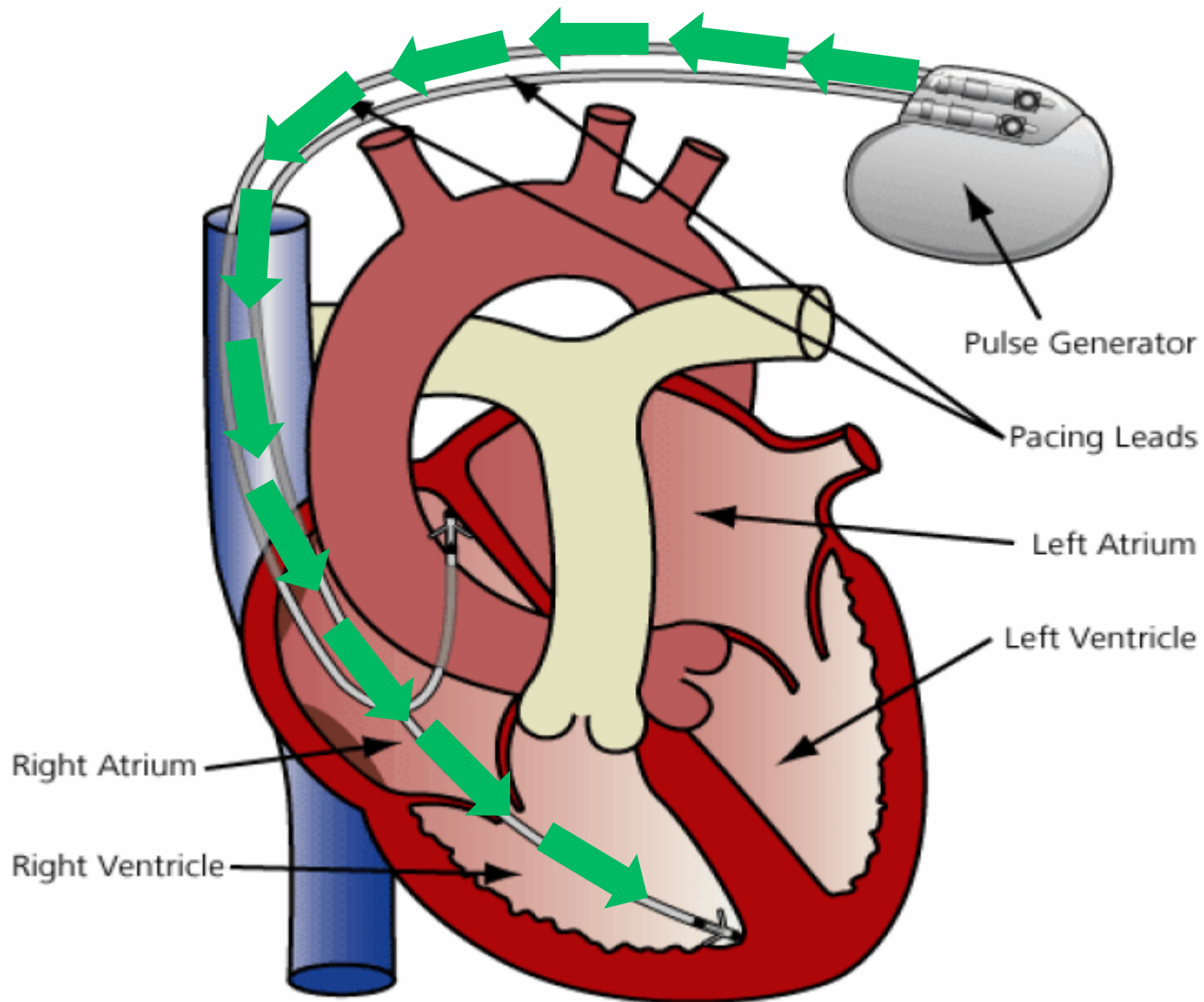
Outline

- Background
 - PRET-C
 - Timed Concurrent Control Flow Graph
- Problem statement
- Methodology
- Results
- Conclusions

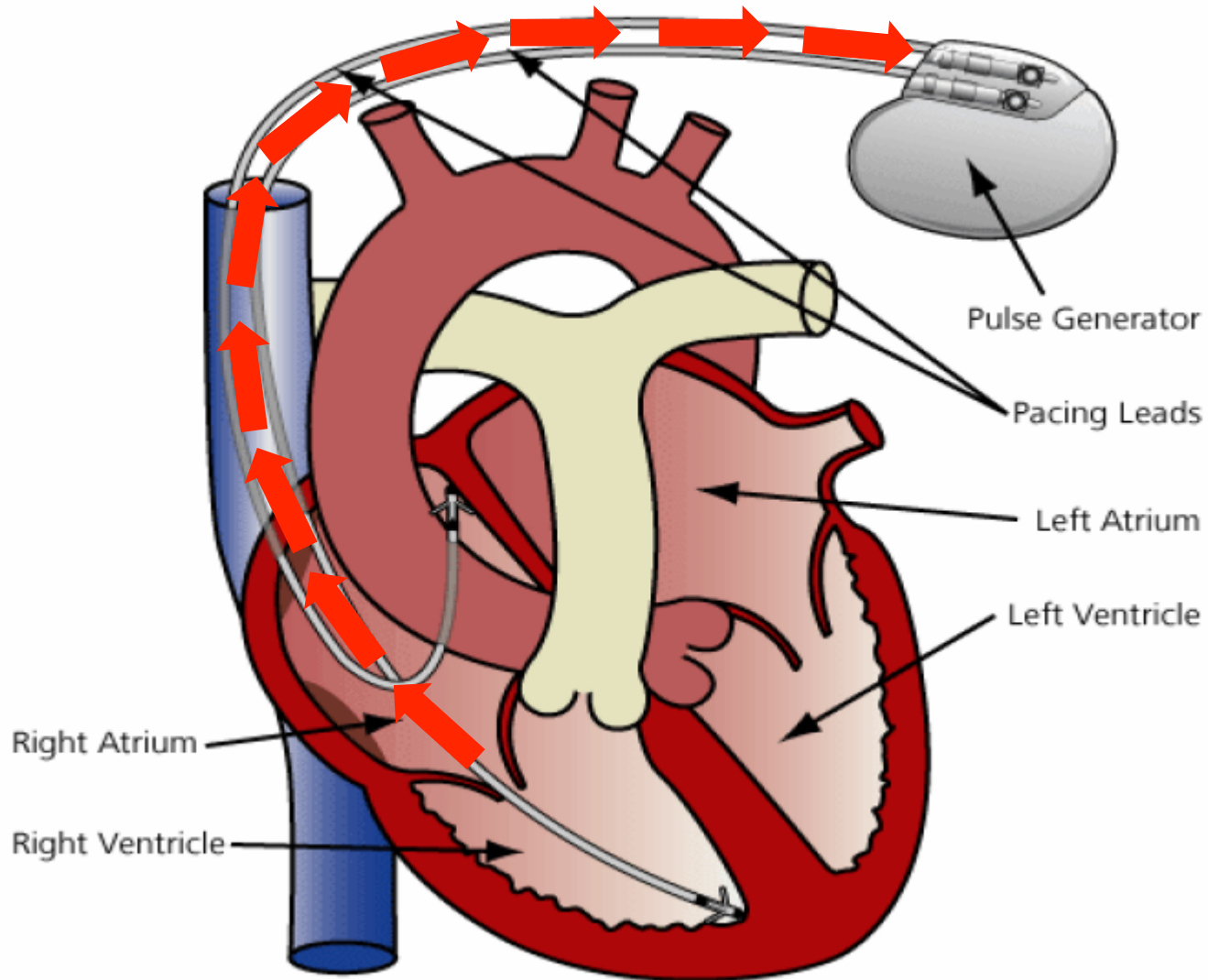
Key terms

- Worst case execution time (WCET) – It is the maximum time taken by a software on a given hardware architecture, and a given application context. WCET analysis is the task of computing a safe over-approximation of the actual WCET [Puschner et al. RTAS'06]
- Worst case response time – While WCET is defined relative to a single task, response time is usually defined for a set of concurrent tasks. Response time is defined as the time for computing a response (output) relative to a given stimulus (input).

IMPLANTABLE CARDIAC PACEMAKER



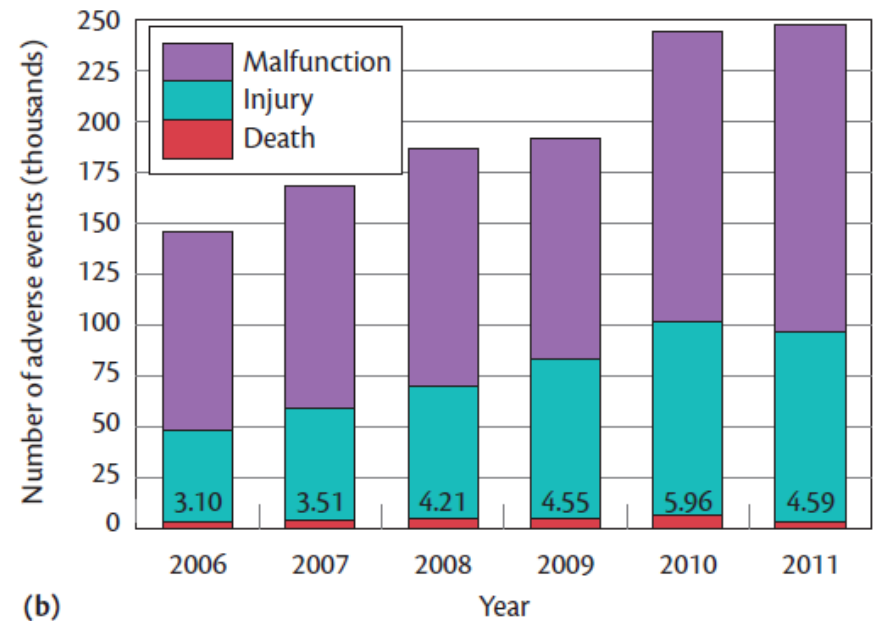
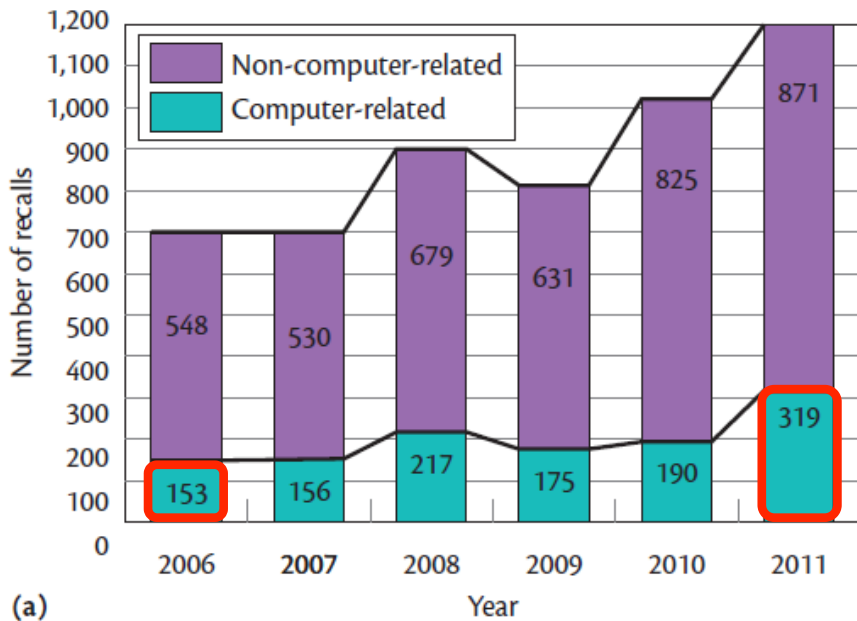
IMPLANTABLE CARDIAC PACEMAKER



A dual chamber pacemaker

- A pacemaker maintains the timing relationship between the atrial and ventricular events [Jiang et al. TACAS'12].
- These requirements are related to the response time of the pacemaker e.g.,
 - The maximum interval between two ventricular events is less than or equal to TLRI (avoid bradycardia).
 - There must not be any PMT.

FDA recalls and adverse events (2006-2011)



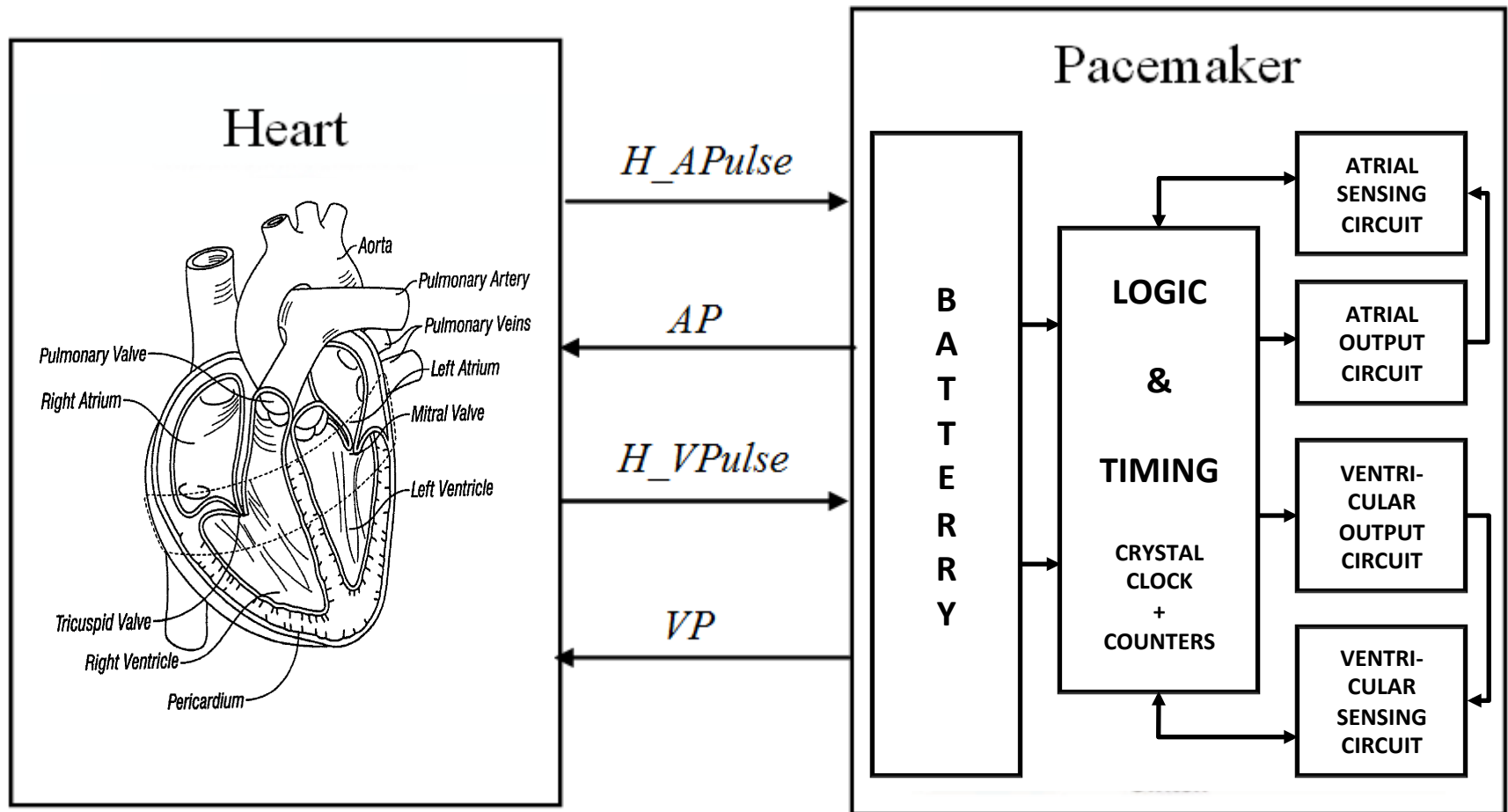
(a)

(b)

	Class I: high risk	Class II: medium risk	Class III: low risk	Total recalls	Number of devices
Software	14 (33.3%)	718 (65.6%)	46 (75.3%)	778 (64.3%)	2,303,441 (19.2%)
Hardware	8 (19.0%)	158 (14.4%)	13 (27.4%)	179 (14.8%)	4,228,133 (35.2%)
Other	10 (23.8%)	124 (11.3%)	8 (12.3%)	142 (11.7%)	2,831,048 (23.5%)
Battery	8 (19.0%)	57 (5.2%)	5 (6.8%)	70 (5.8%)	2,385,613 (19.8%)
I/O	2 (4.8%)	38 (3.5%)	1 (2.7%)	41 (3.4%)	276,601 (2.3%)
Total recalls	42 (3.5%)	1,095 (90.5%)	73 (6.0%)	1,210	12,024,836

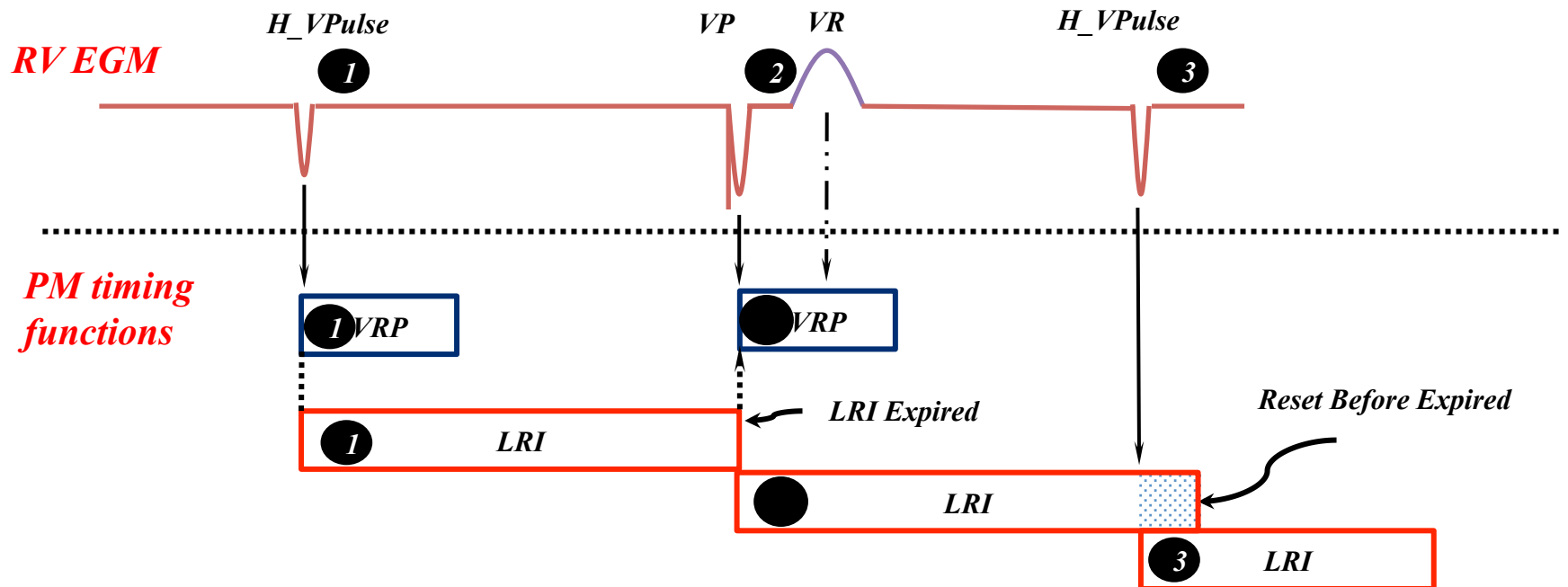
[Ref.]: Alemzadeh, H., Iyer, R.K., Kalbarczyk, Z., Raman, J., “Analysis of Safety-Critical Computer Failures in Medical Devices”, *Security and Privacy*, IEEE, vol.11, no.4. pp.14,26. July-Aug, 2013.

IMPLANTABLE CARDIAC PACEMAKER

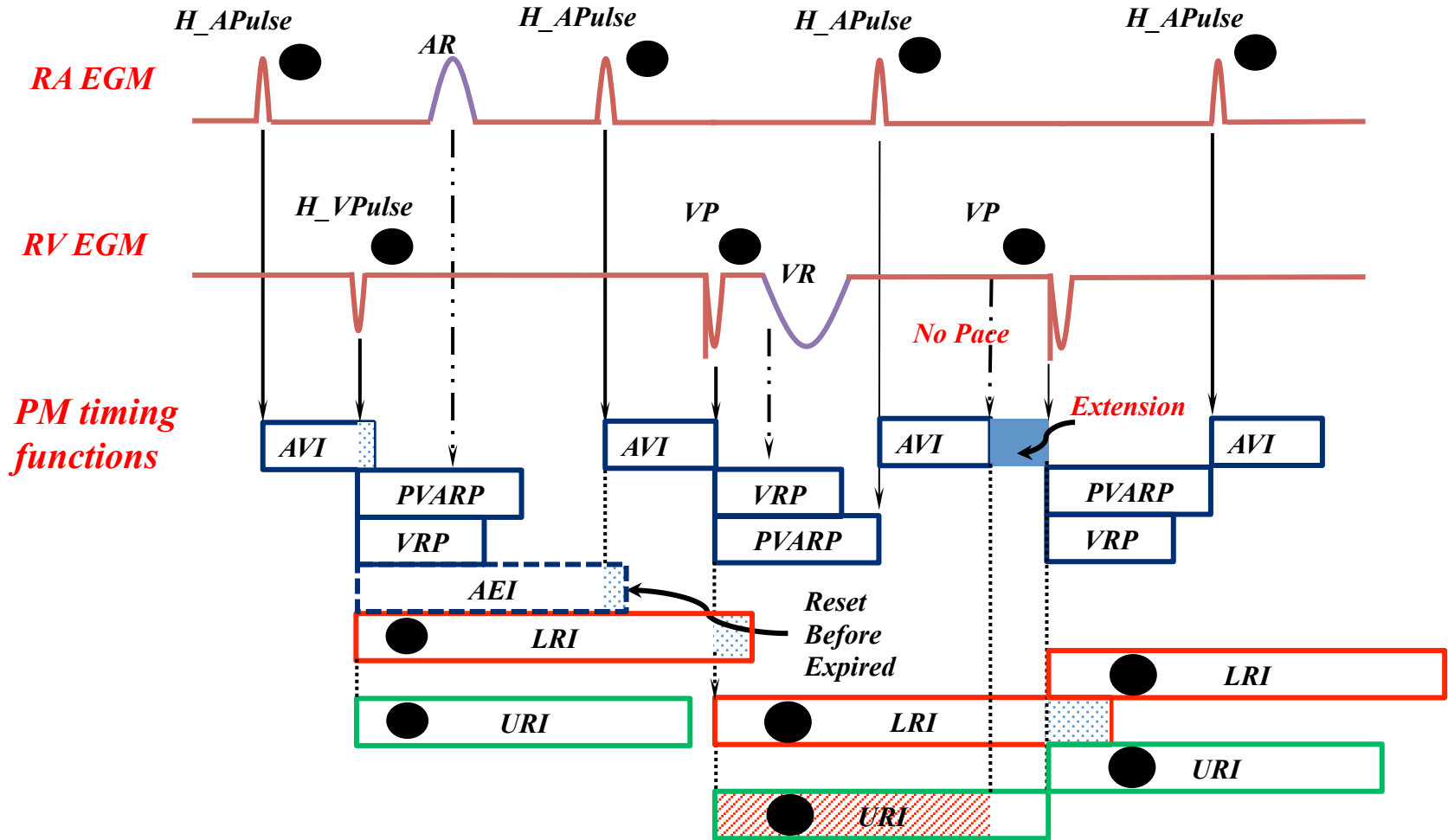


S. Serge Barold, Roland X. Stroobandt, and Alfons F. Sinnaeve, *Cardiac Pacemakers Step by Step*, Futura Publishing, 2004.

TIMING DIAGRAM FOR VVI MODE



TIMING DIAGRAM FOR DDD MODE



WCET analysis of synchronous programs

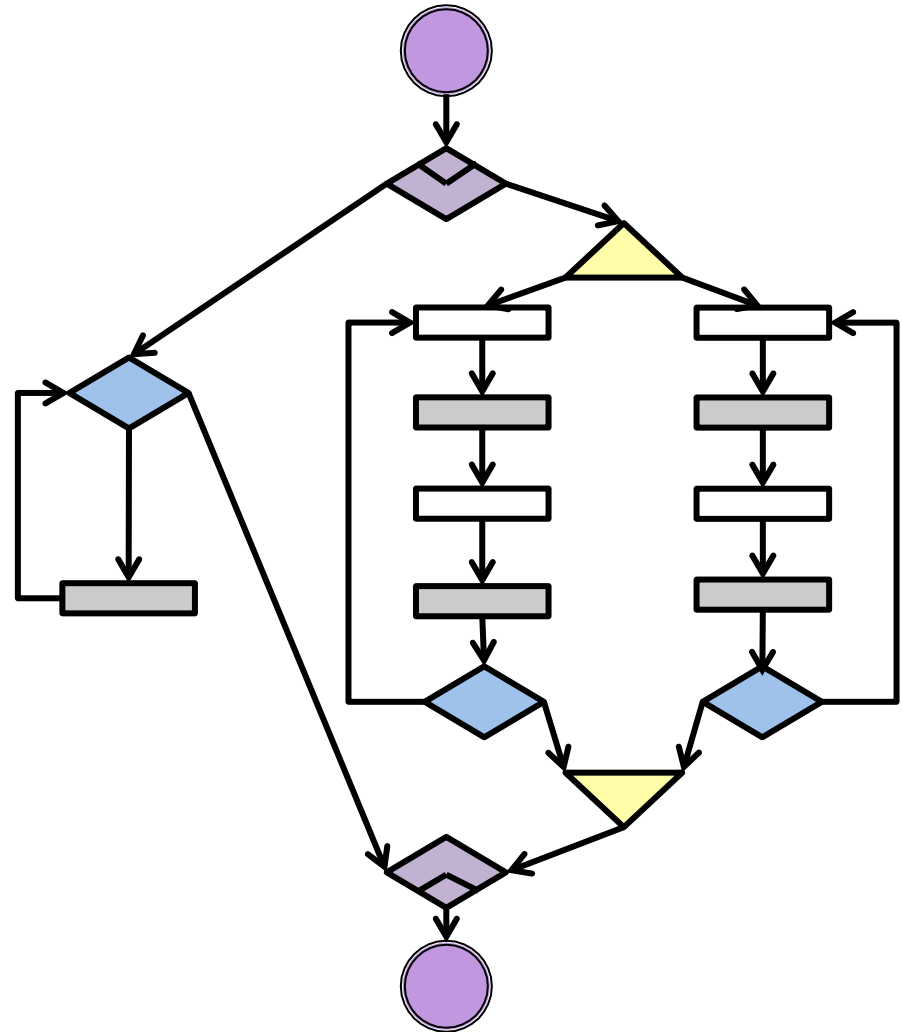
- Also referred to as worst case reaction time (WCRT) analysis.
- Here, system computes a set of reactions indefinitely. Reactions are also known as ticks.
- WCRT refers to the worst case length of any reaction / tick.
- Objectives:
 - How to satisfy timing constraints (Partha)
 - How to also minimize power consumption (Hugh)

Related work

- **Plus-max** [Boldt et al. SLA++P'07, Mendler et al. DATE'09].
- **IPET** [Ju et al. journal of RTS'12, DAC'09].
- **Model checking** [Roop et al. CASES'09].
- **Reachability** [Kuo et al. DAC'11, Yip et al. ACSD'13].
- Techniques for improved precision:
 - **Infeasible path elimination** [Andalam et al. DATE'11]
 - **Hybrid approach** [Raymond et al. RTNS'13]: Model checking +ILP.

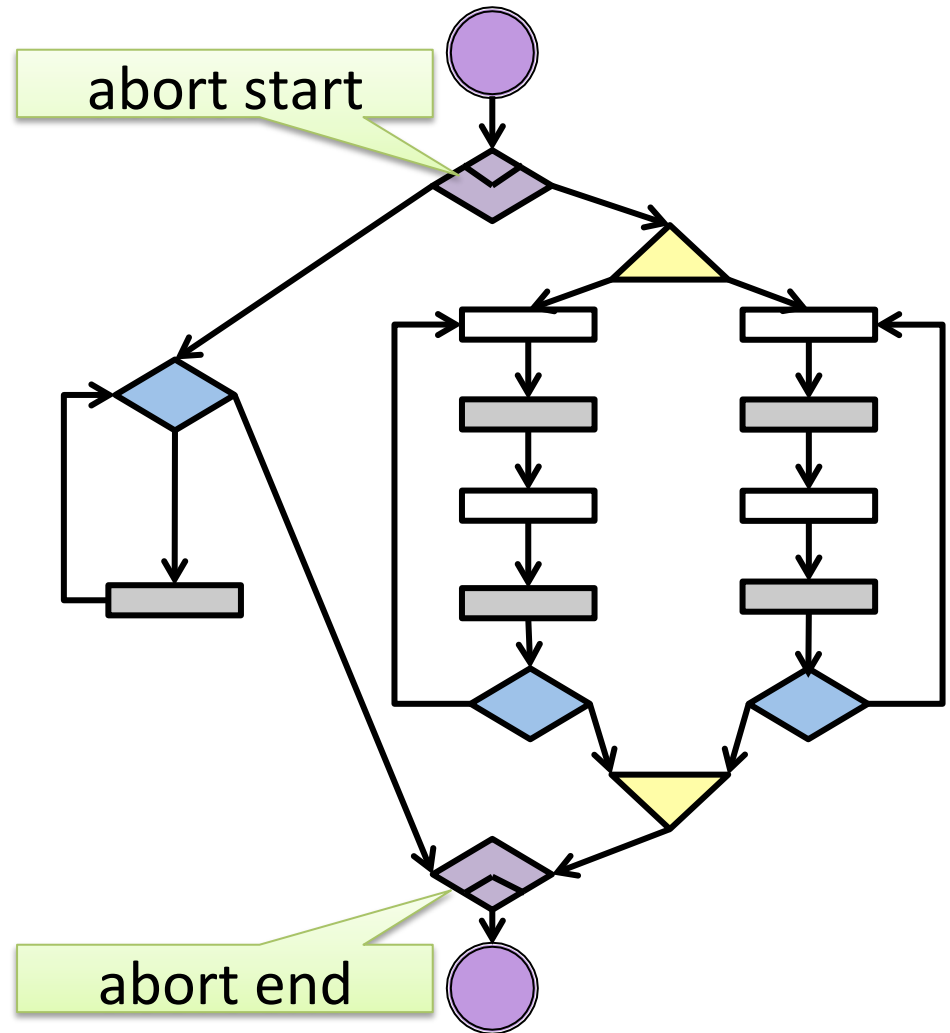
Synchronous program and TCCFG

```
int main (){  
  abort{  
    PAR(t1,t2);  
  }when(S0)  
}
```



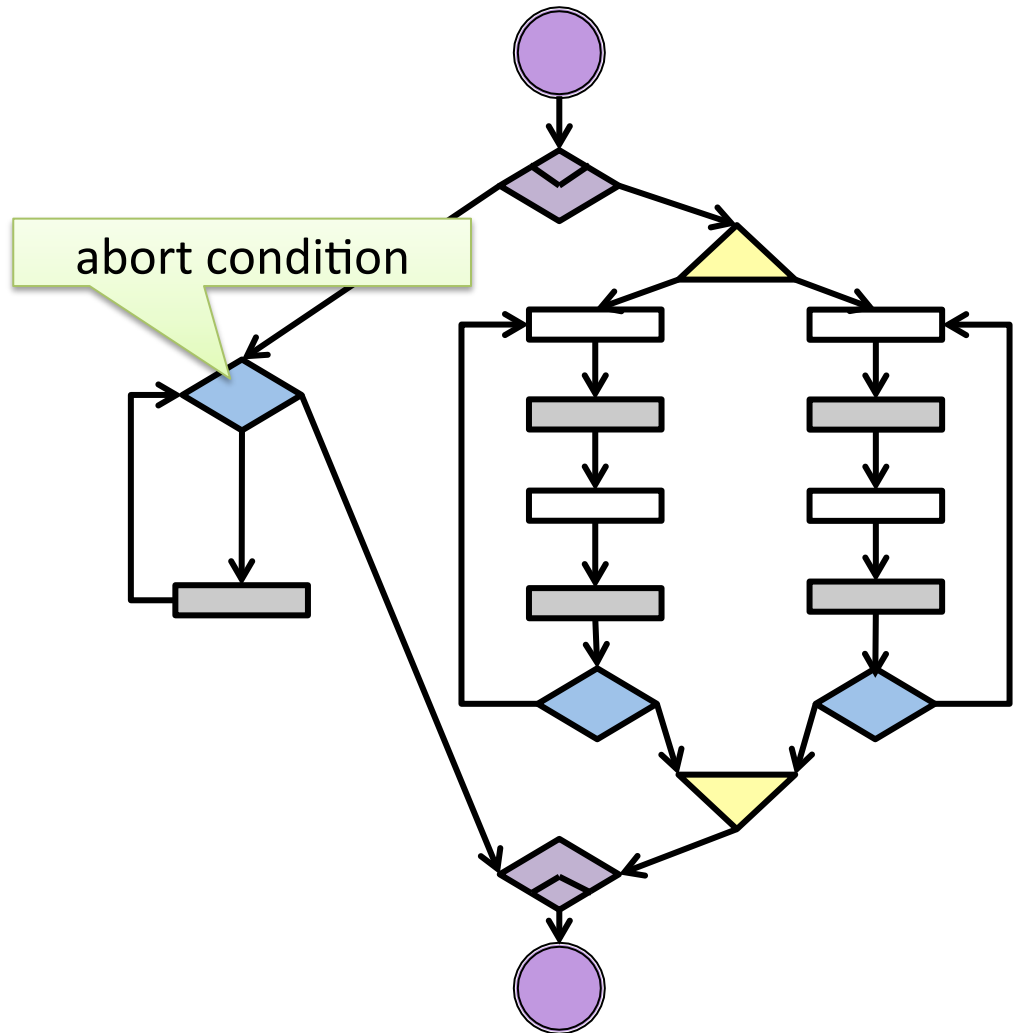
Execution

```
int main (){  
  abort{  
    PAR(t1,t2);  
  }when(S0)  
}
```



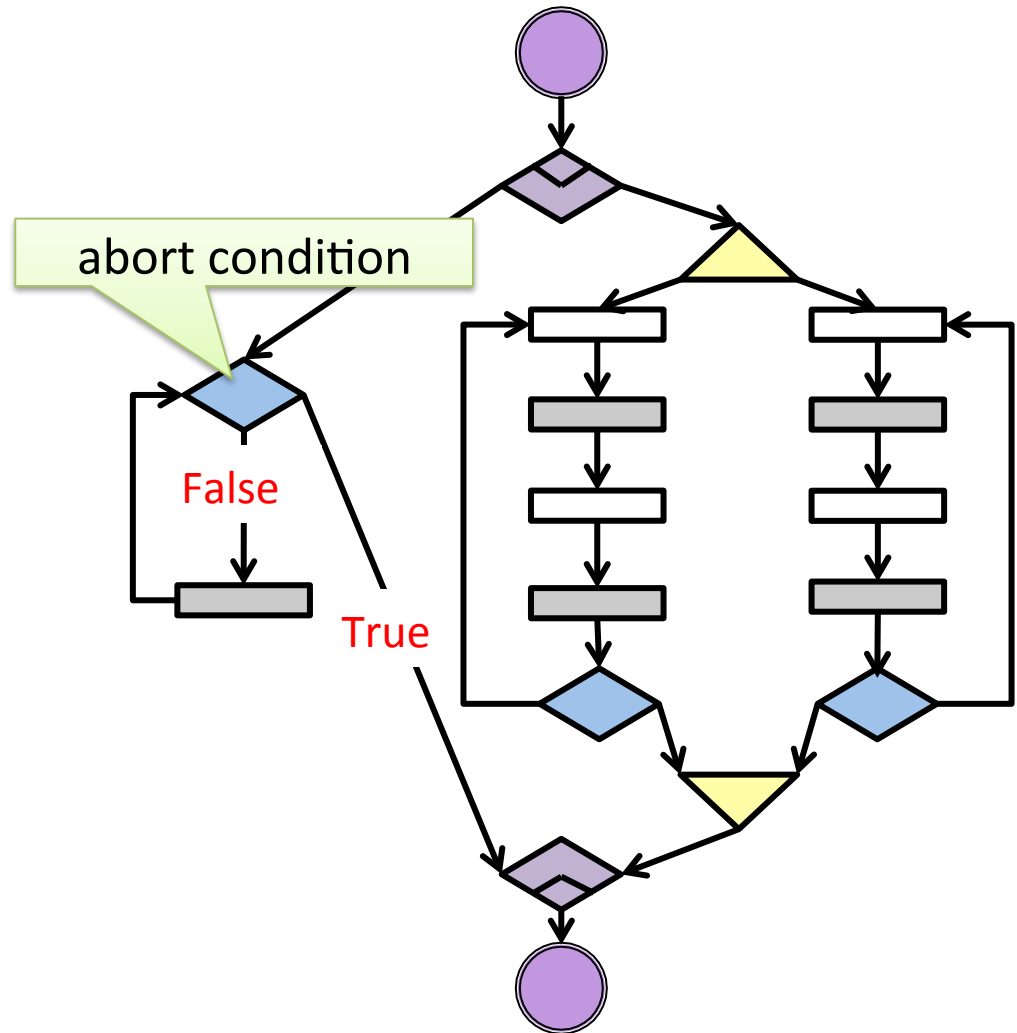
Execution

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int main (){  
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}
```



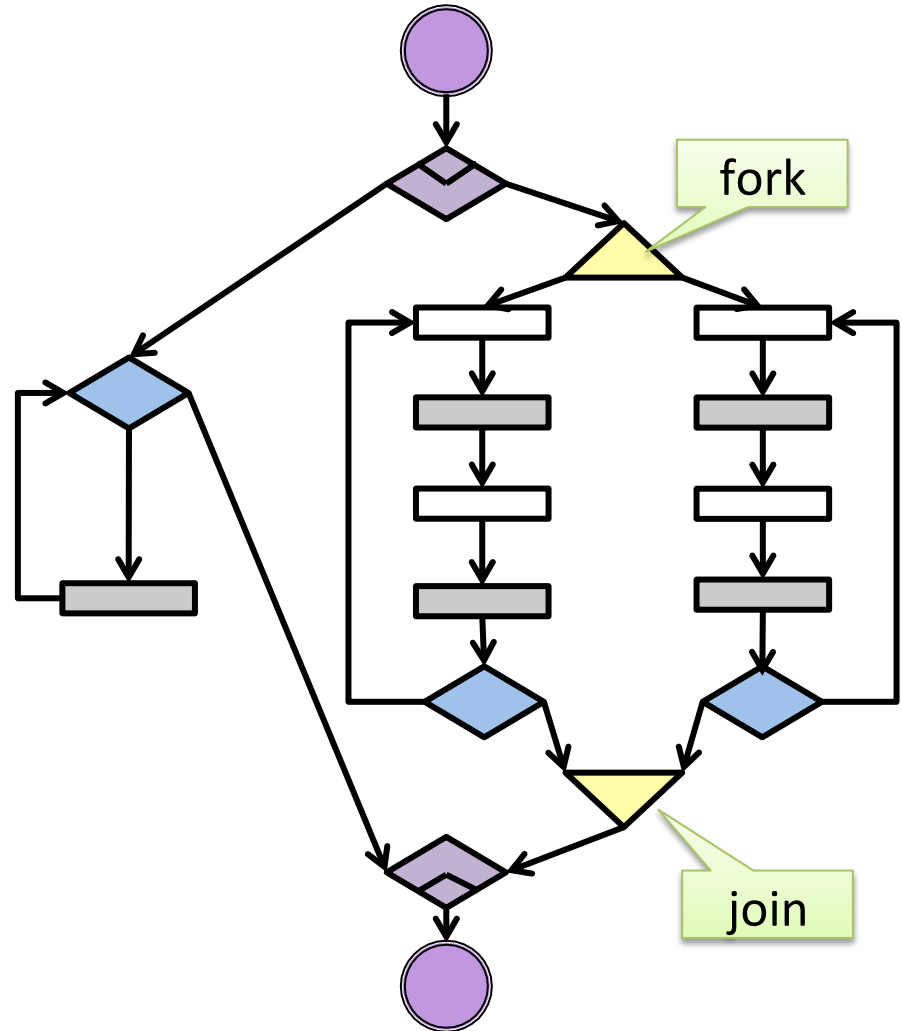
Execution

```
int main (){  
  abort{  
    PAR(t1,t2);  
  }when(S0)  
}
```



PRET-C and TCCFG

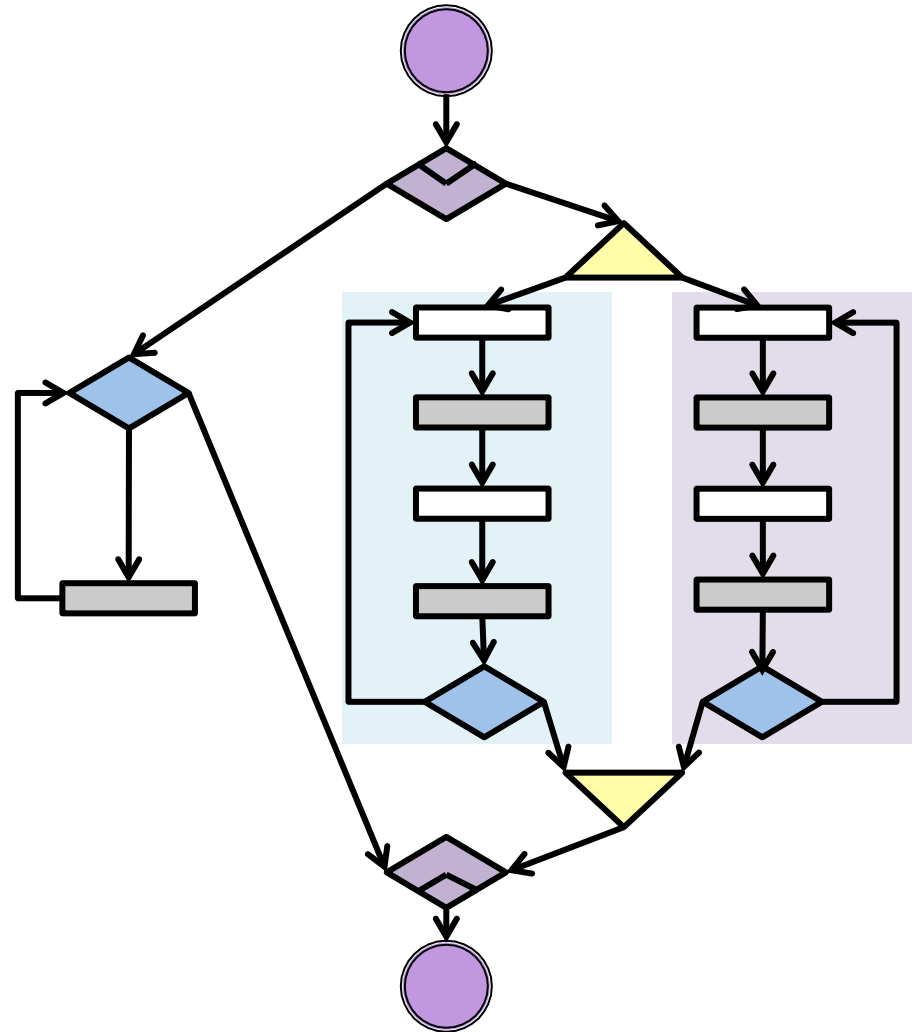
```
int main (){  
  abort{  
    PAR(t1,t2);  
  }when(S0)  
}
```



Execution

```
thread t1(){  
  do{  
    foo1();  
    EOT;  
    foo2();  
    EOT;  
  }while(S1)  
}
```

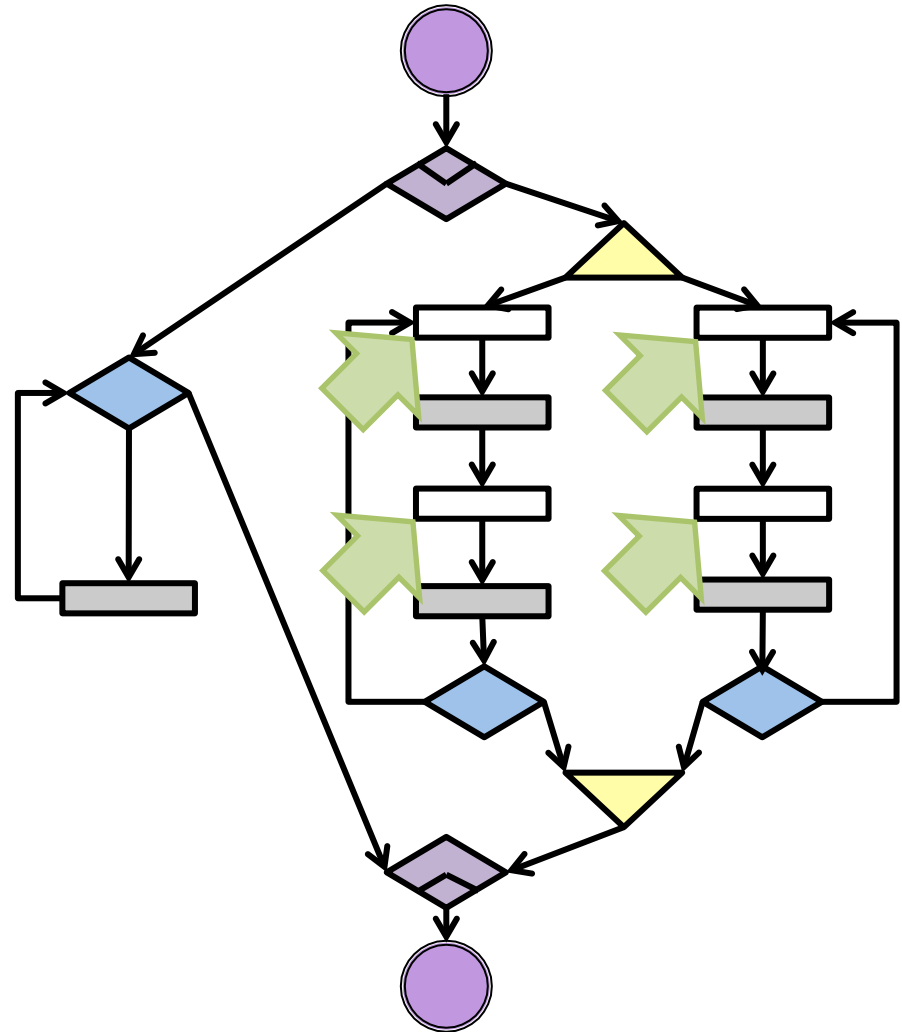
```
thread t2(){  
  do{  
    foo3();  
    EOT;  
    foo4();  
    EOT;  
  }while(S2)  
}
```



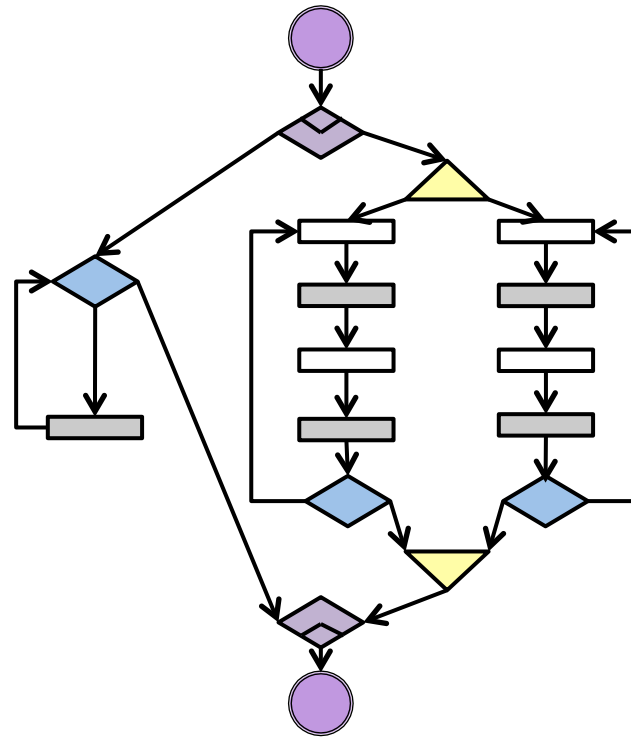
Execution

```
thread t1(){  
  do{  
    foo1();  
    EOT;  
    foo2();  
    EOT;  
  }while(S1)  
}
```

```
thread t2(){  
  do{  
    foo3();  
    EOT;  
    foo4();  
    EOT;  
  }while(S2)  
}
```

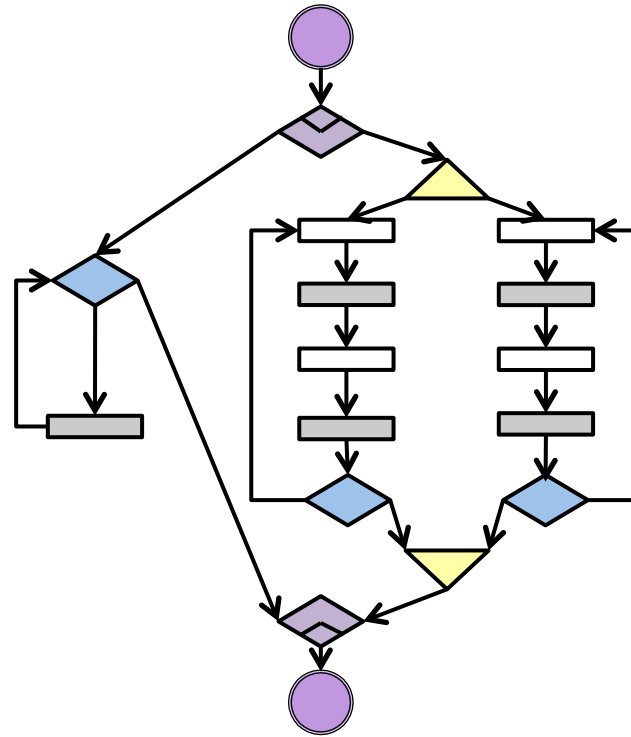


Execution paths in TCCFG



→ Time

Execution paths in TCCFG

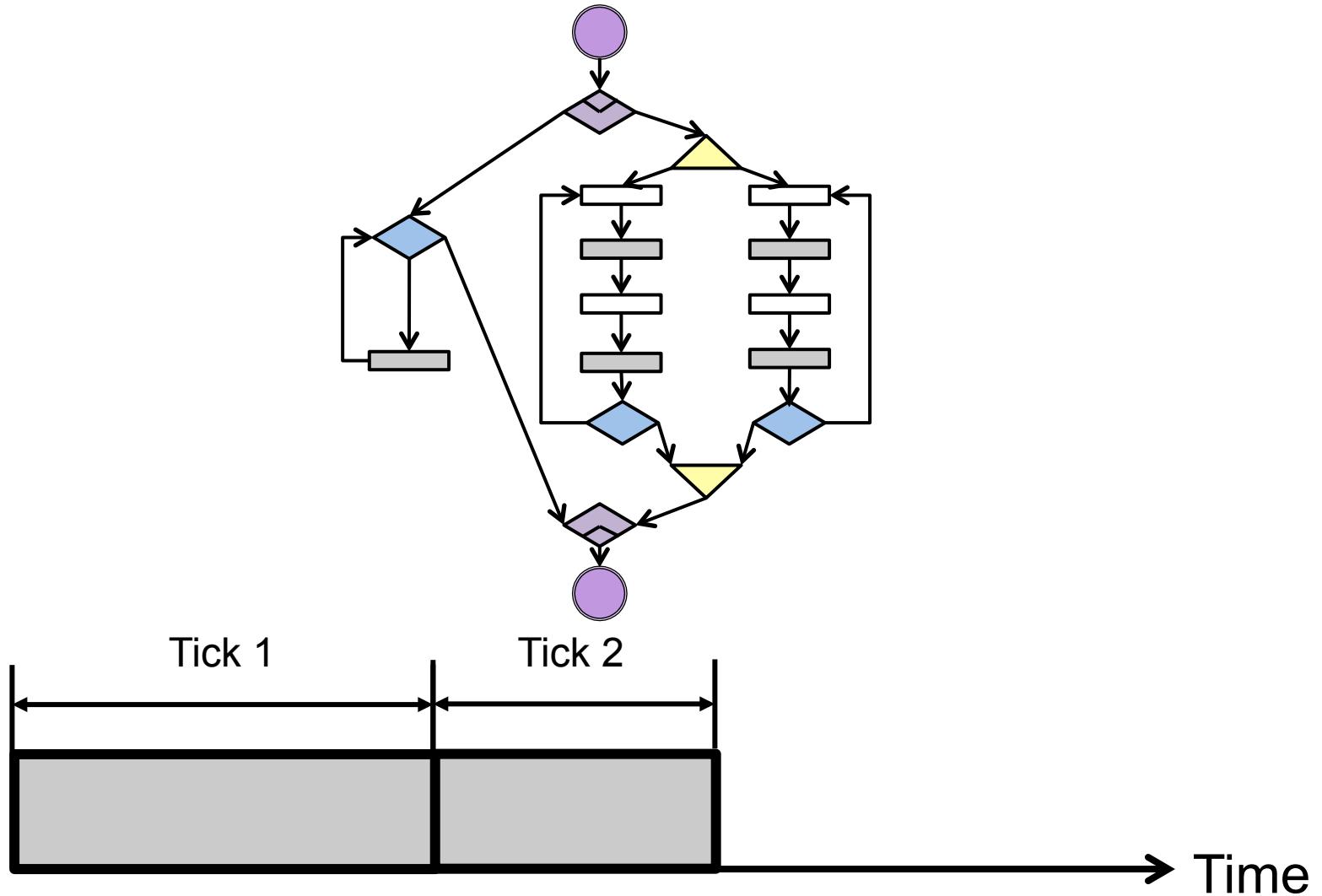


Threads execute
in a fixed order.

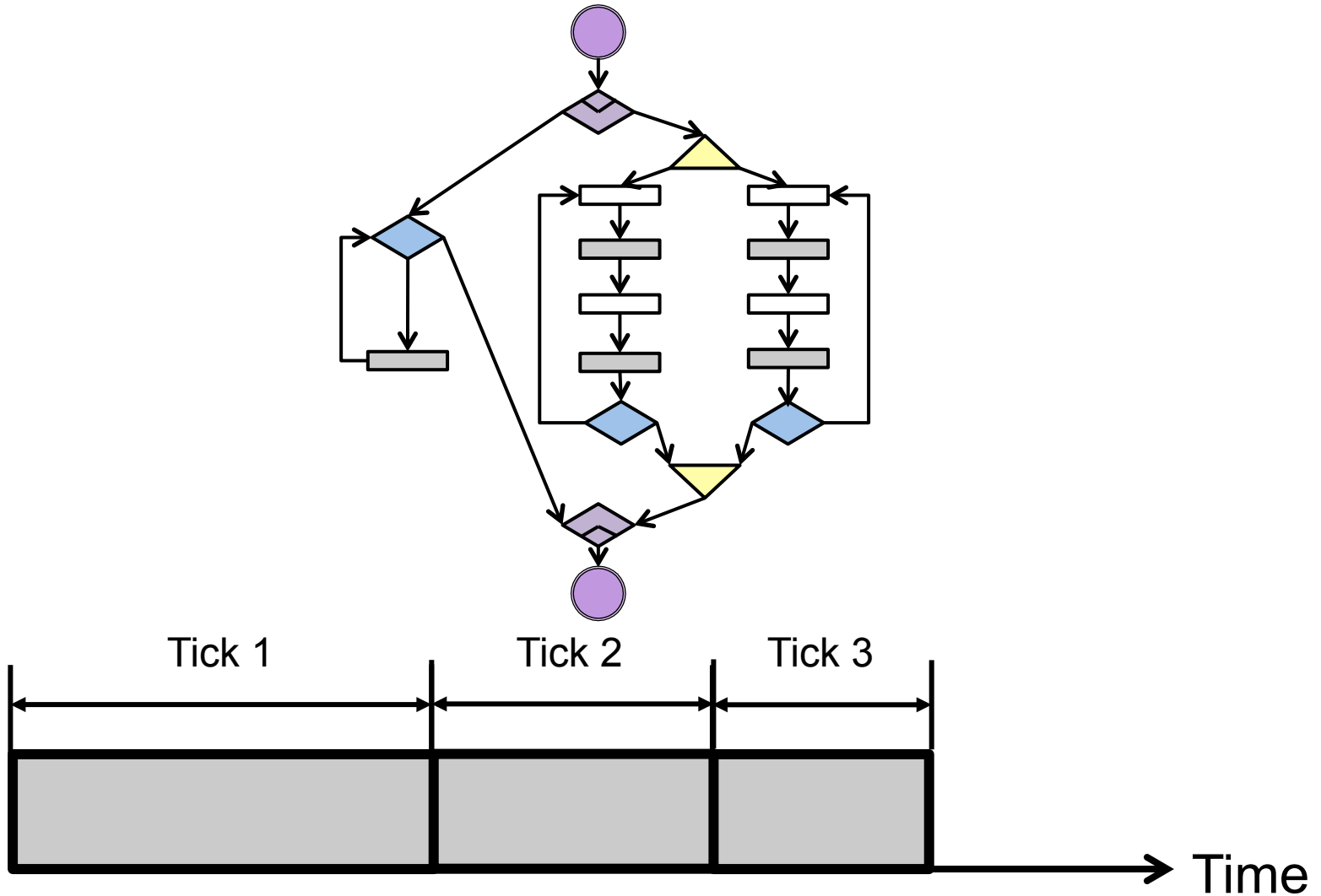
From Left to Right



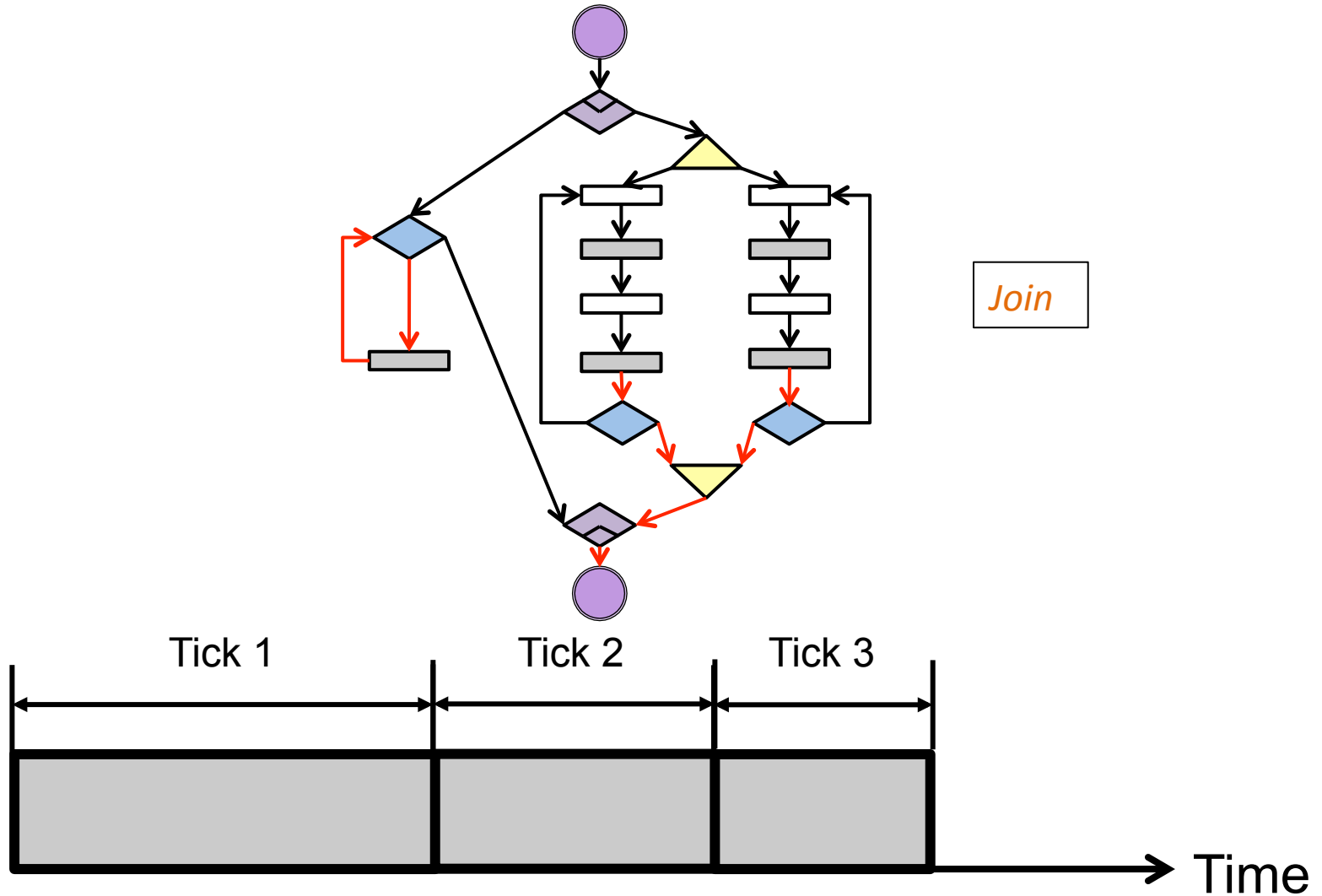
Execution paths in TCCFG



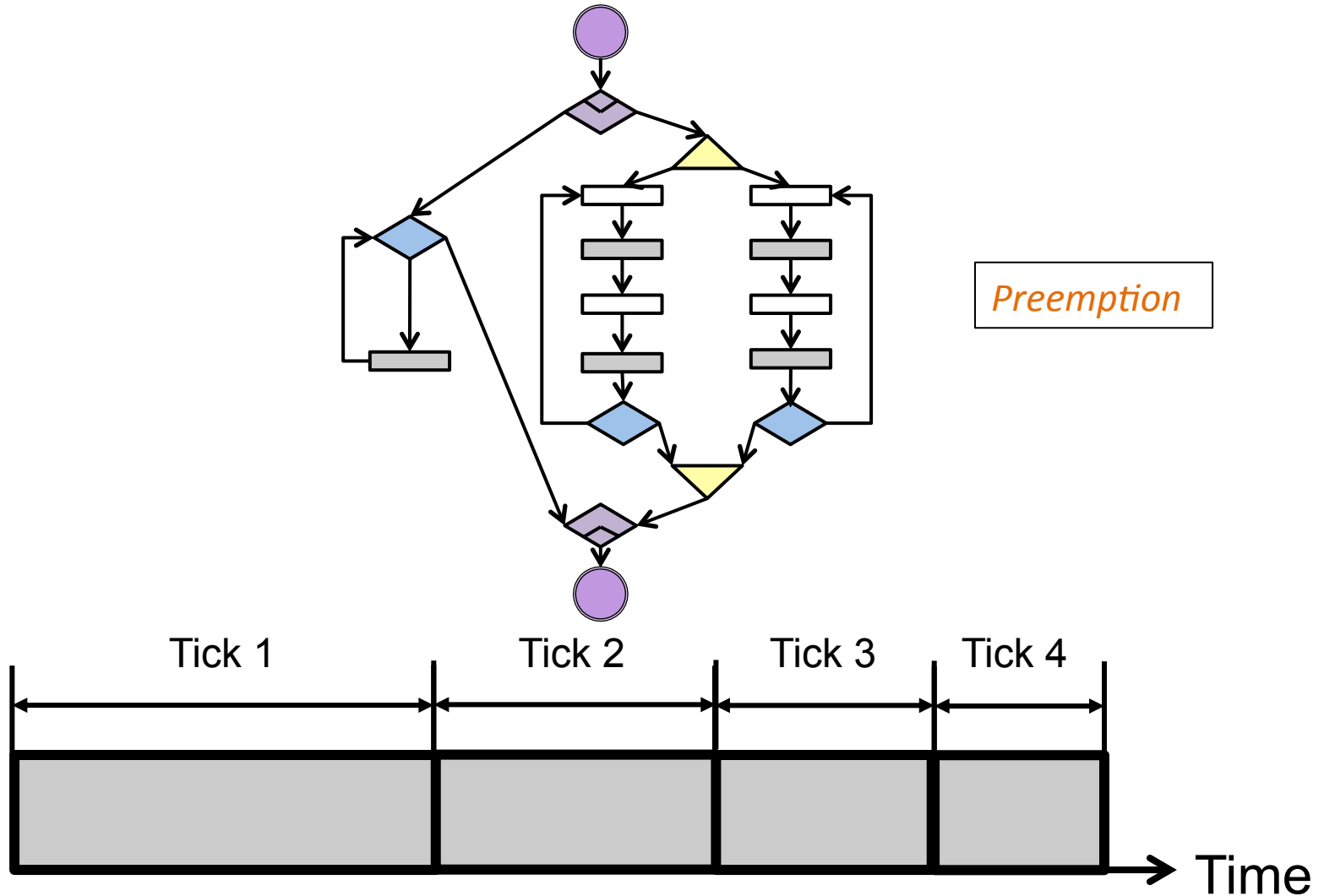
Execution paths in TCCFG



Execution paths in TCCFG

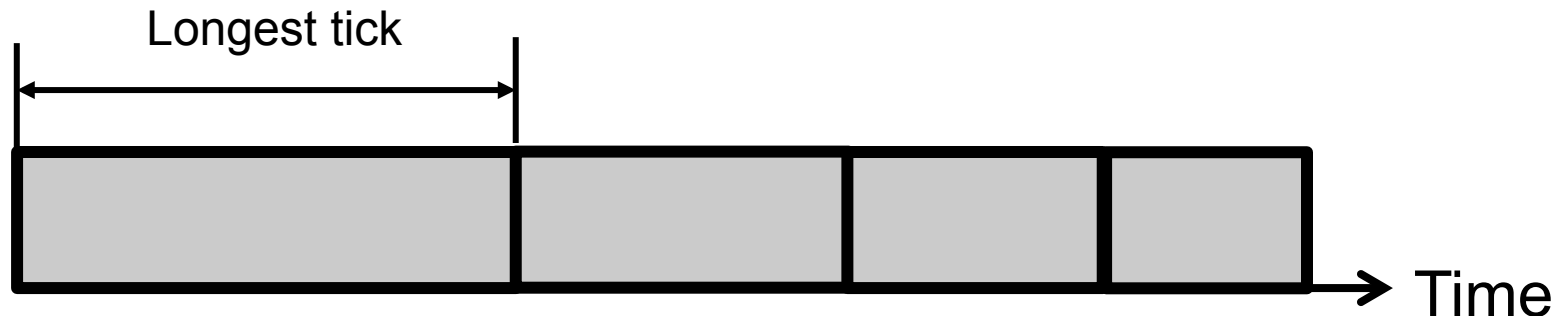


Execution paths in TCCFG

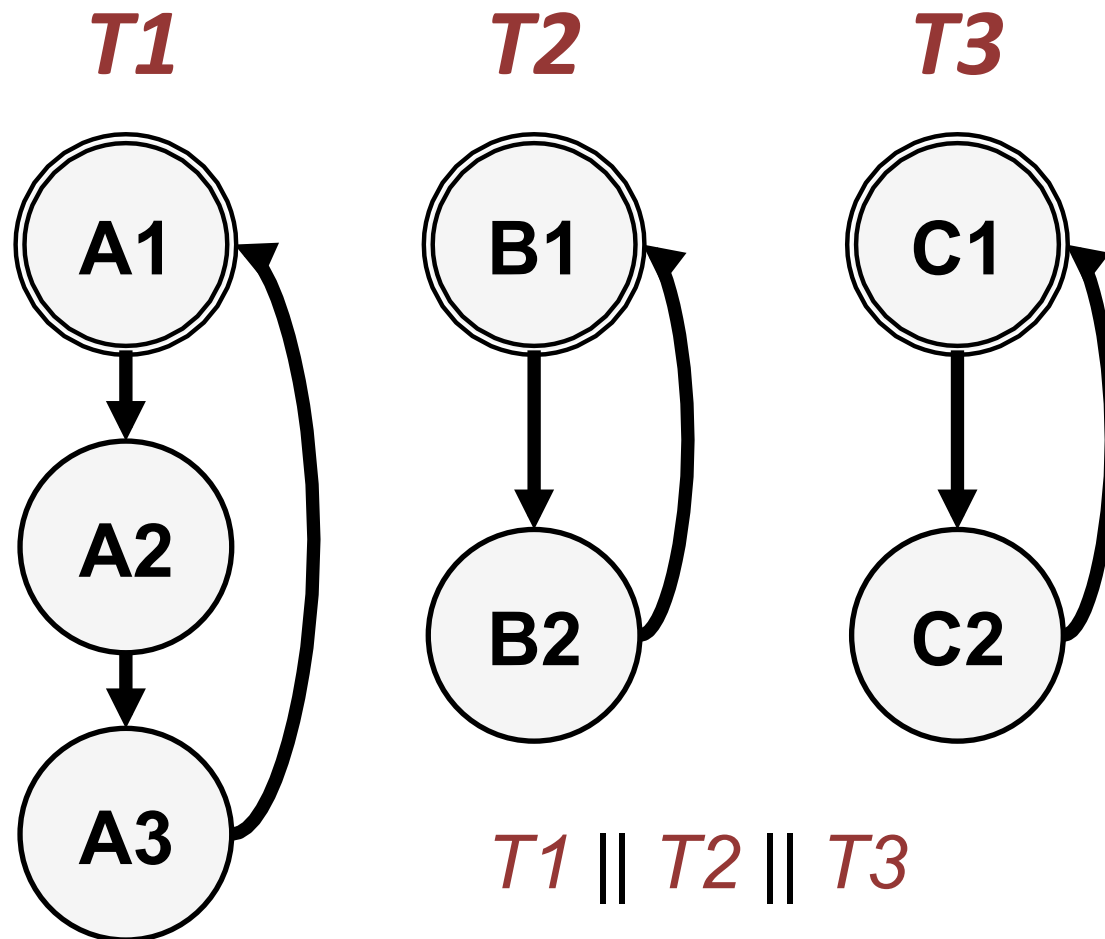


Synchronous languages

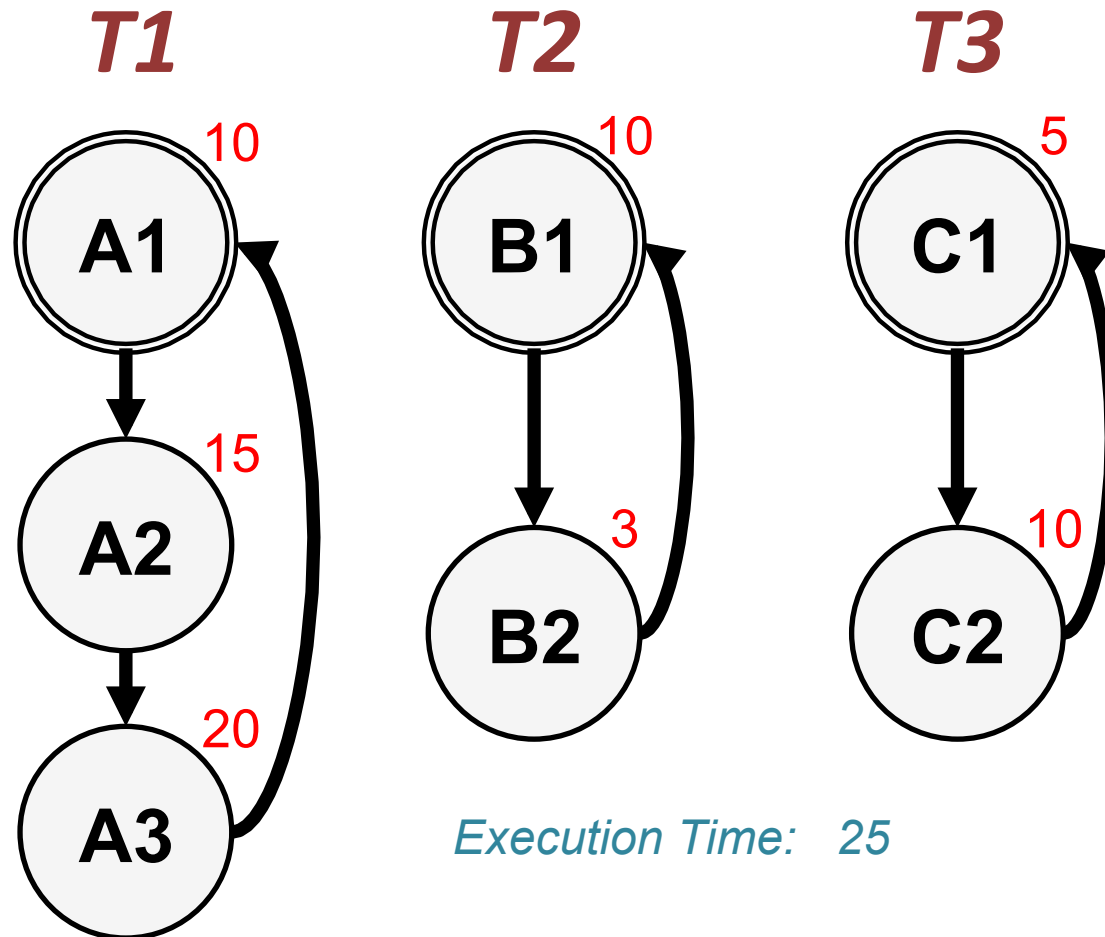
- Worst Case Reaction Time analysis
 - WCRT analysis
- Synchrony hypothesis
 - *Reactive system operates infinitely fast compared to the environment.*
- Validation
 - $\text{Min}(\text{inter-arrival-time of events}) \geq \text{Max}(\text{Reaction Time})$
 - $\text{Deadline} \geq \text{WCRT}$



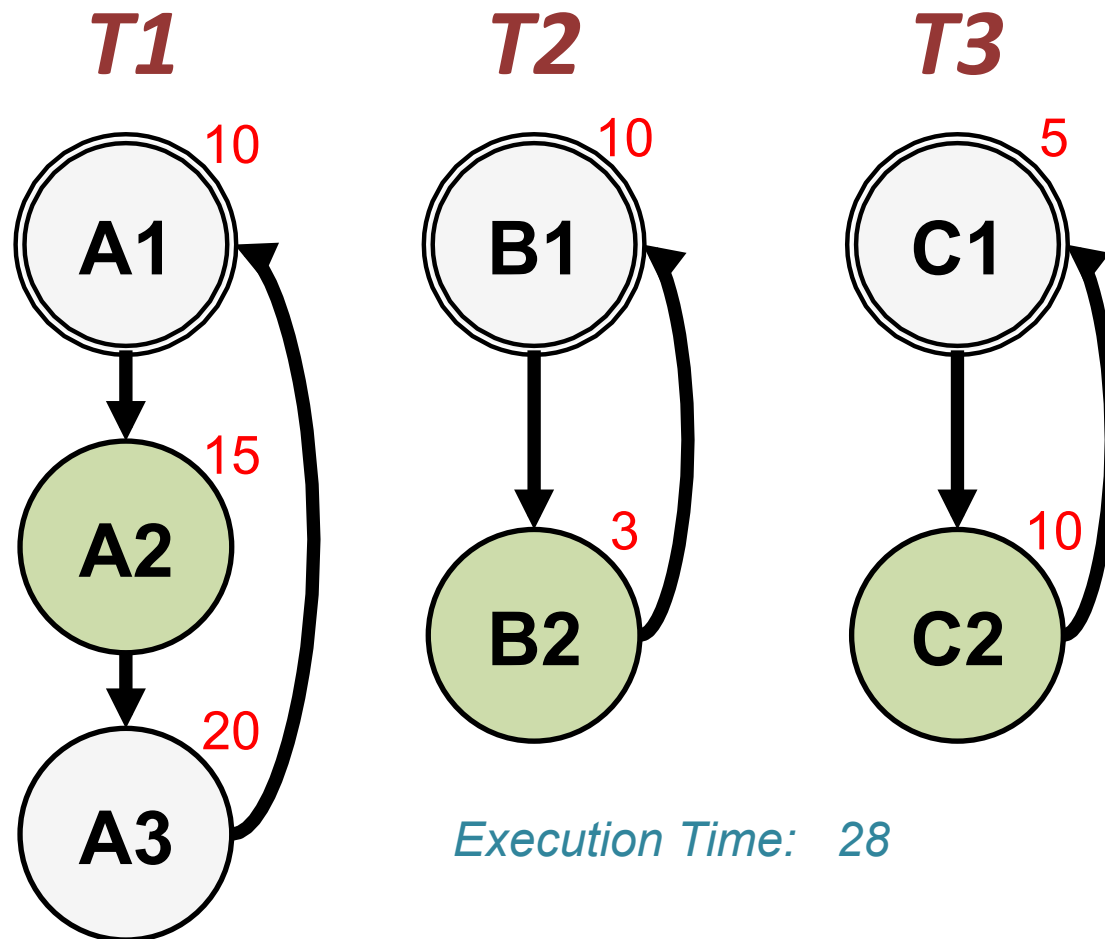
Motivating example



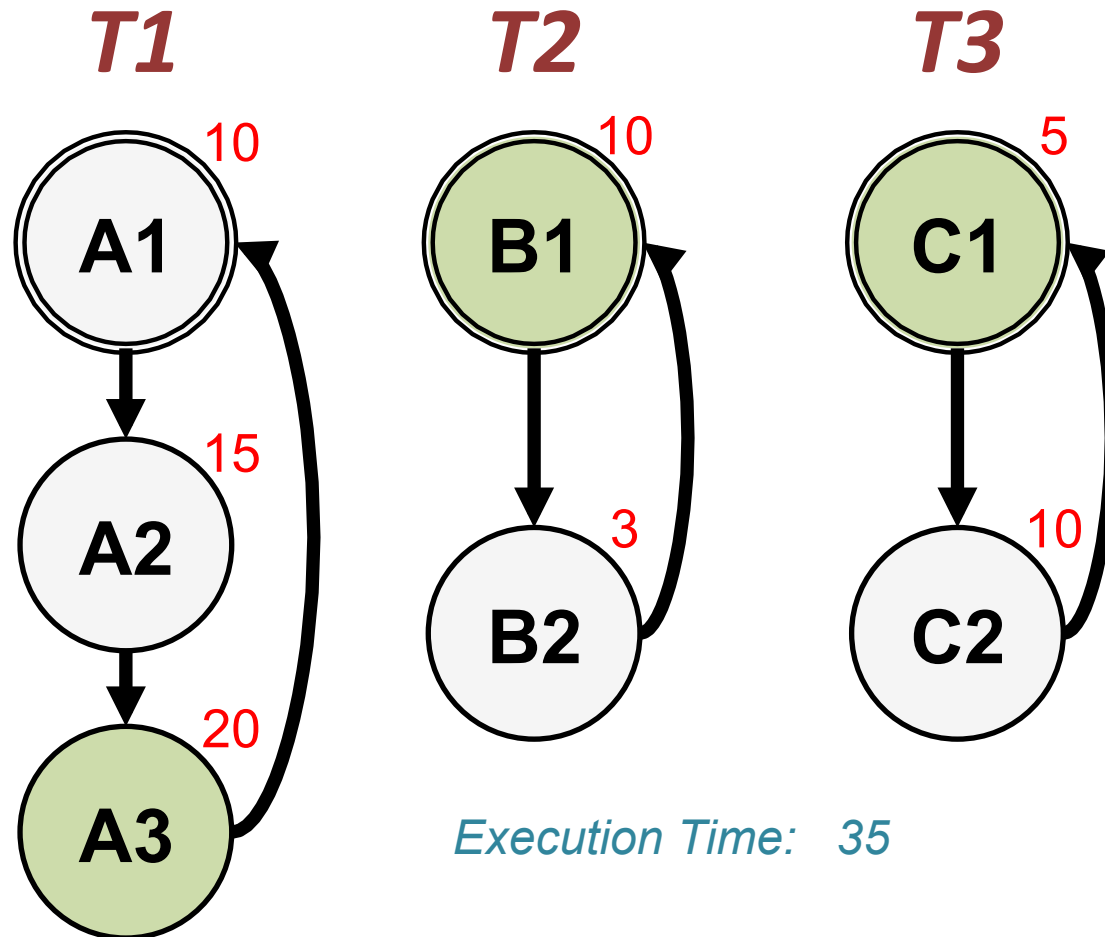
Motivating example



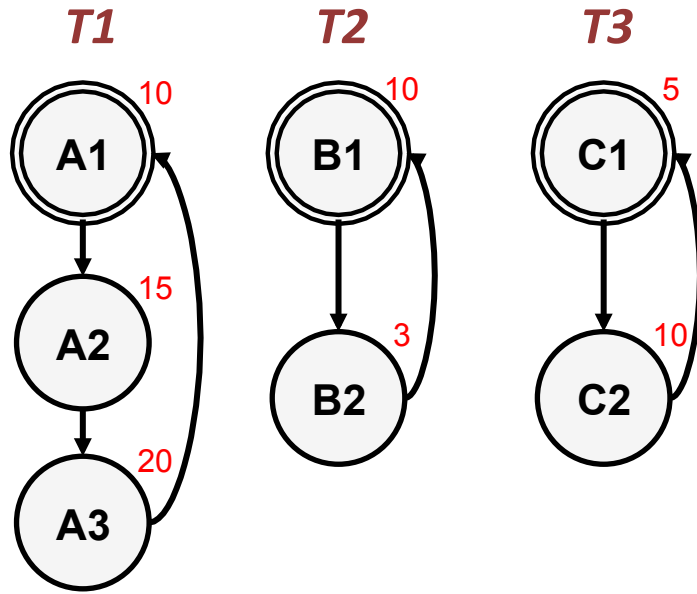
Motivating example



Motivating example



Motivating example



WCRT analysis

-Max-Plus

$$WCRT = \text{Max}(T1) + \text{Max}(T2) + \text{Max}(T3)$$

$$= A3 + B1 + C1$$

Tick alignment

-State Exploration

$$A1+B1+C1 = 25$$

$$A2+B2+C2 = 28$$

$$A3+B1+C1 = 35$$

$$A1+B2+C2 = 23$$

$$A2+B1+C1 = 30$$

$$A3+B2+C2 = 33$$

$$WCRT = \text{Max}(25, 28, 35, 23, 30, 33)$$

$$= 35 \text{ cycles}$$

Scalability

Conventional approaches

- Plus-max

Sum the largest execution time of
each thread



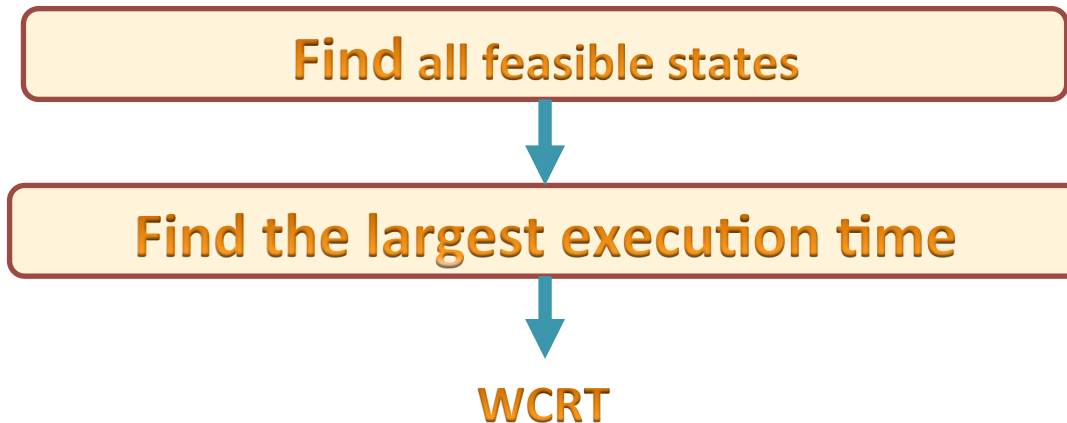
WCRT


M. Boldt and C. Traulsen and R. Hanxleden. *Worst Case Reaction Time Analysis of Concurrent Reactive Programs*. ENTCS, 203(4), 2008.

L. Ju, B. K. Huynh, A. Roychoudhury, and S. Chakraborty. *Performance debugging of Esterel specifications*. CODES-ISSS 2008.


Conventional approaches

- State exploration

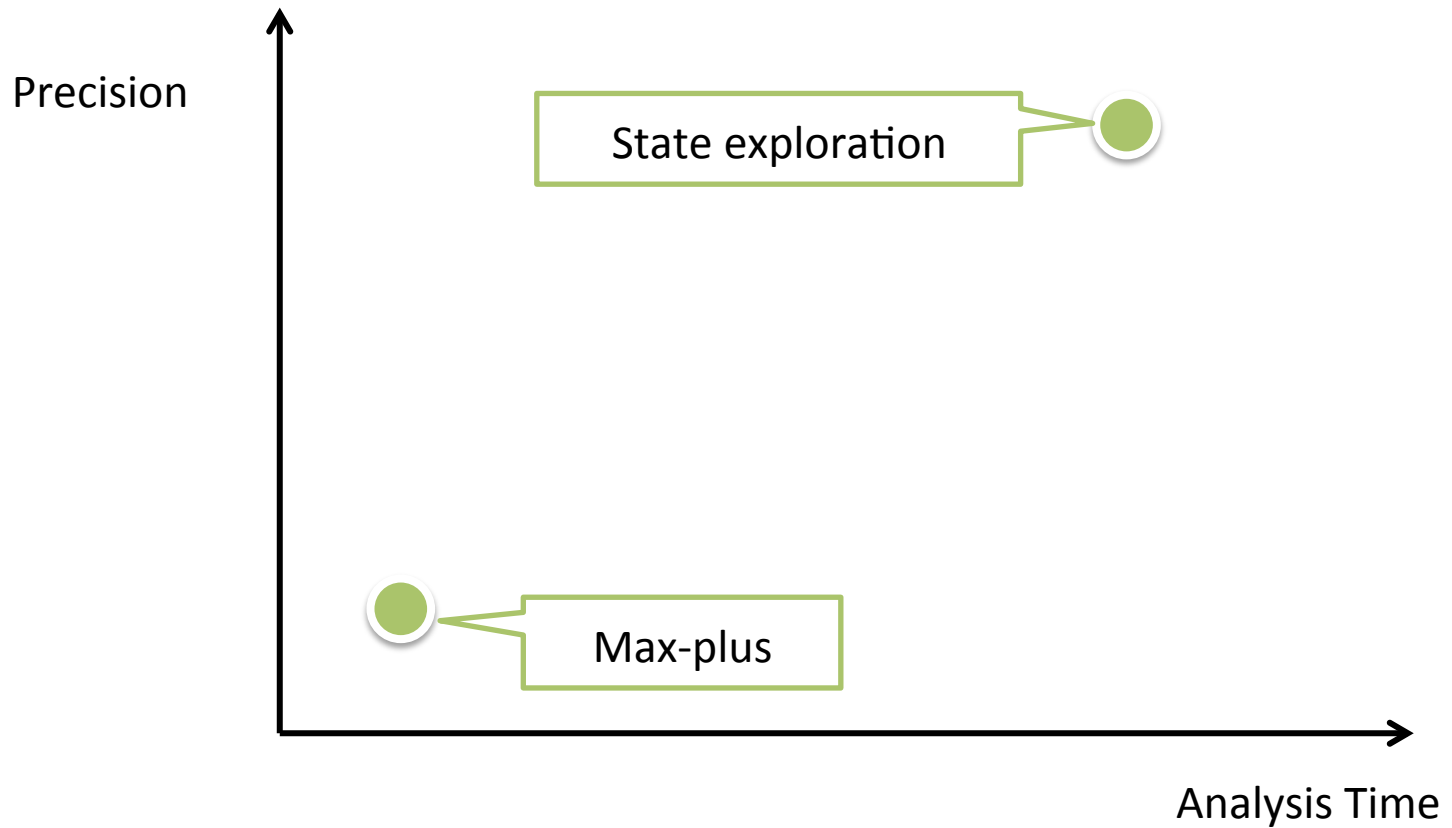


L. Ju, B. K. Huynh, S. Chakraborty, and A. Roychoudhury. *Context-sensitive timing analysis of Esterel programs*. *DAC*, 2014. 

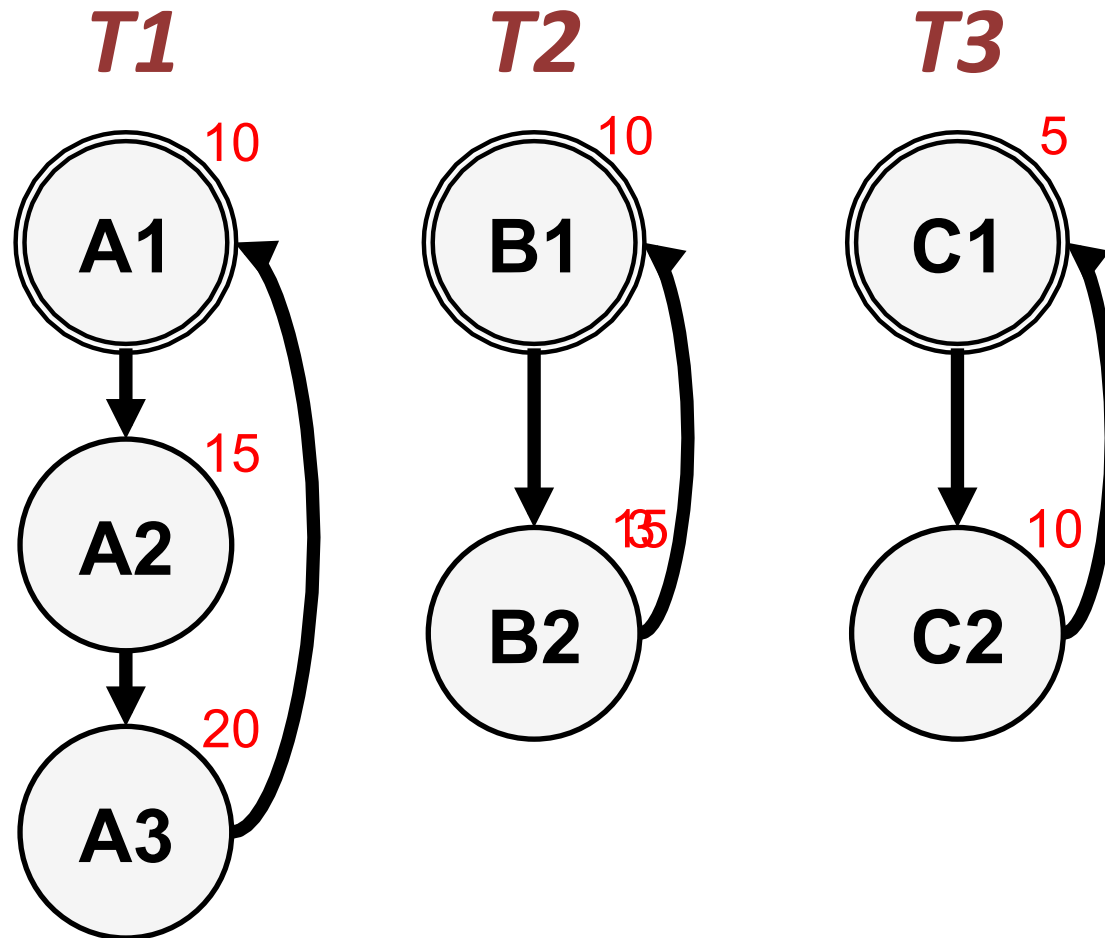
S. Andalam, P. S. Roop, and A. Girault. *Pruning infeasible paths for tight WCRT analysis of synchronous programs*. *DATE*, 2015. 

M. Kuo, R. Sinha, and P. S. Roop. *Efficient WCRT analysis of synchronous programs using reachability*. *DAC*, 2016. 

Trade-off

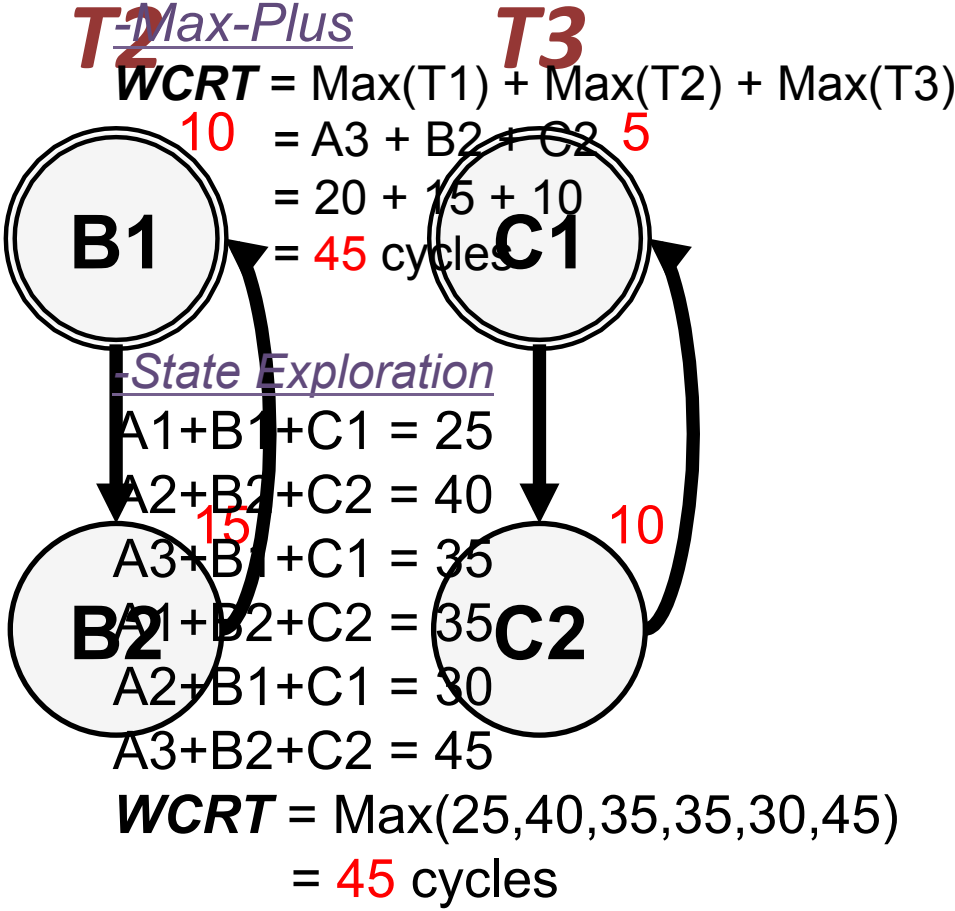
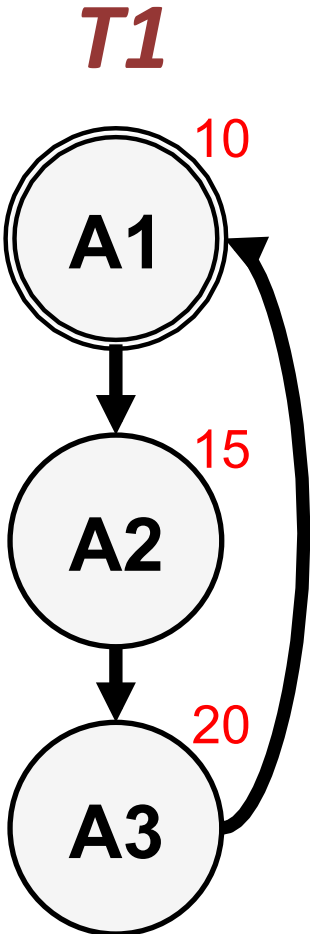


Motivating example

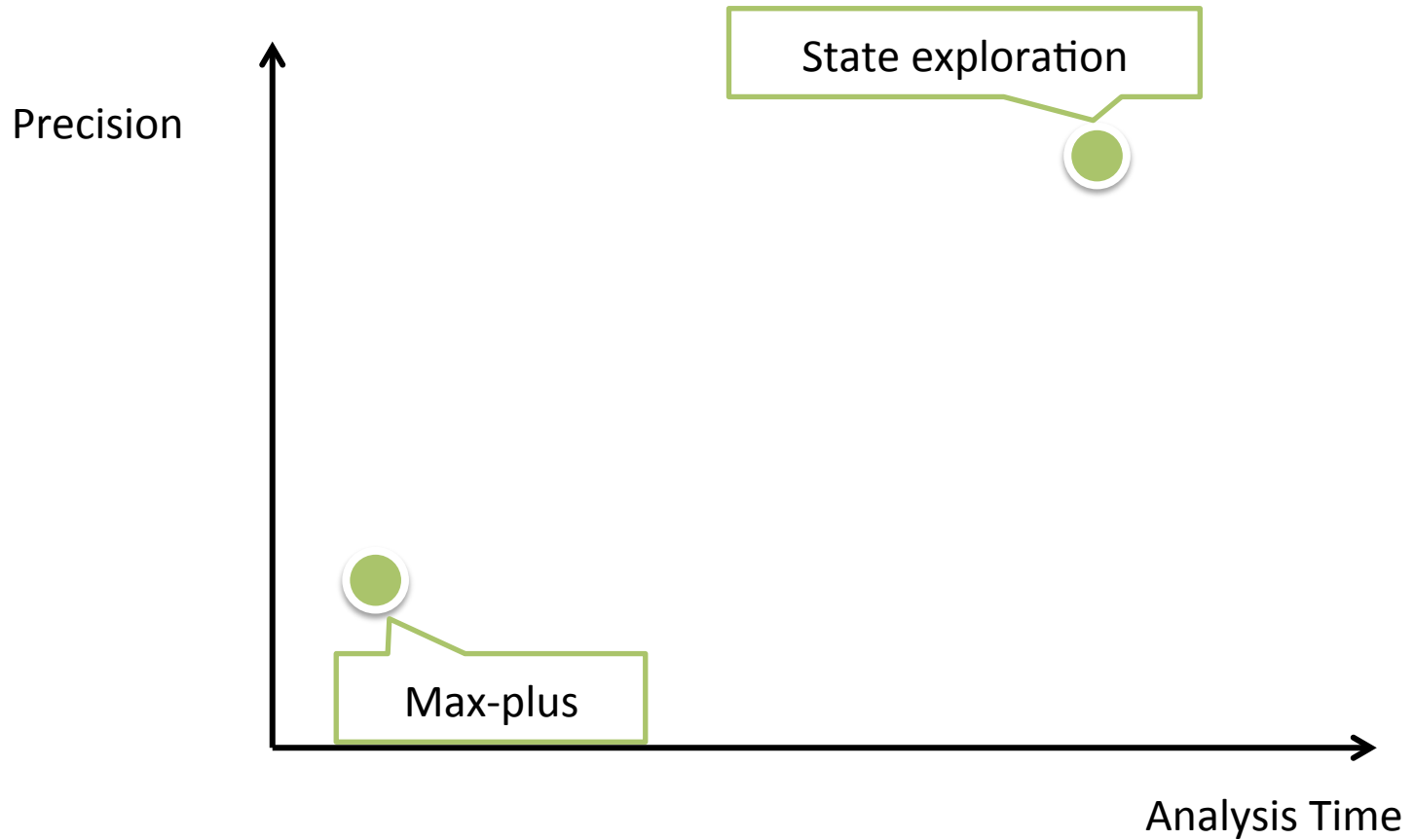


Motivating example

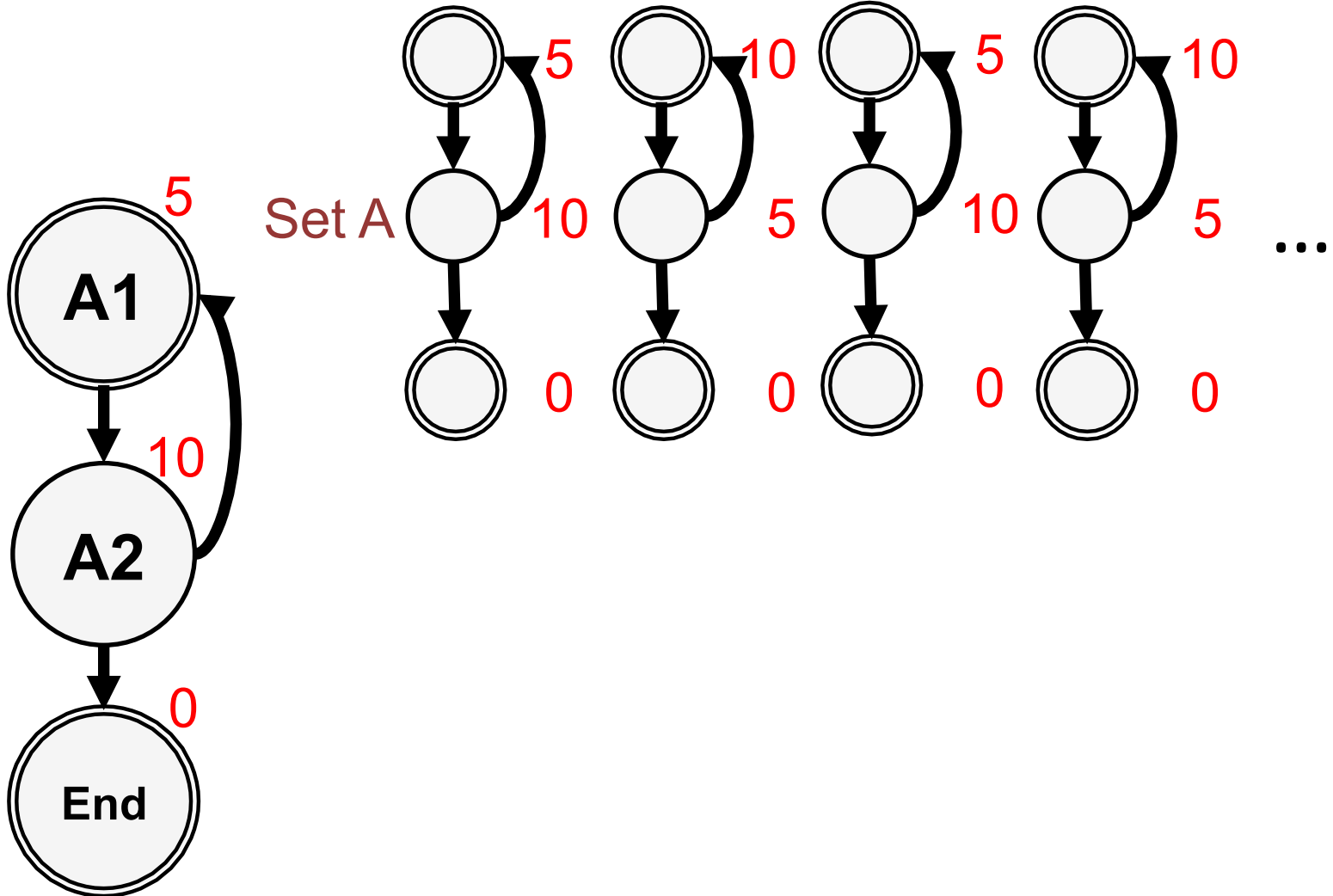
WCRT analysis



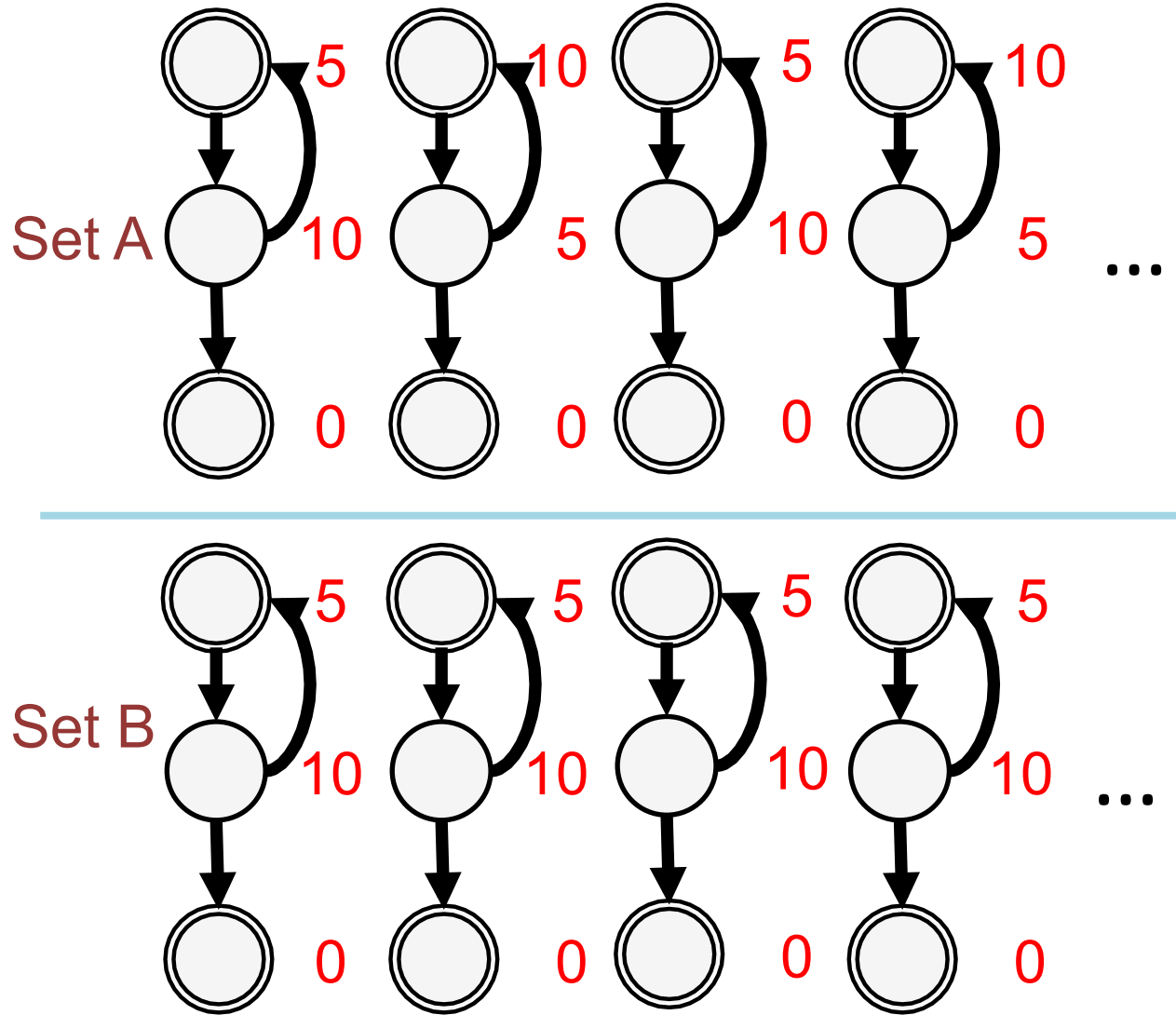
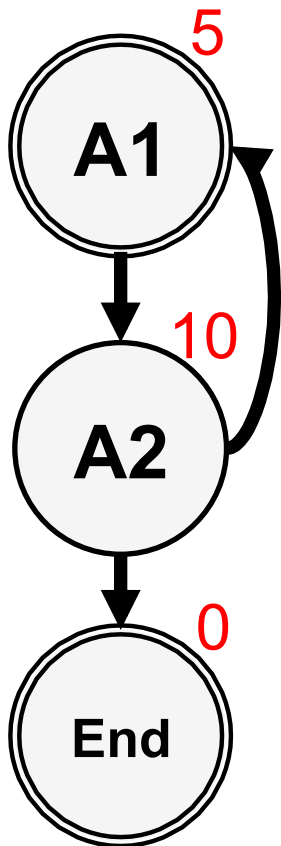
Trade-off



Synthetic examples

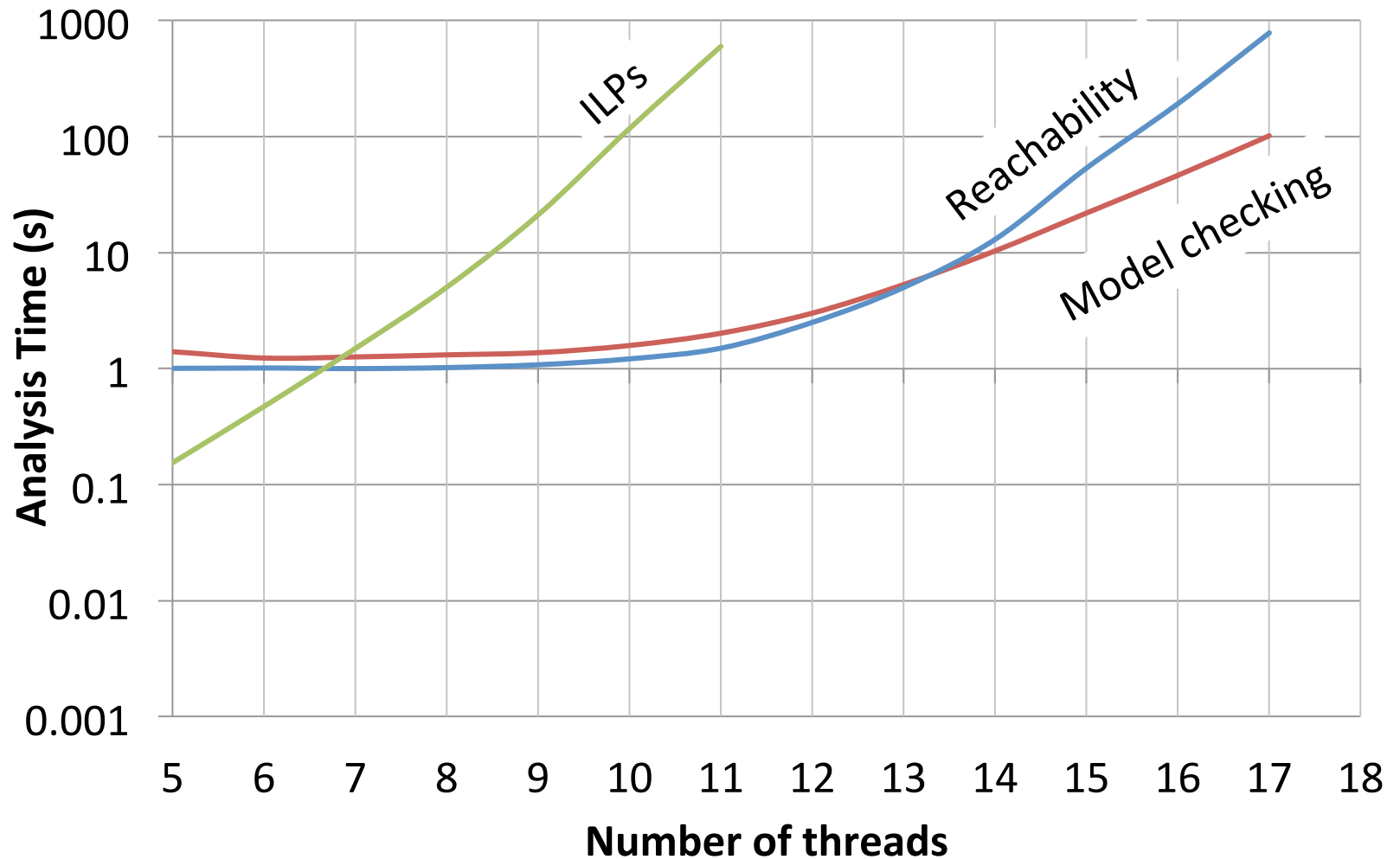


Two sets



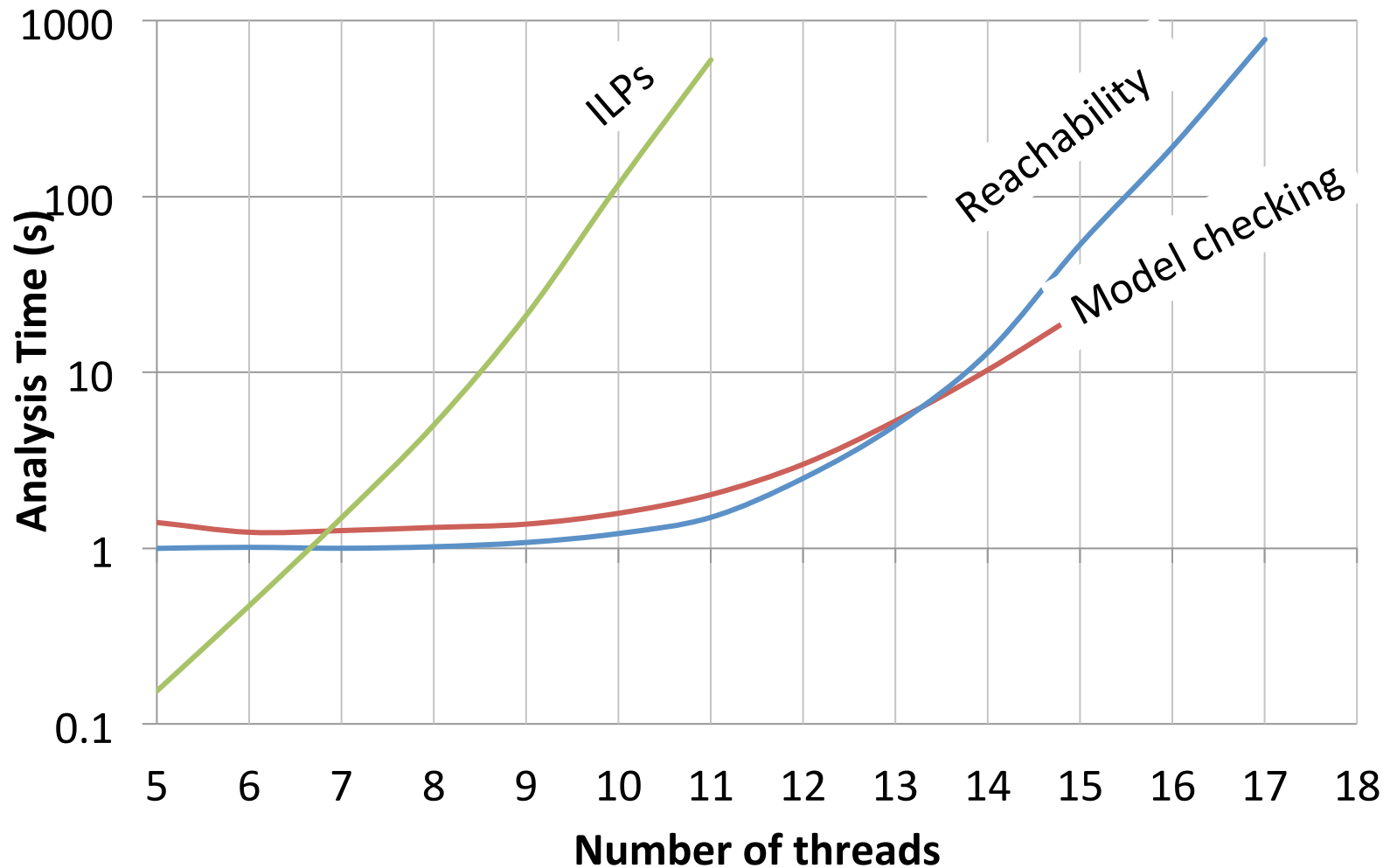
Comparing state-exploration techniques

Set A



Comparison contd.

Set B

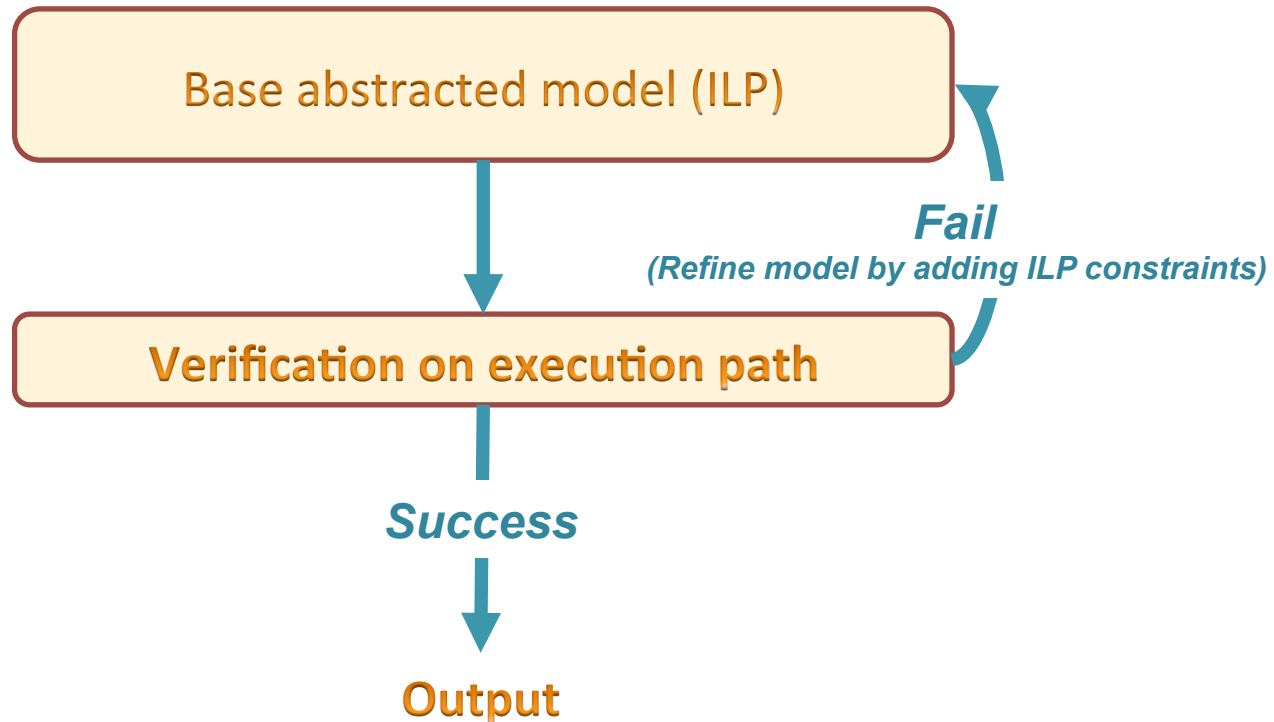


Observations

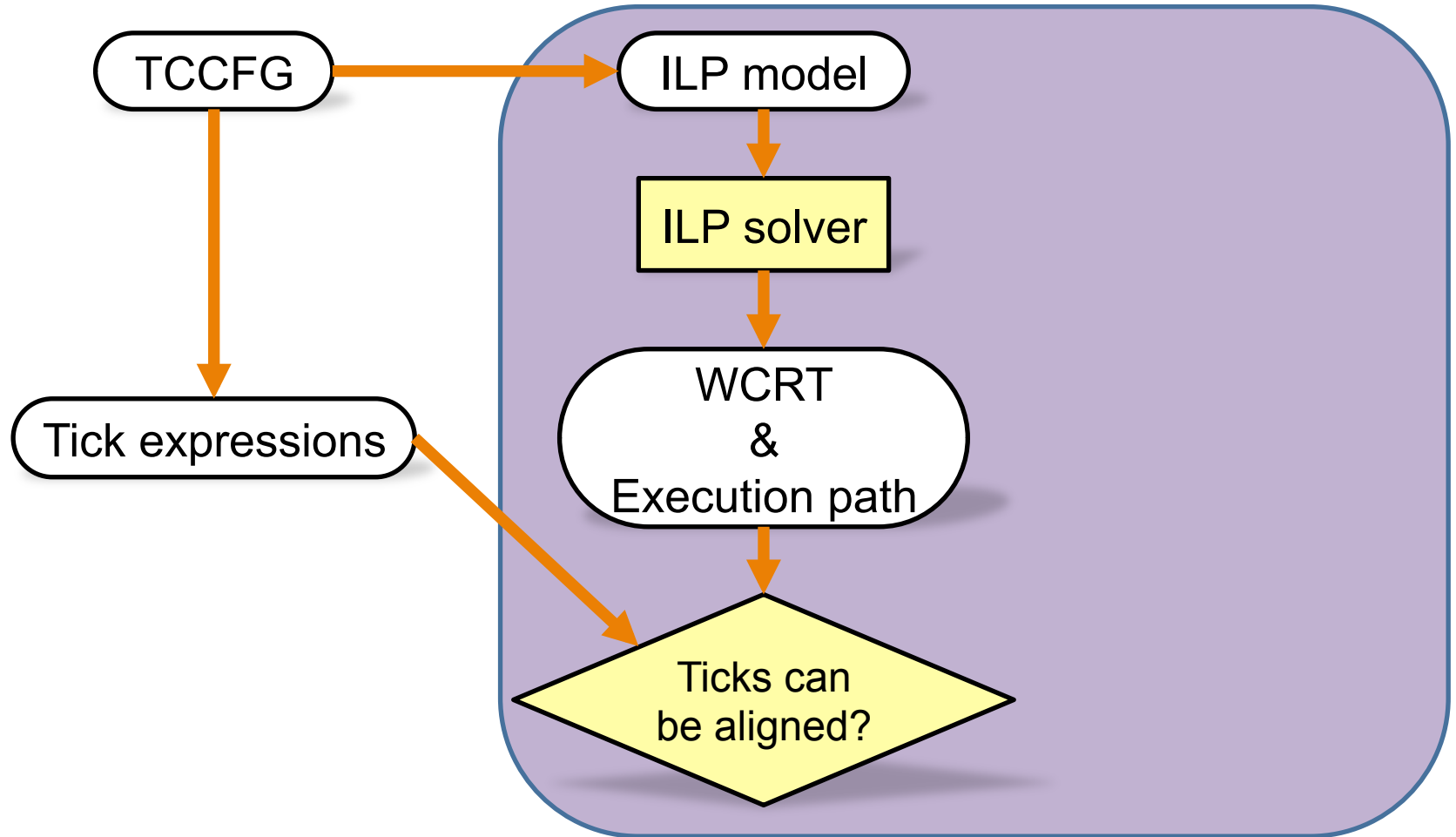
- Longer analysis time does not necessarily translate into better precision.
- Time Complexity: **EXPONENTIAL**
 $\Theta(n \text{ lcm}(\phi_1, \dots, \phi_n))$.
- Similar problem exists for model checking. However, there are algorithms such as CEGAR [Clarke et al, JACM'03] that work well in practice.
- Refine to remove spurious counter examples.

Proposal

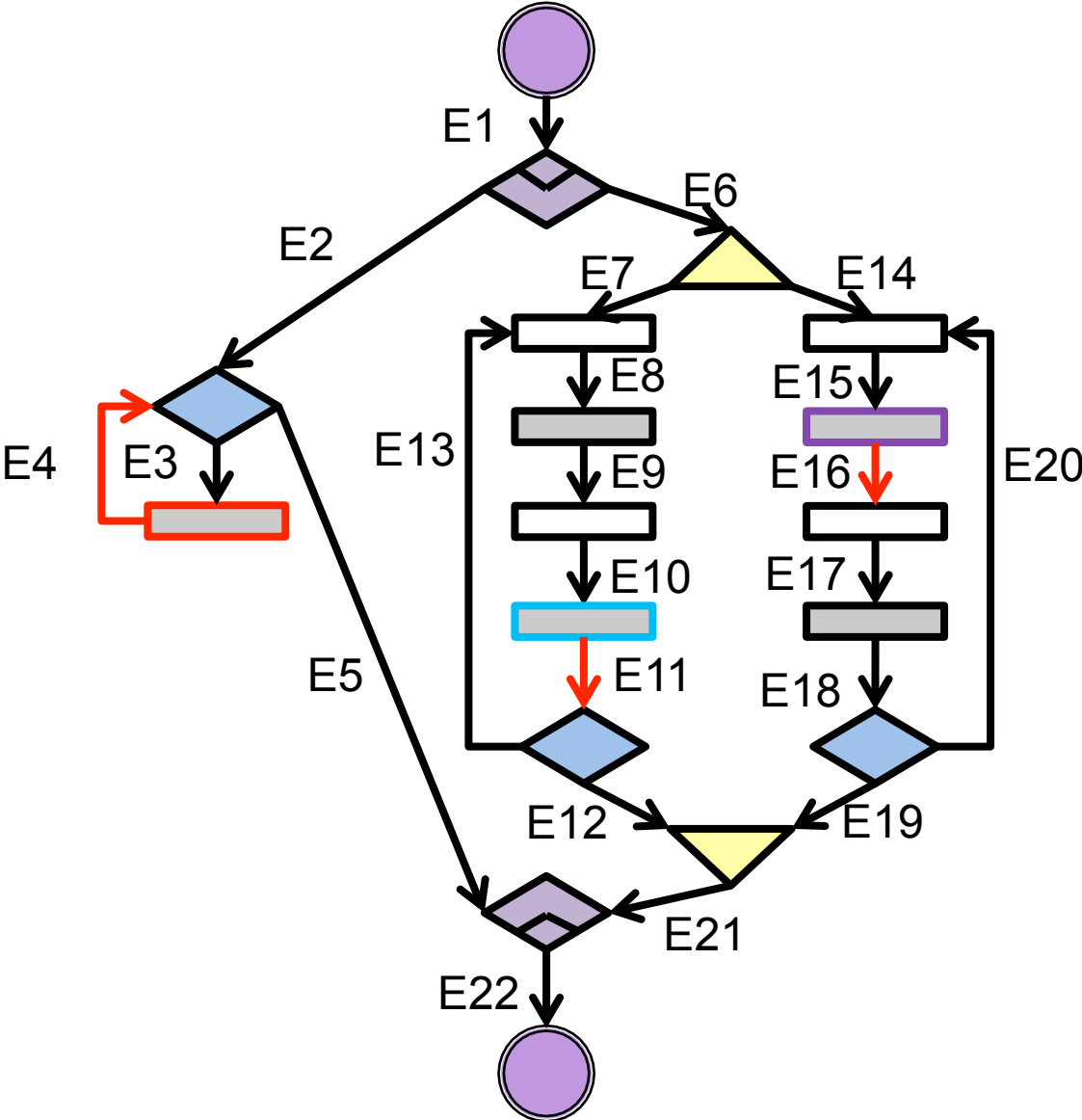
- A scalable and extendable timing analysis framework (ILPc)



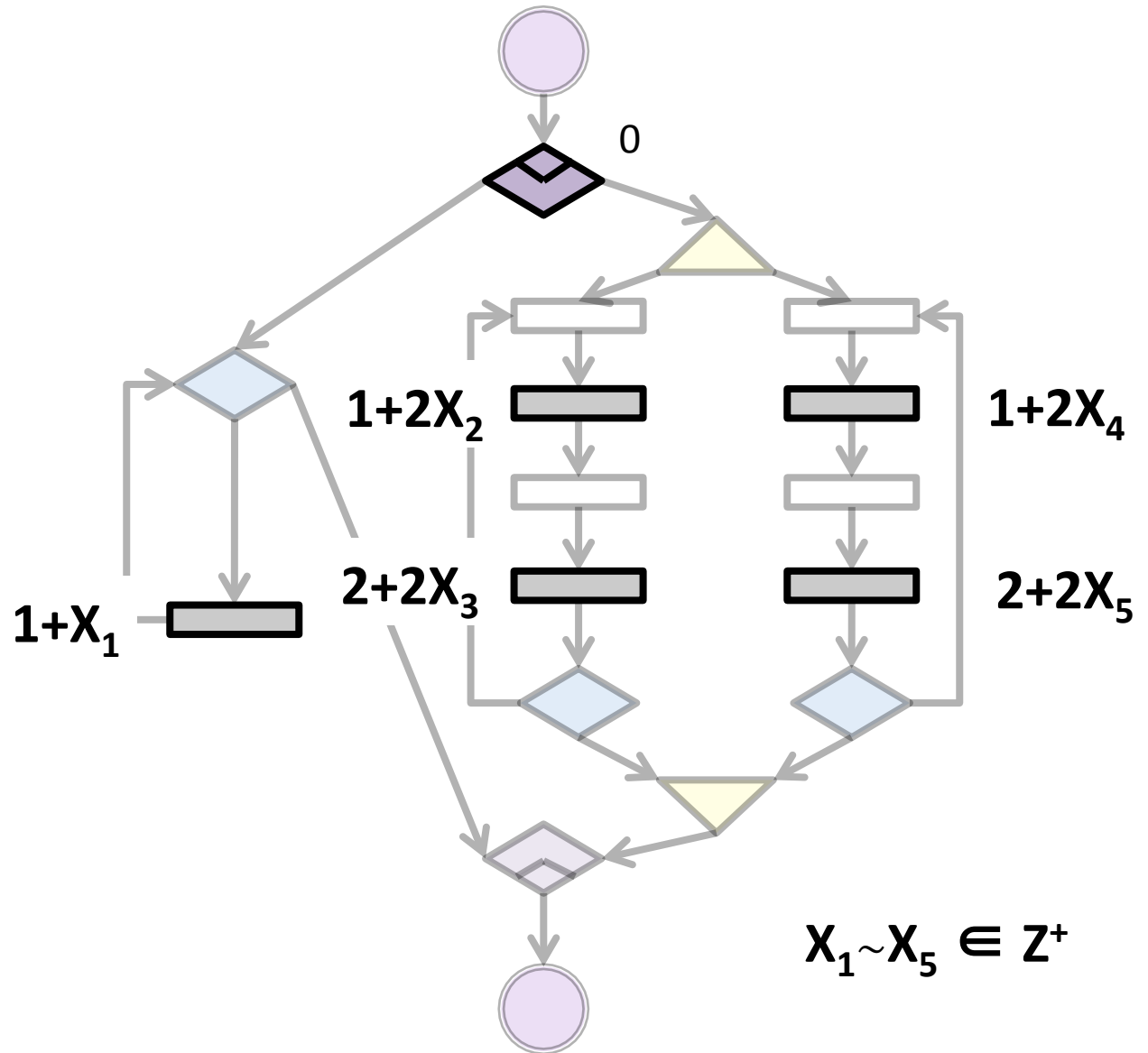
Overview of ILPc



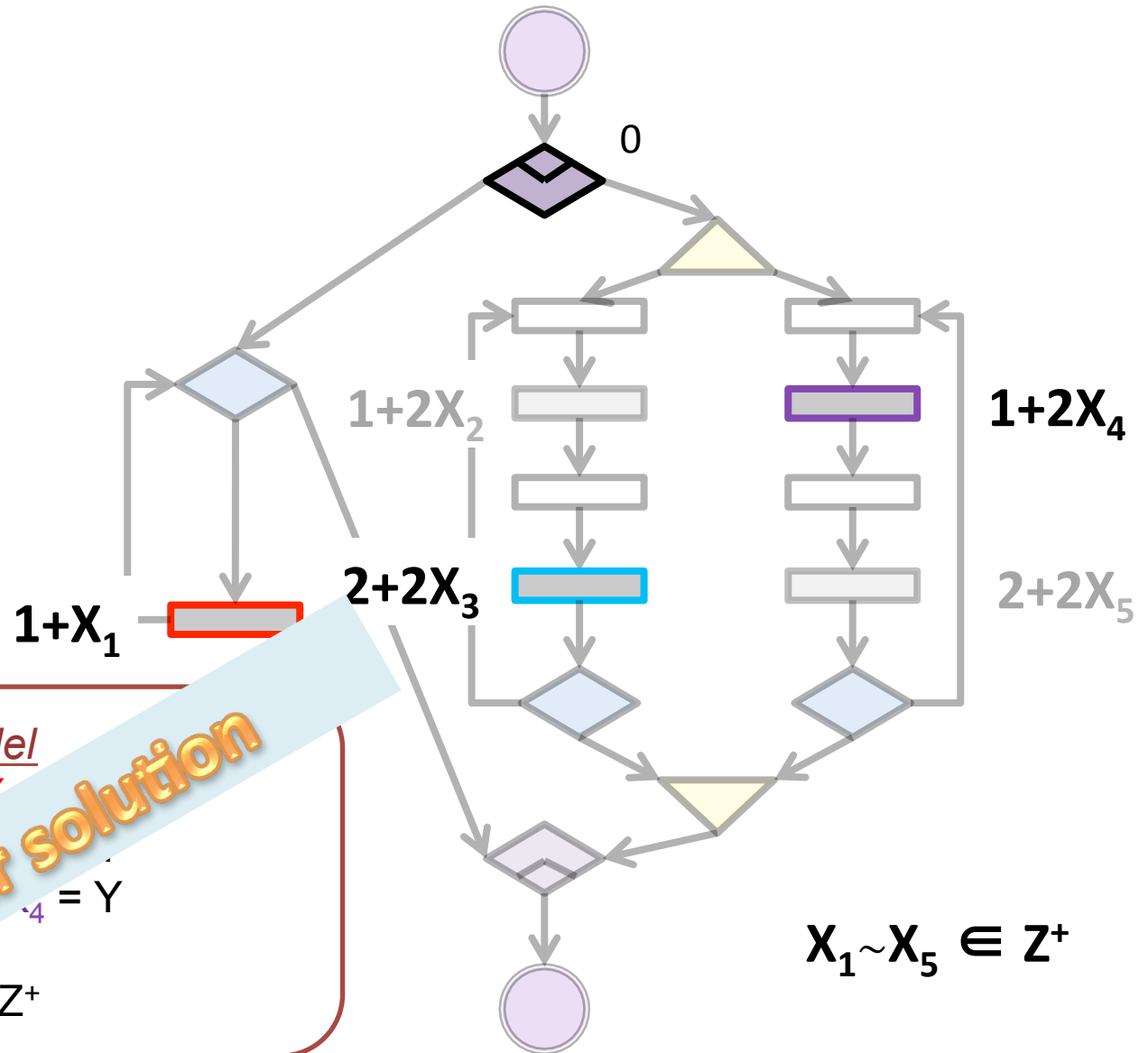
Base ILP model produces a path



Verifying tick alignment



Verifying tick alignment

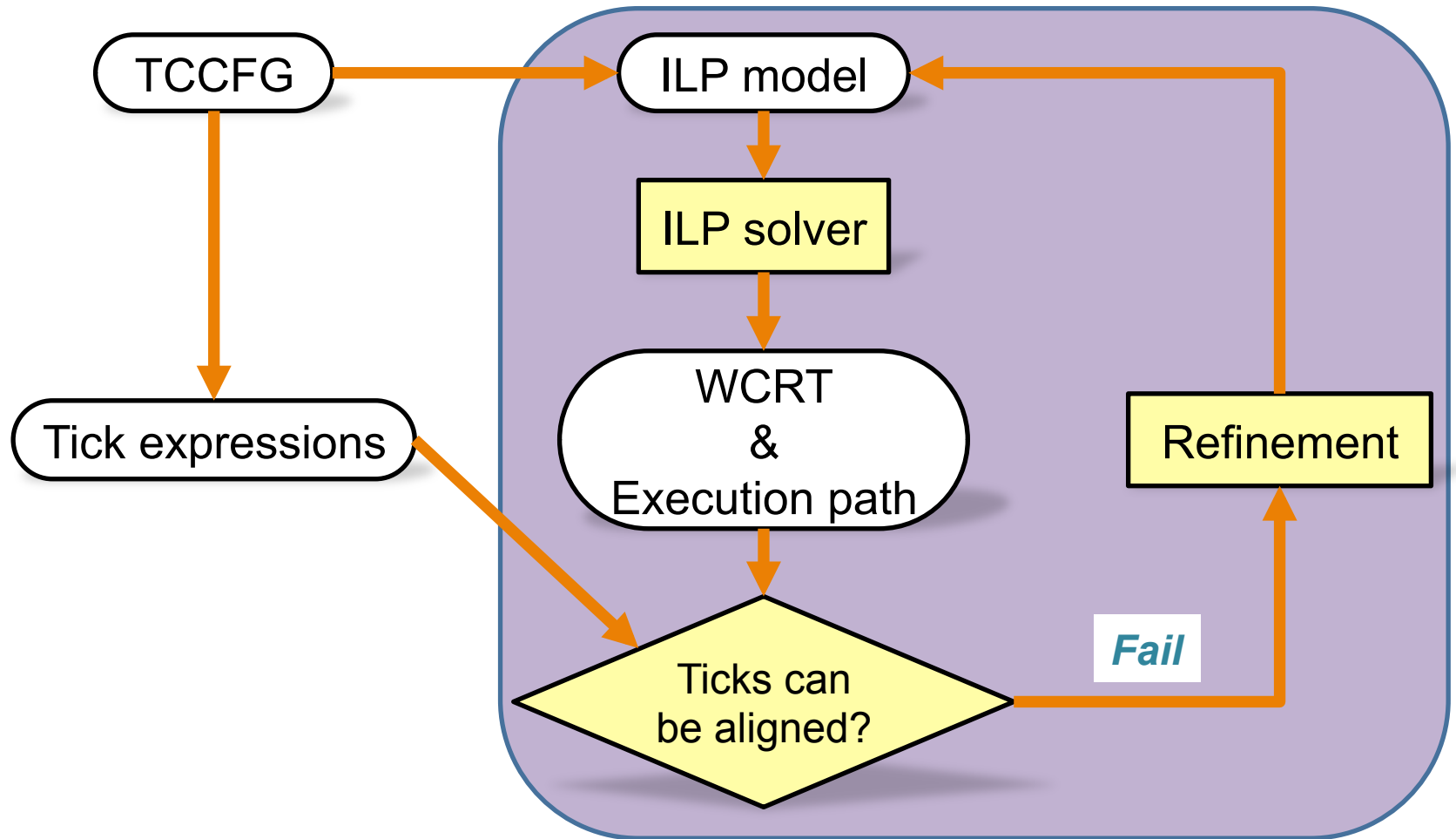


No integer solution

ILP model
 $1 + X_1 + \dots = Y$
 $Y \in \mathbb{Z}^+$

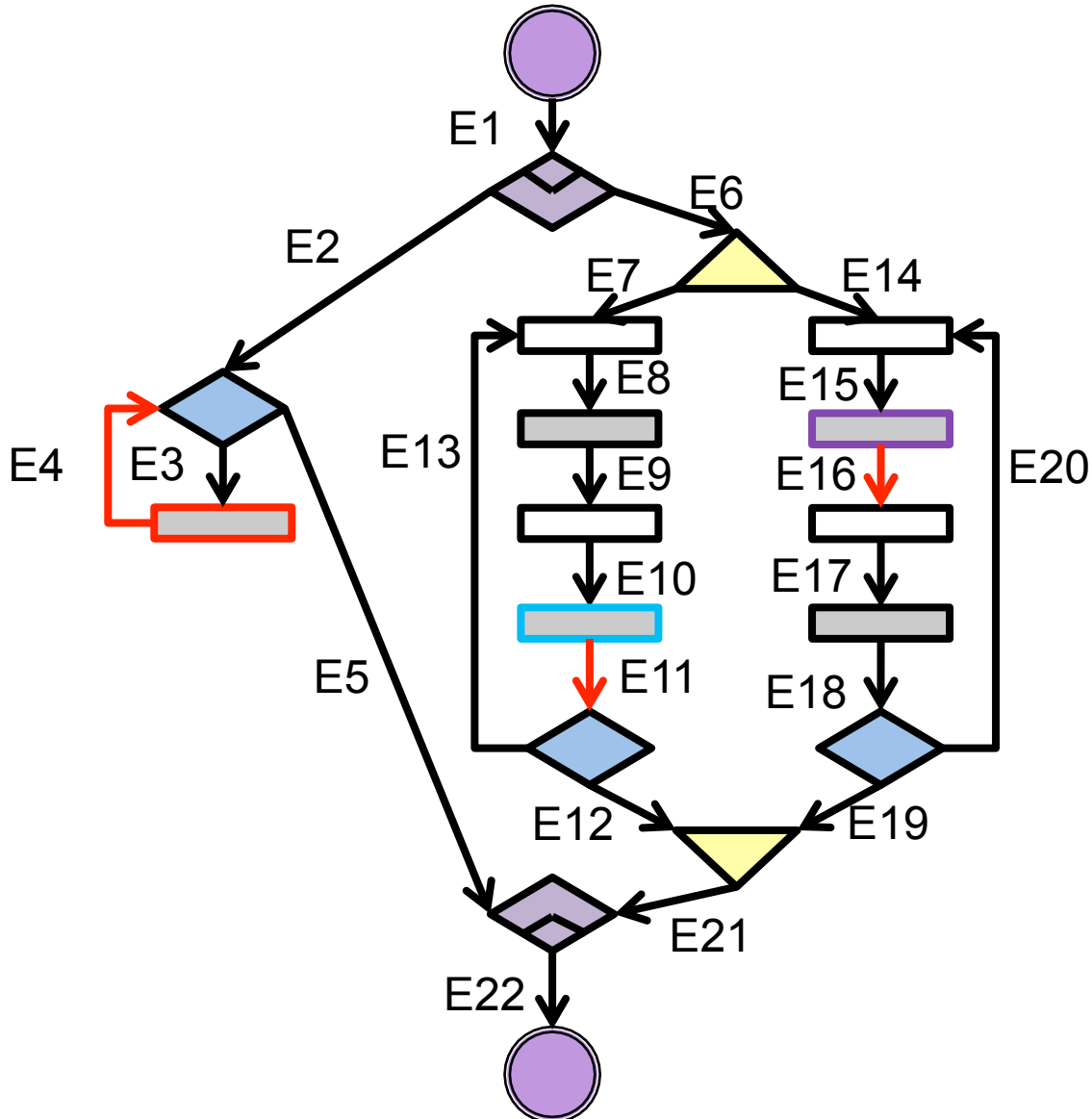
$X_1 \sim X_5 \in \mathbb{Z}^+$

Overview of ILPc

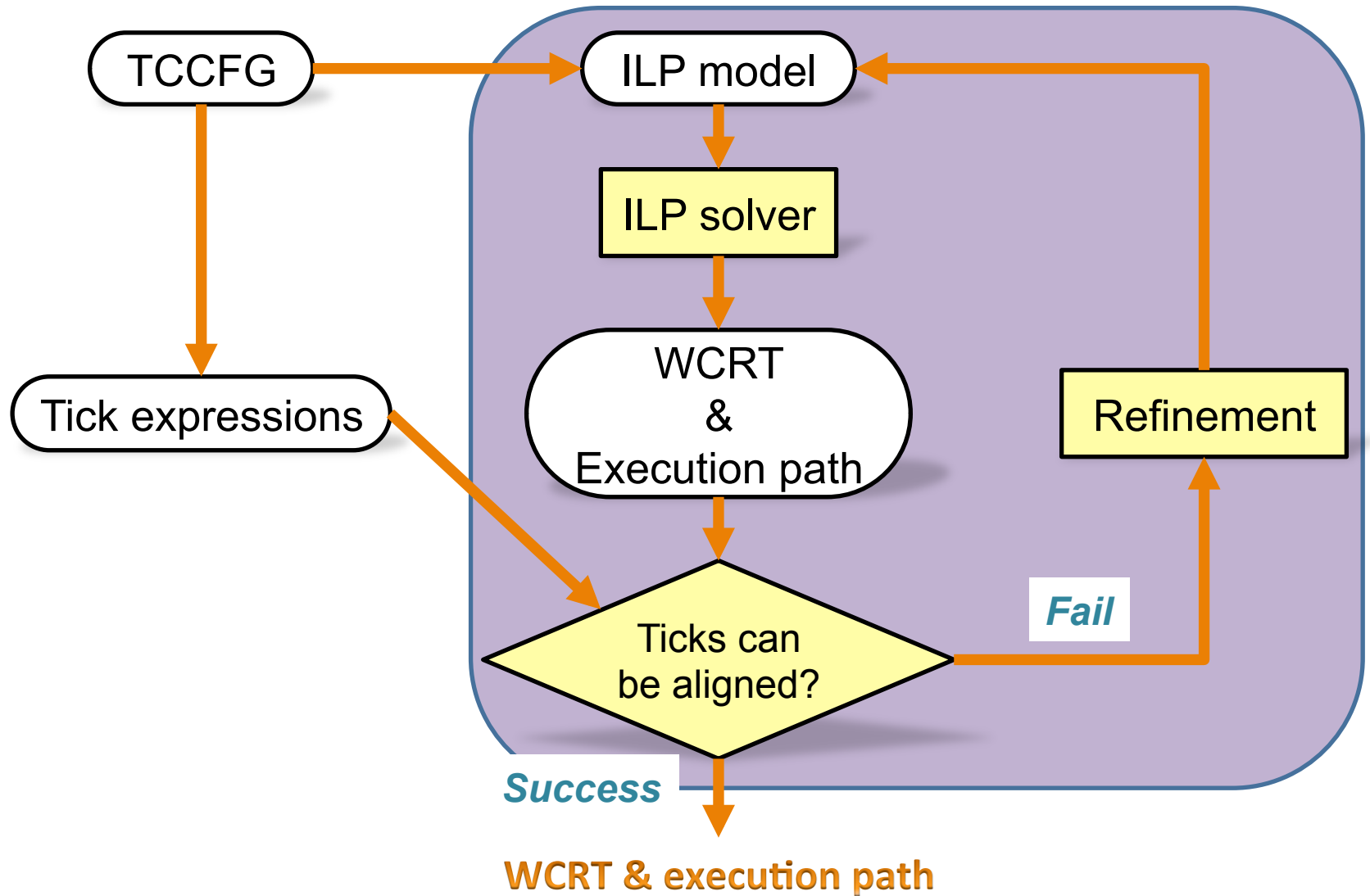


Refinement

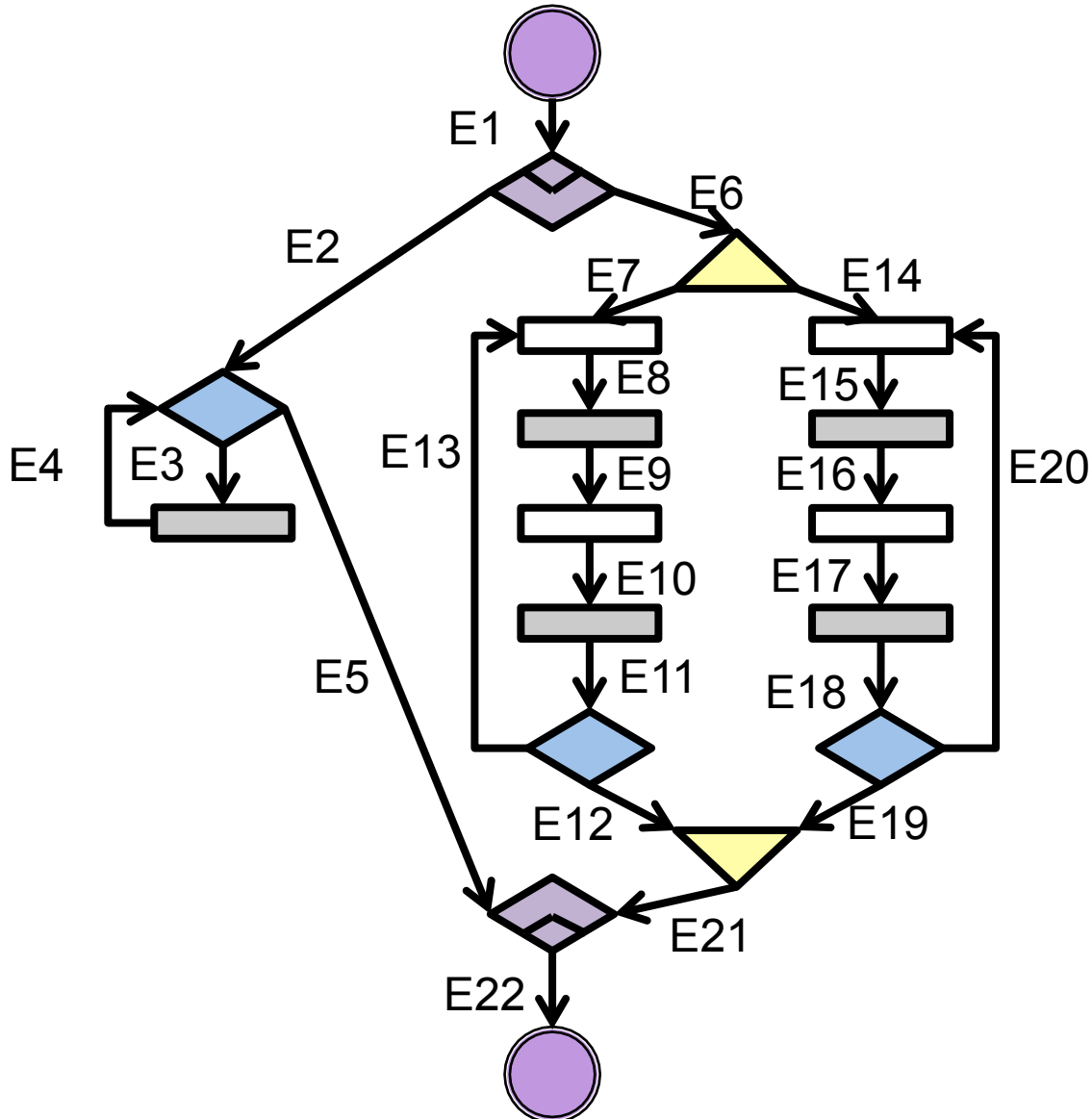
$$E4 + E11 + E16 \leq 2$$



Overview of ILPc



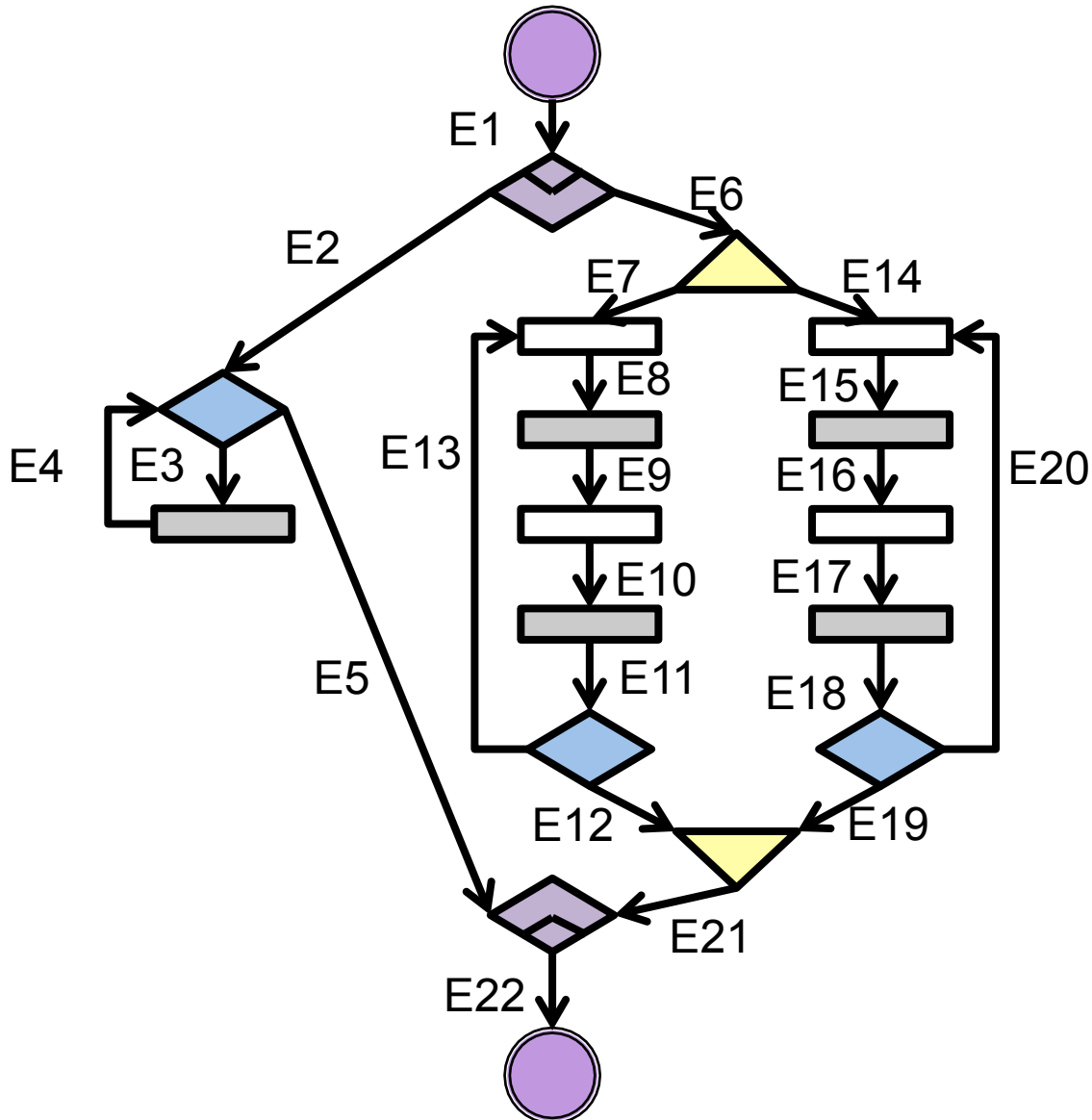
ILP model



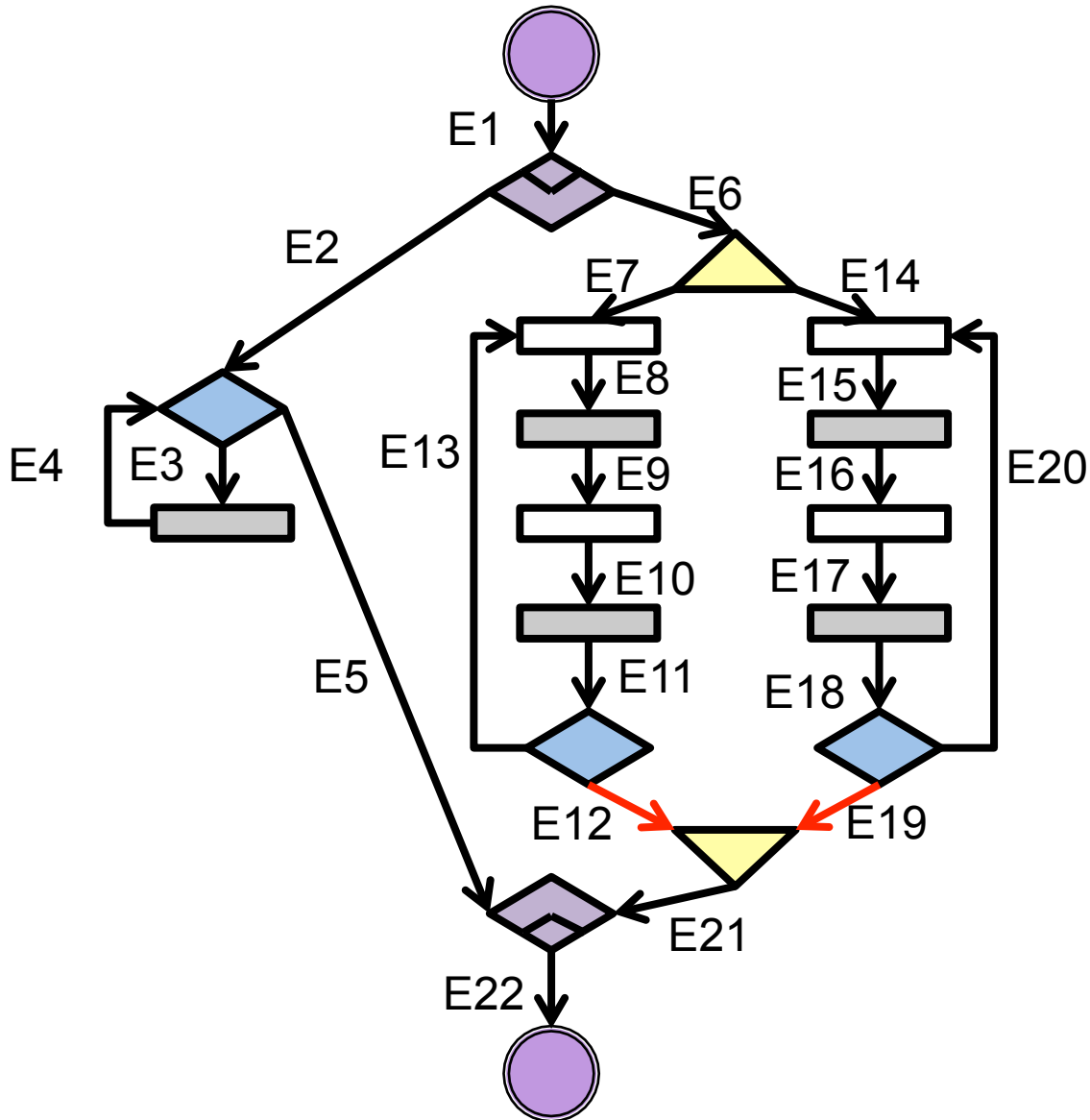
ILP model

Objective function:

$$obj = \sum C_i \times E_i$$



ILP model

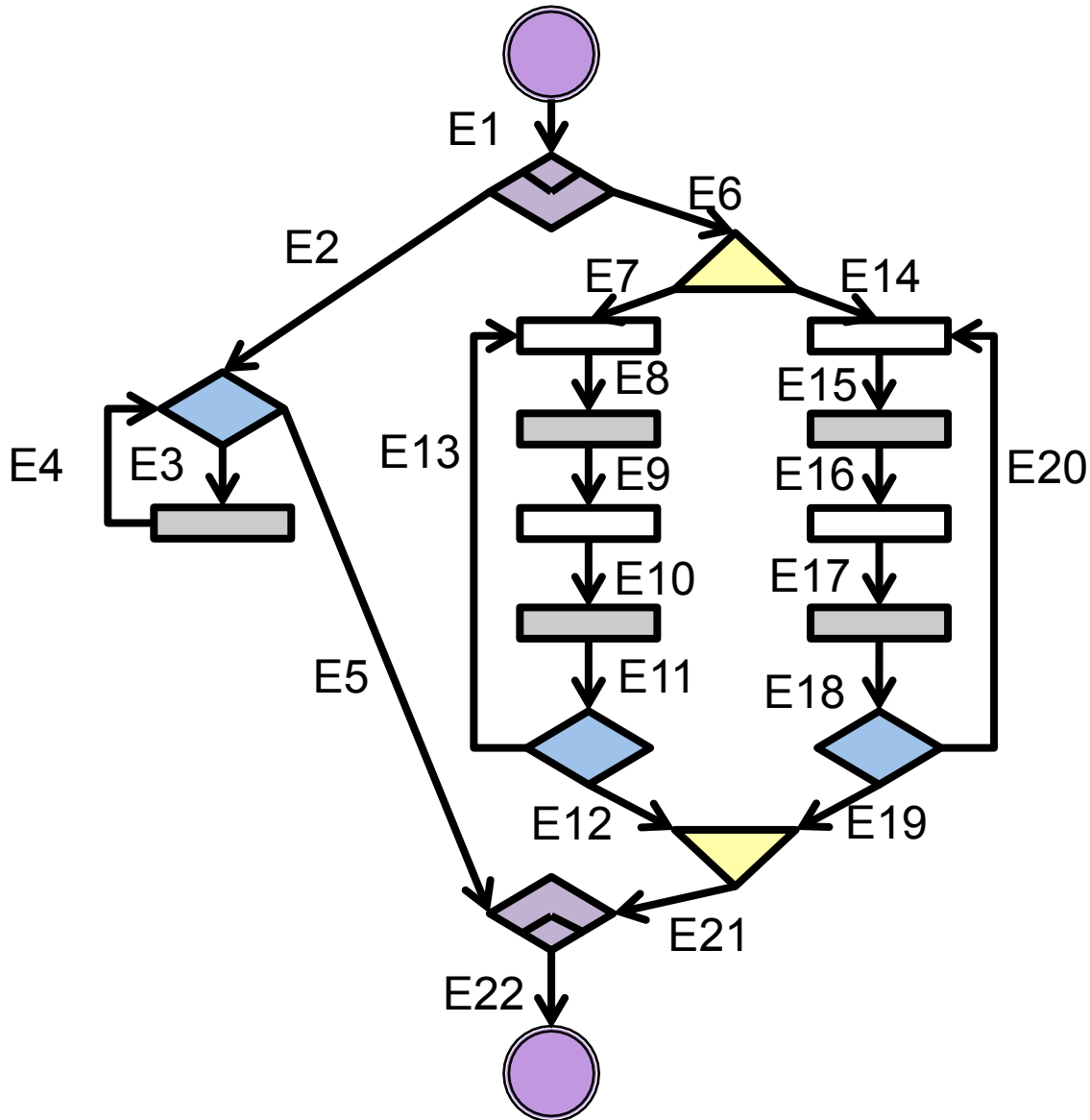


Objective function:

$$obj = \sum C_i \times E_i$$

Execution cost occur upon exiting a node

ILP model

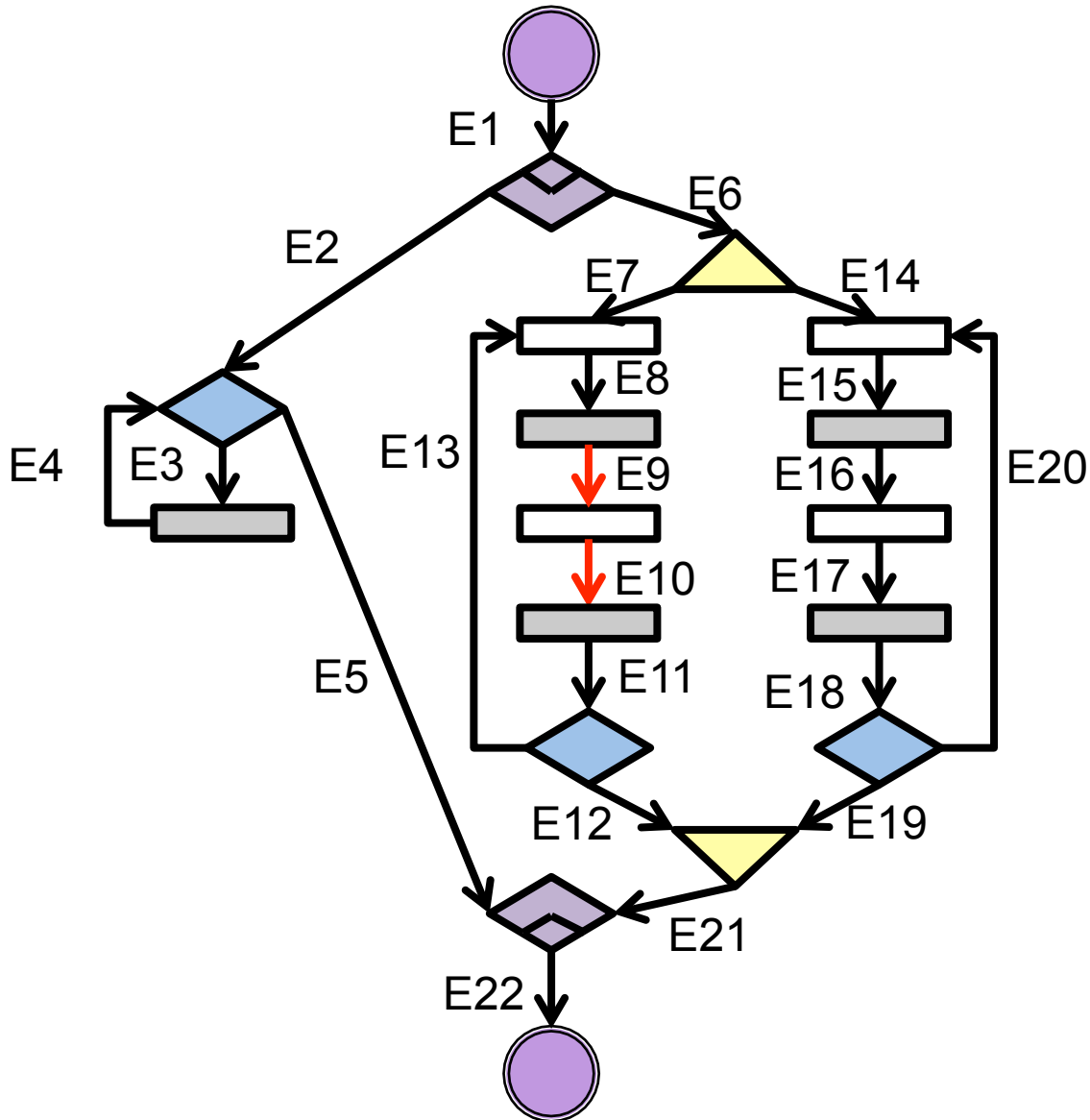


Objective function:

$$obj = \sum C_i \times E_i$$

Conventional nodes:

ILP model



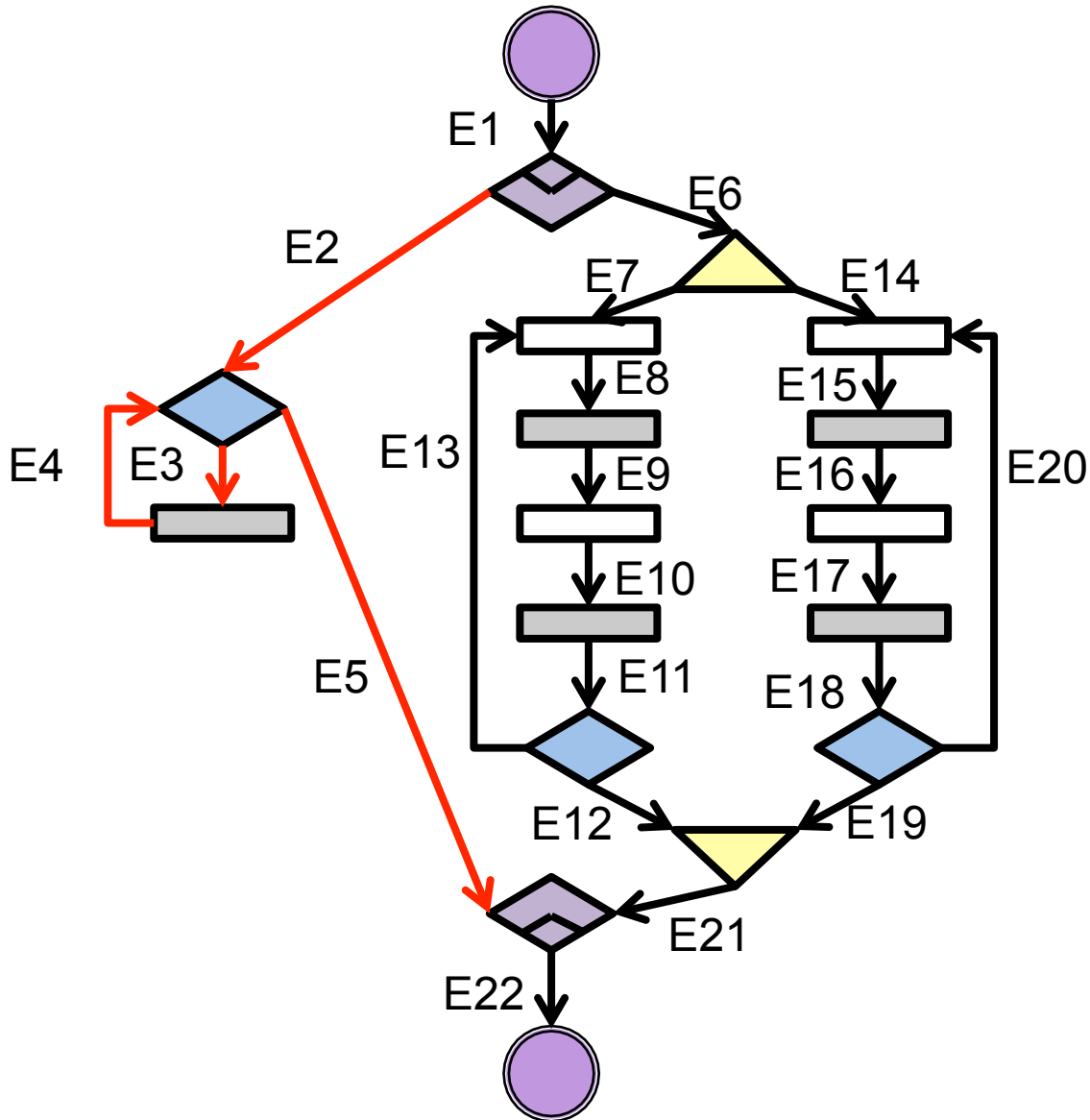
Objective function:

$$obj = \sum C_i \times E_i$$

Conventional nodes:

$$E9 = E10$$

ILP model



Objective function:

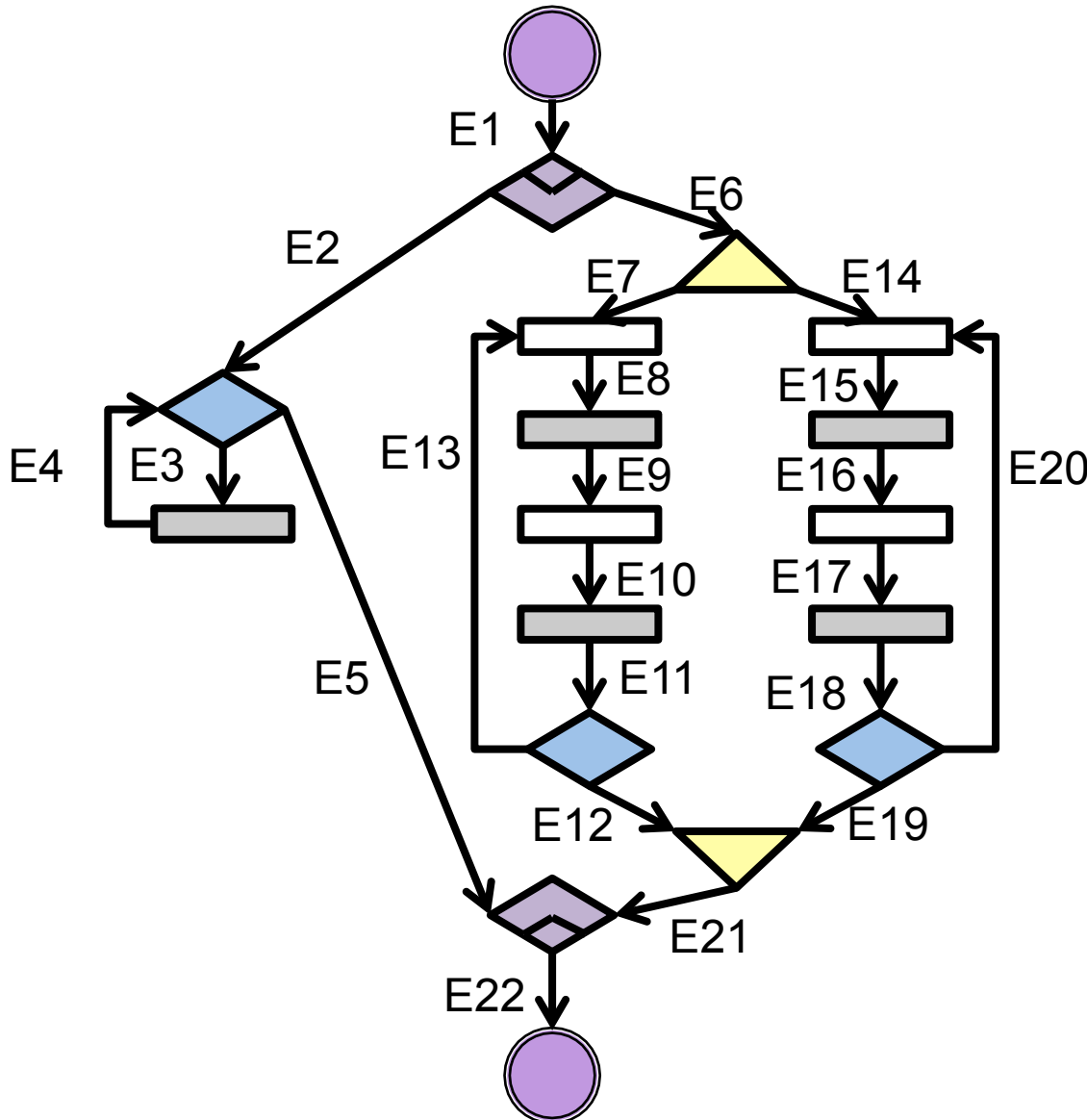
$$obj = \sum C_i \times E_i$$

Conventional nodes:

$$E9 = E10$$

$$E2 + E4 = E3 + E5$$

ILP model



Objective function:

$$obj = \sum C_i \times E_i$$

Conventional nodes:

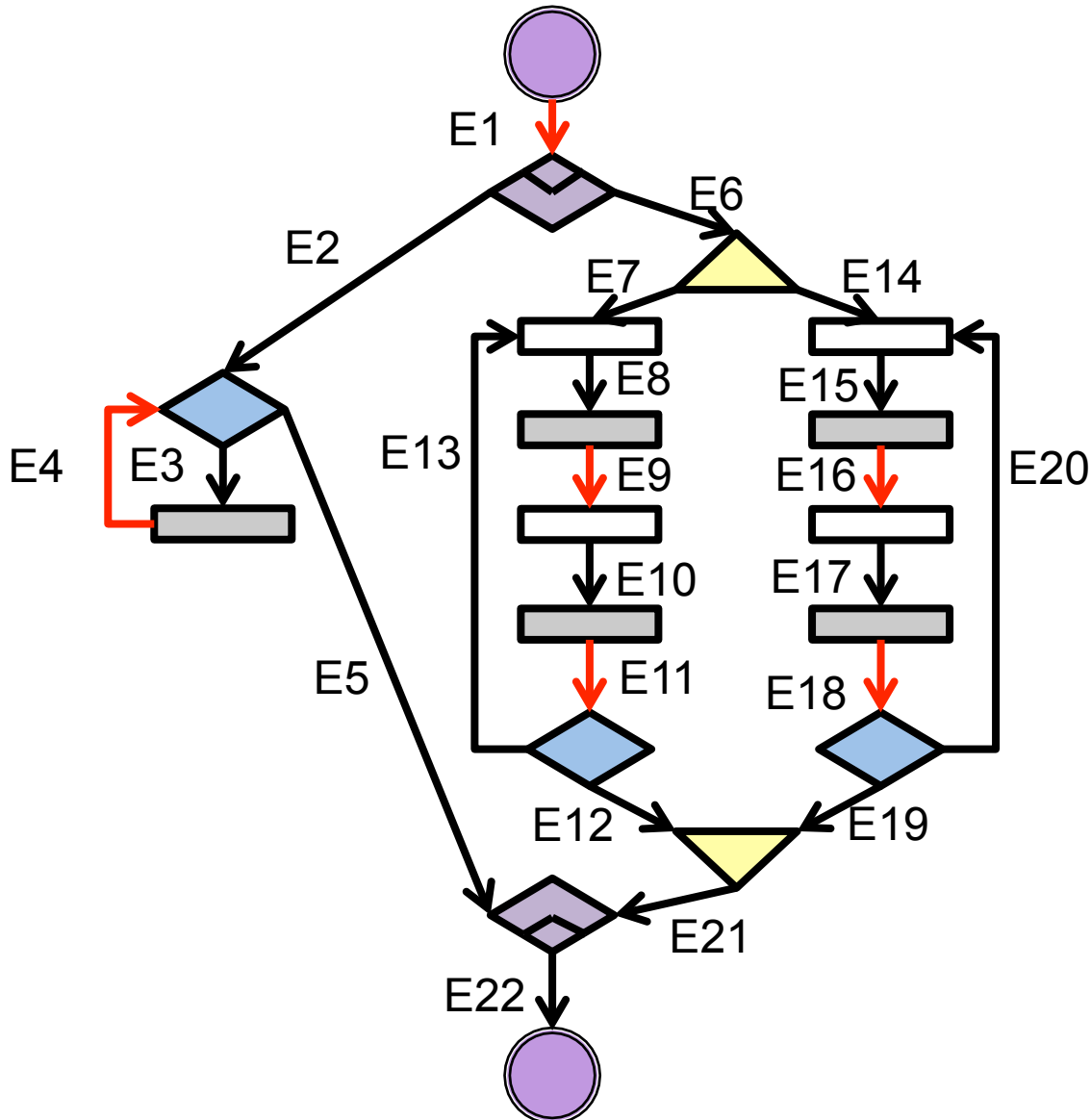
$$E9 = E10$$

$$E2 + E4 = E3 + E5$$

Features:

- $E_i \in \{0,1\}$
- Solver set E_i to 1 whenever is possible
- Inequalities

ILP model



Objective function:

$$obj = \sum C_i \times E_i$$

Conventional nodes:

$$E9 = E10$$

$$E2 + E4 = E3 + E5$$

Features:

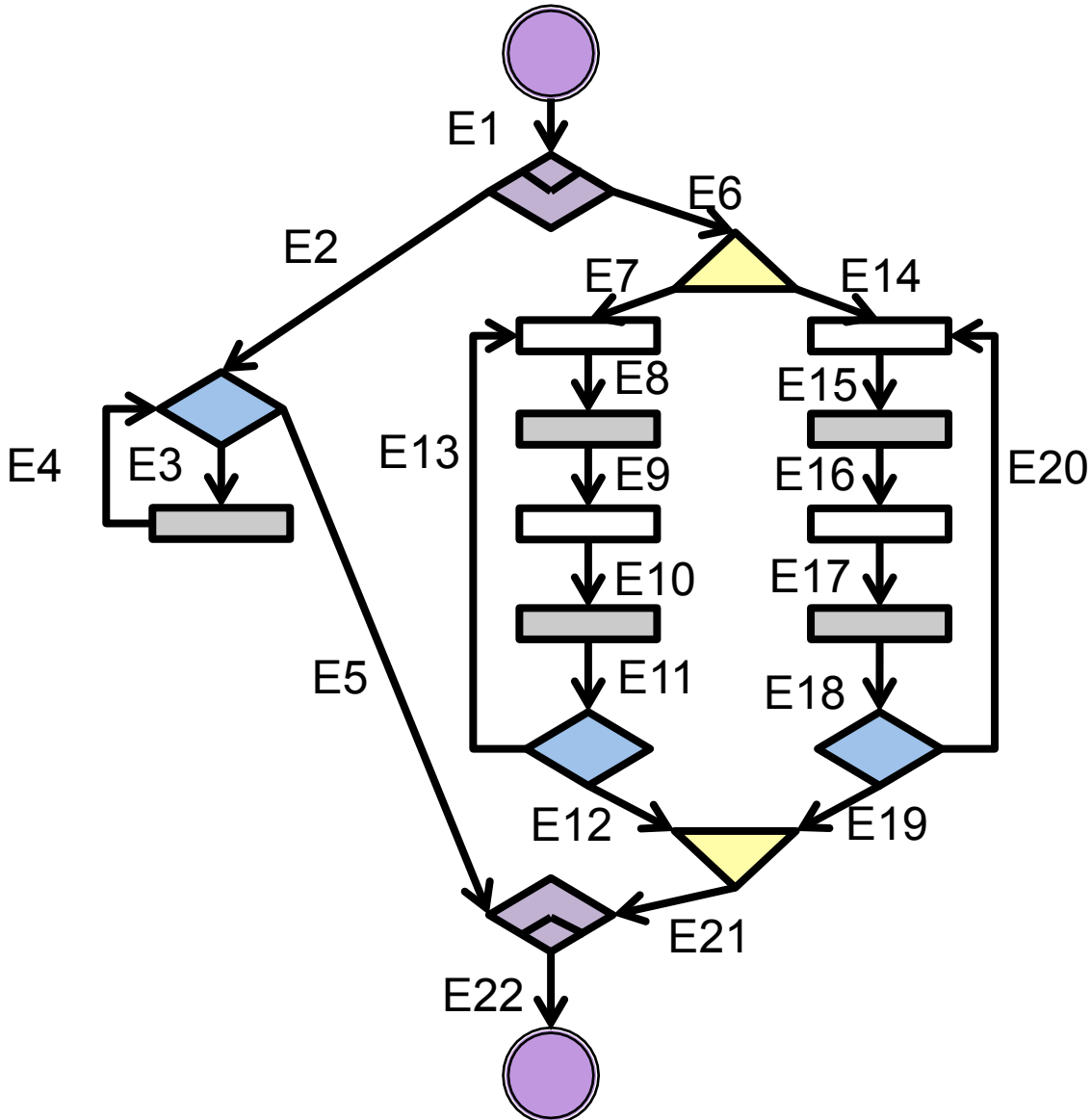
- $E_i \in \{0,1\}$
- Solver set E_i to 1 whenever is possible
- Inequalities

Some special edges:

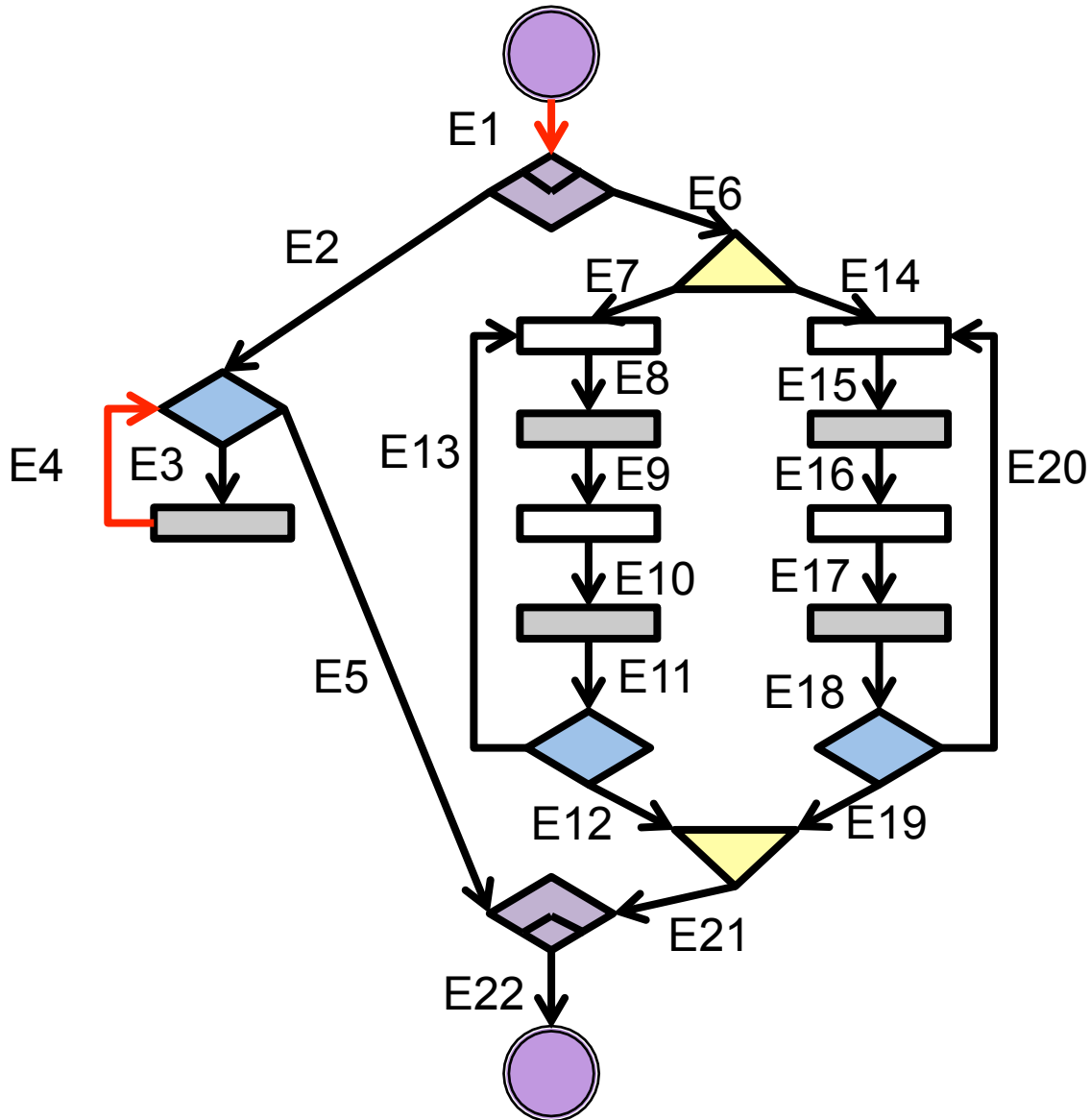
- EOT edges

ILP model

EOT:



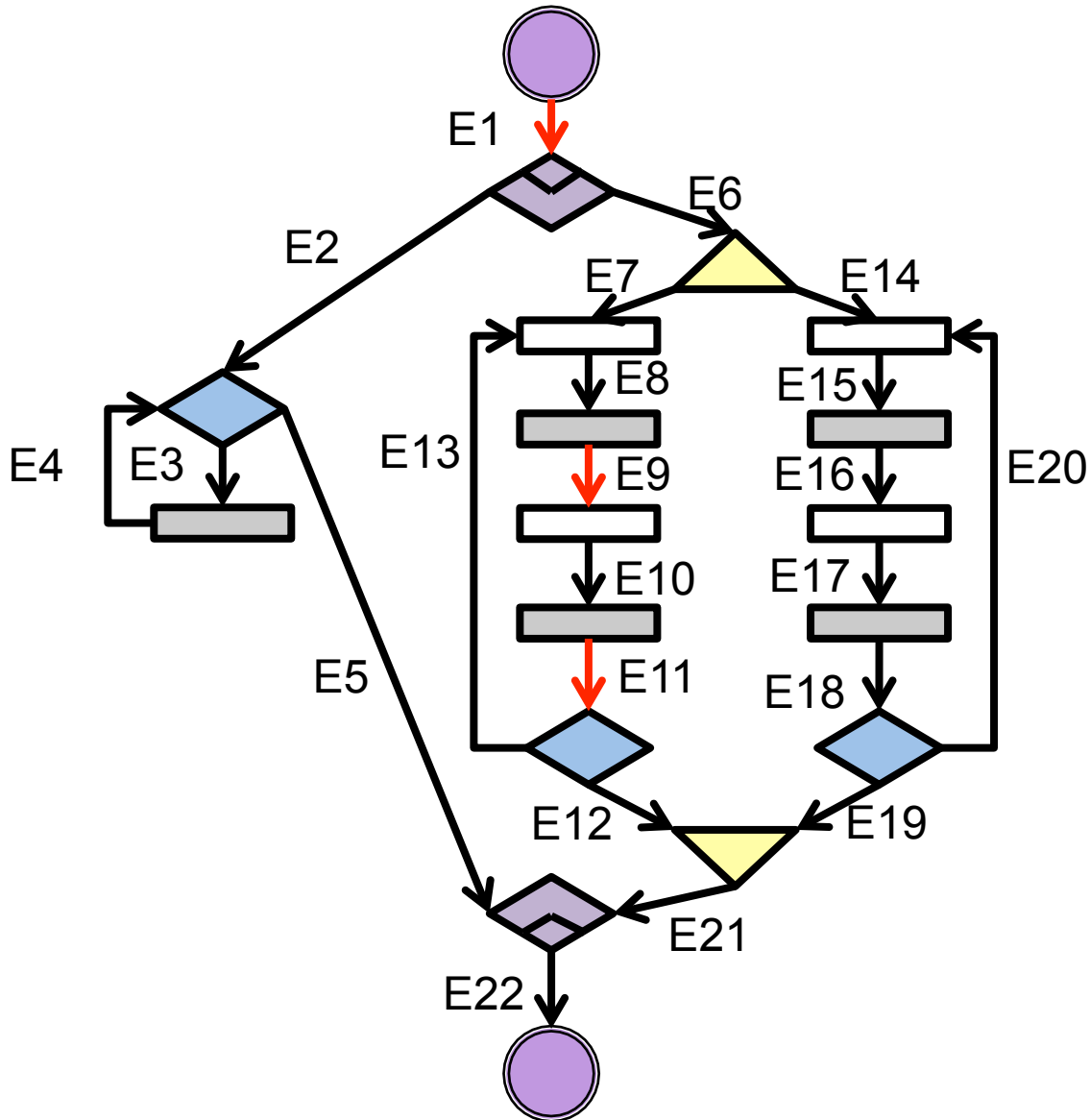
ILP model



EOT:

$$E1 + E4 \leq 1$$

ILP model

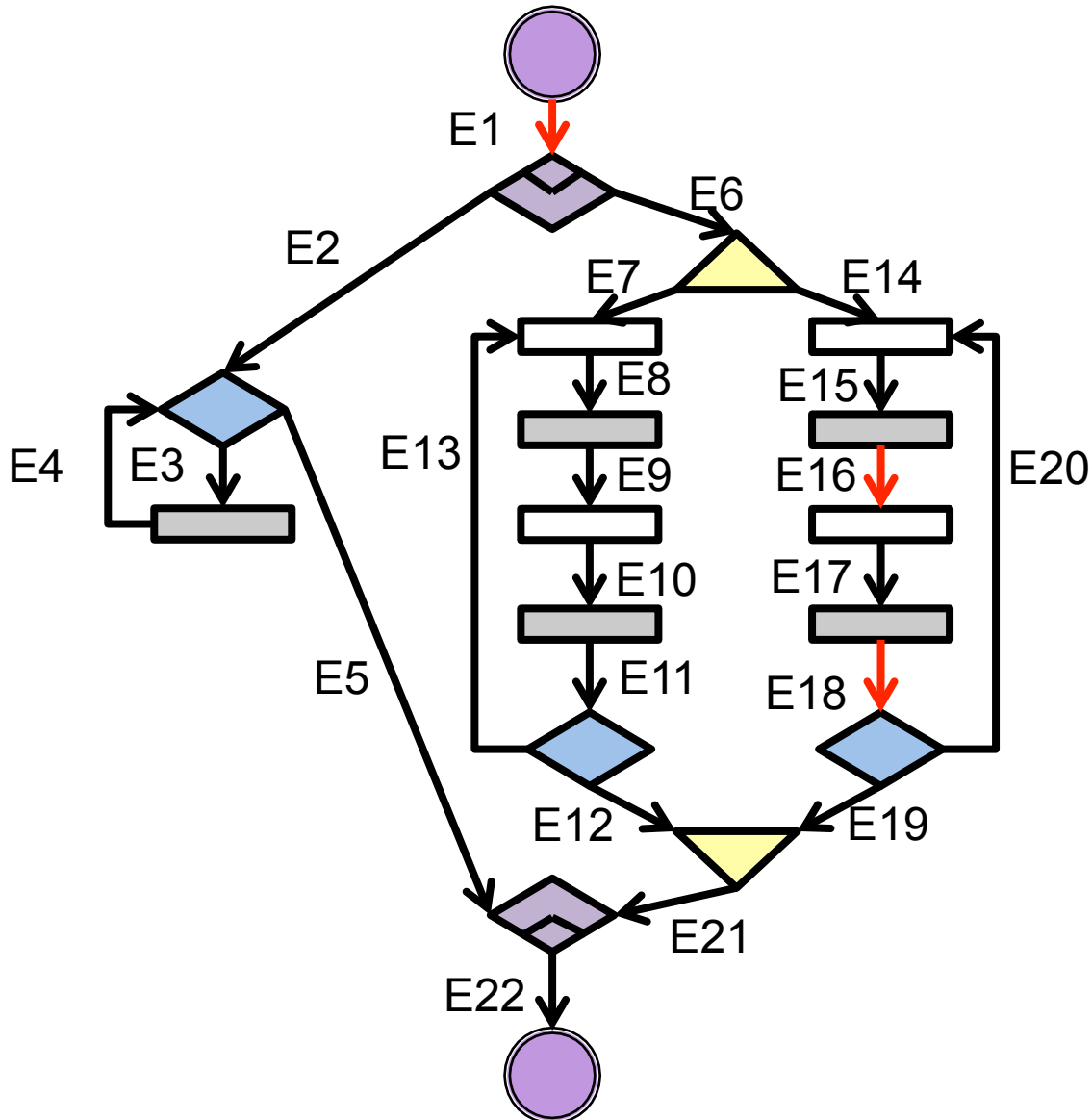


EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

ILP model



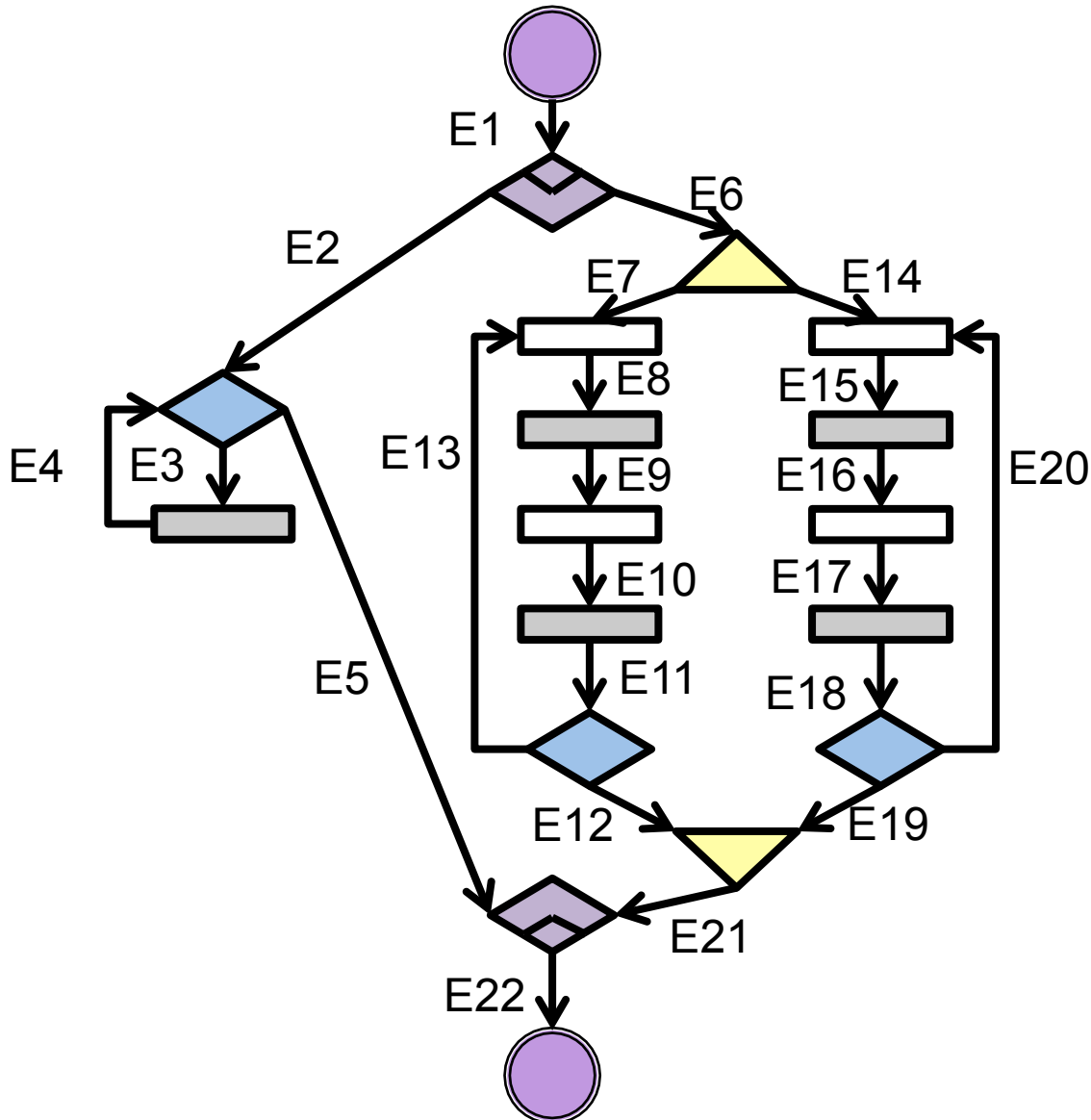
EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

ILP model



EOT:

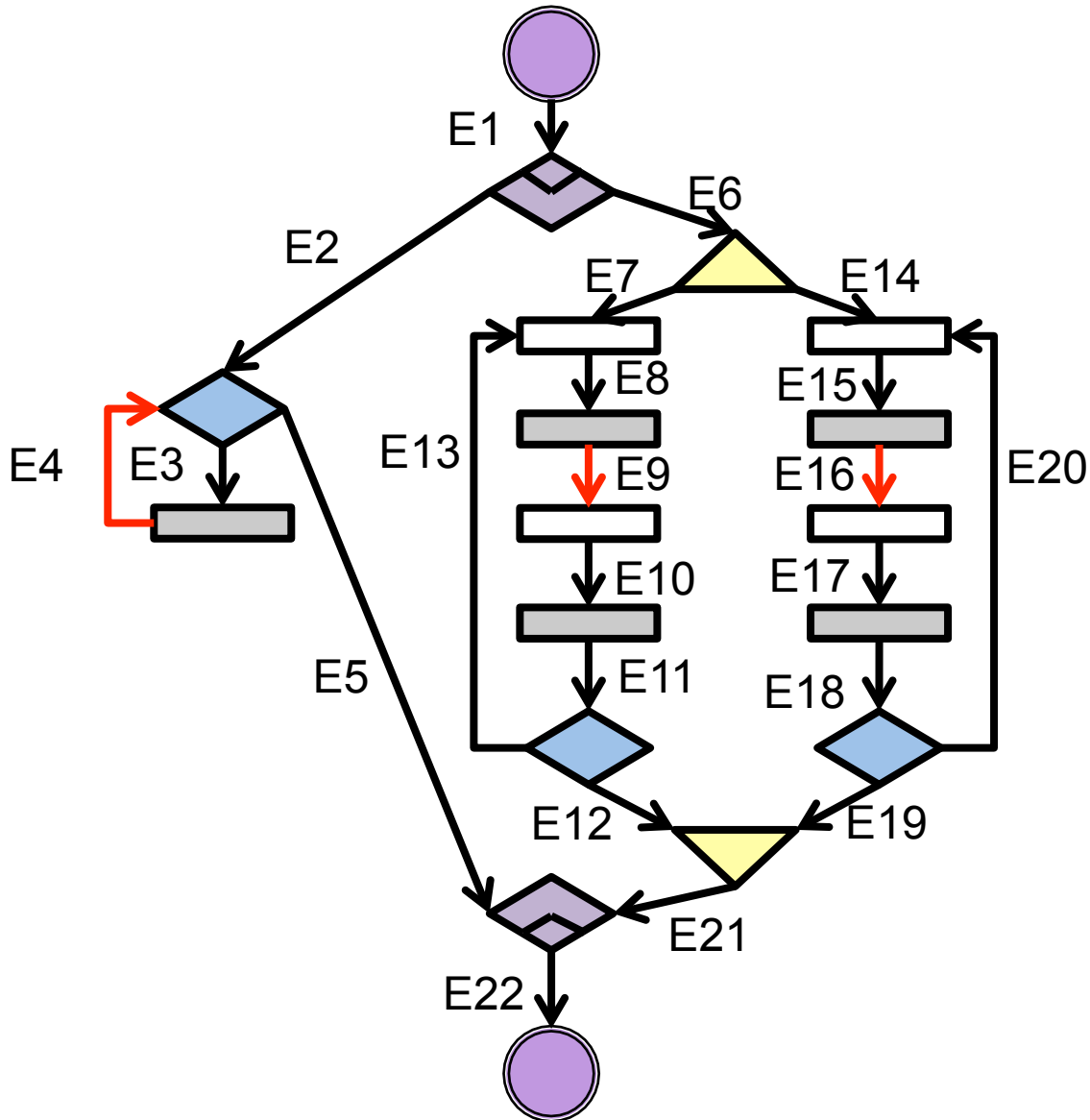
$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

- At most one EOT edge can be active per thread
- Parent / child relationship needs to be considered.

ILP model



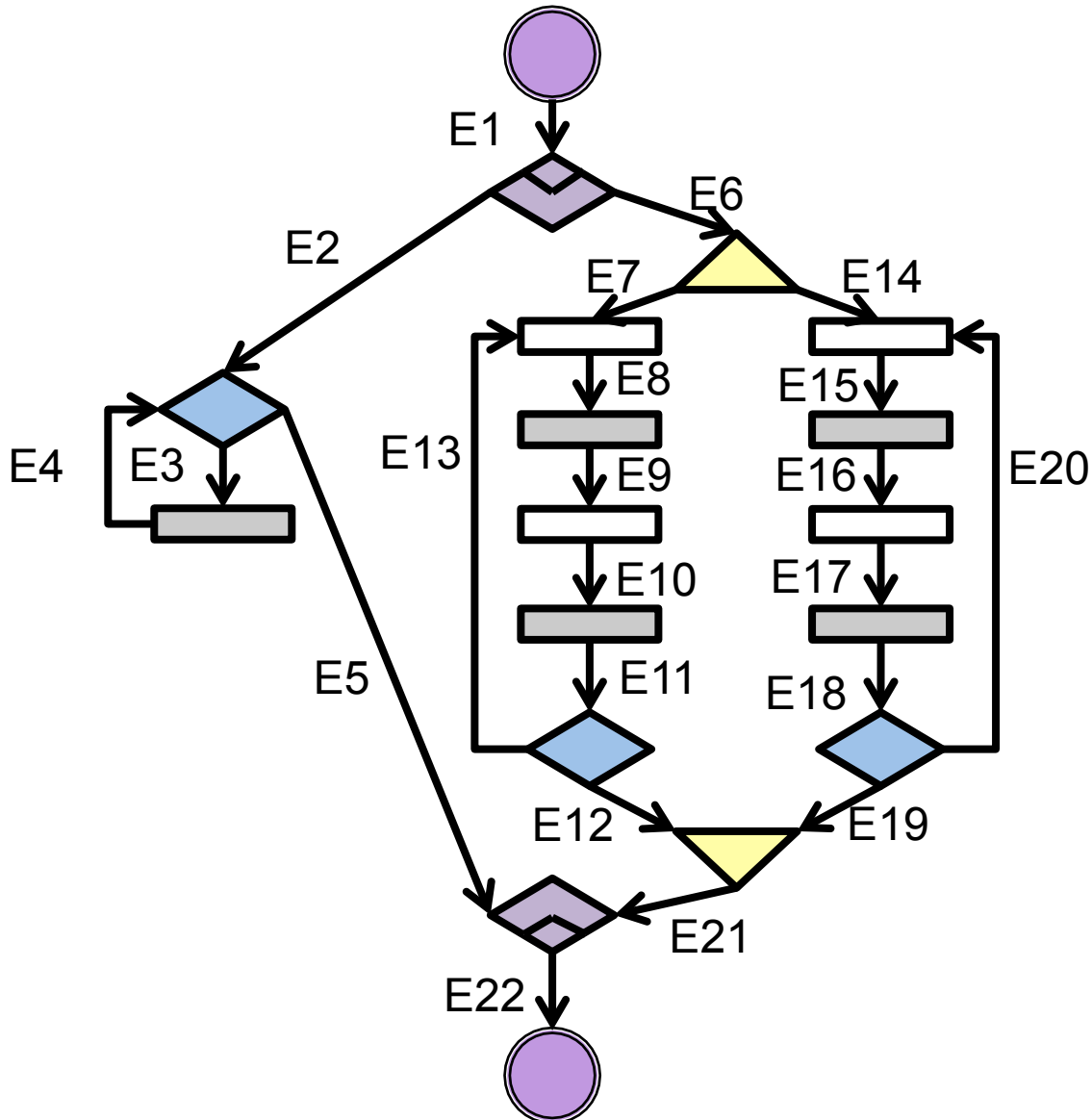
EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

ILP model



EOT:

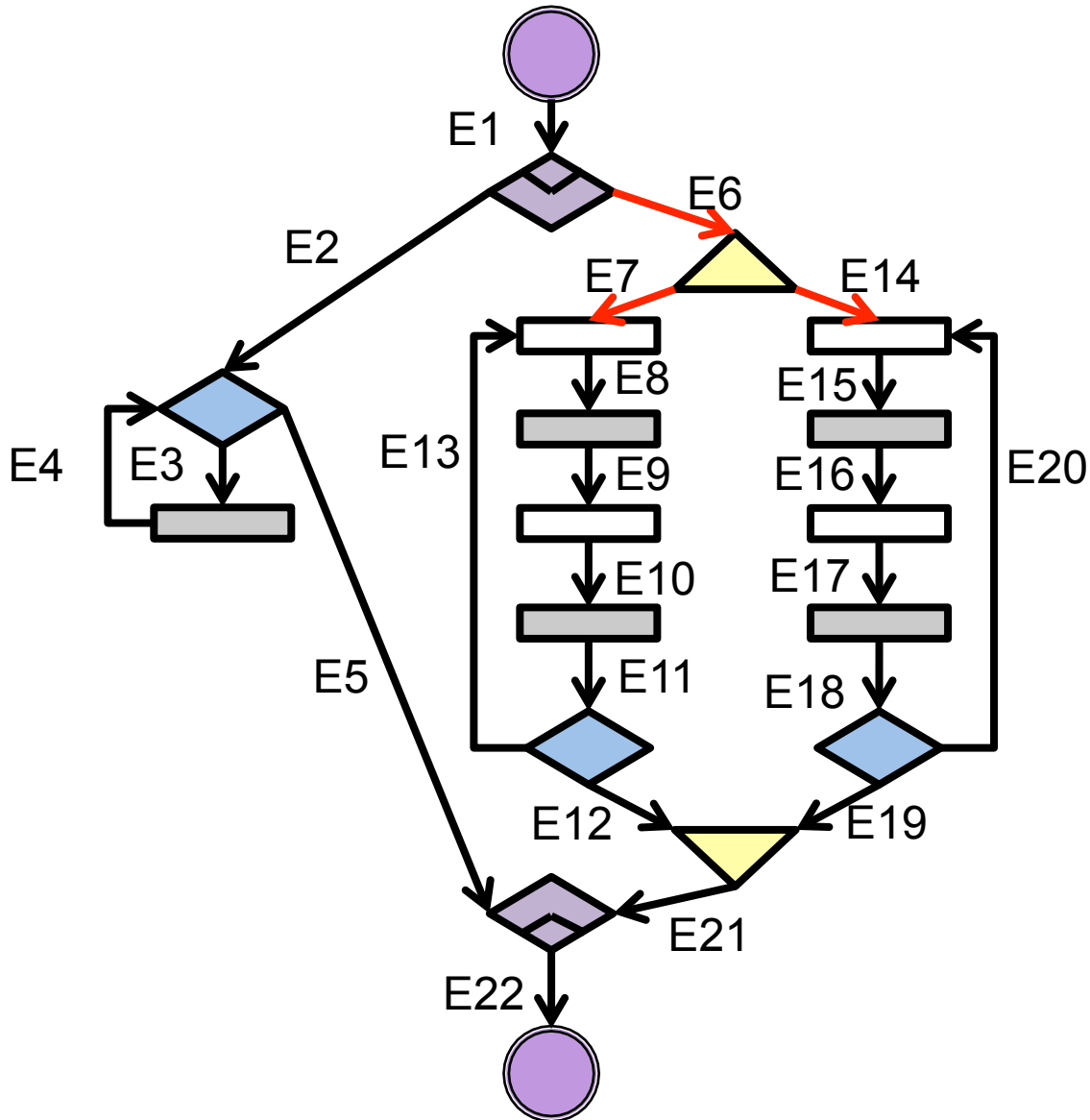
$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

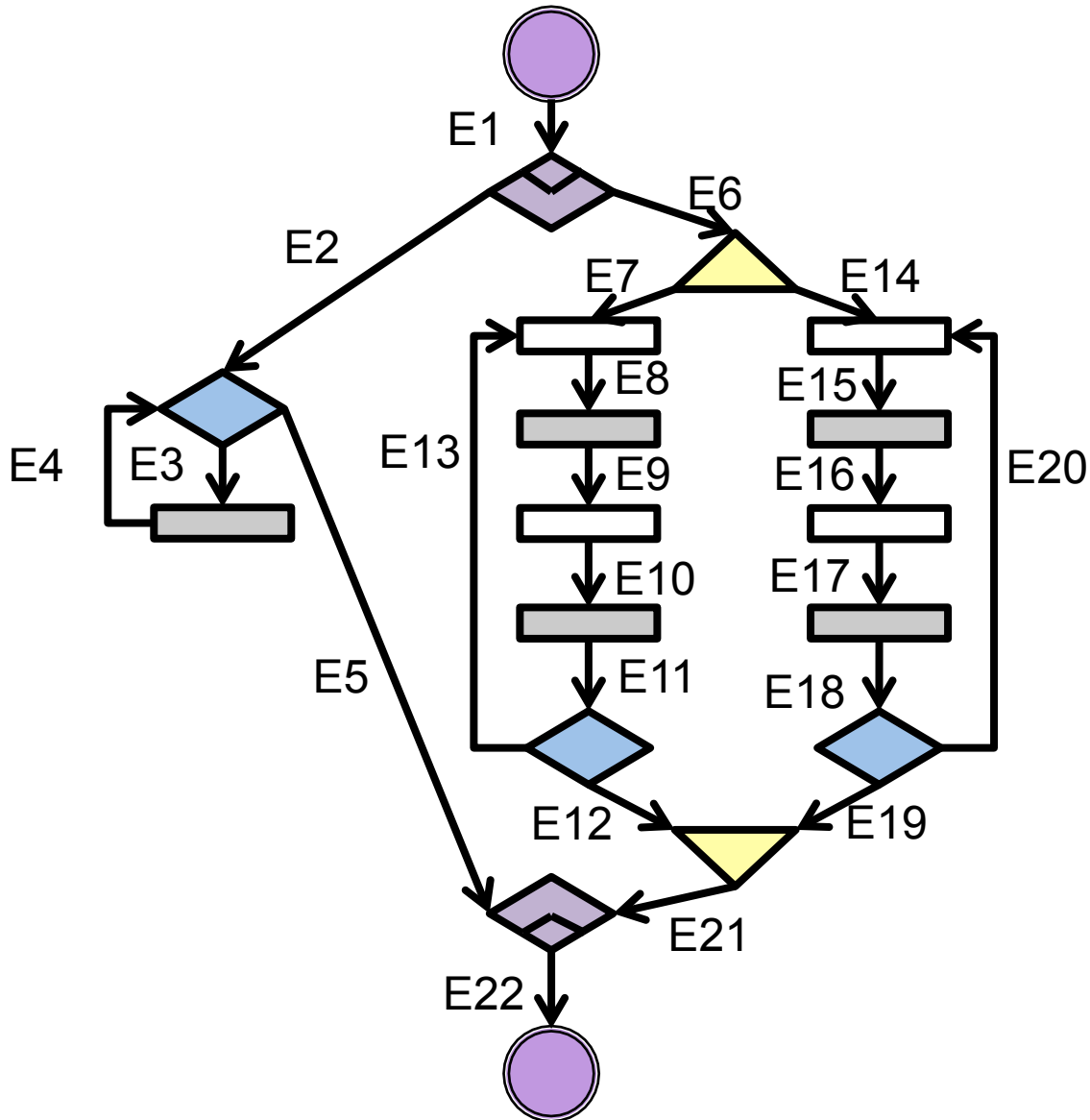
$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

$$E14 = E6$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

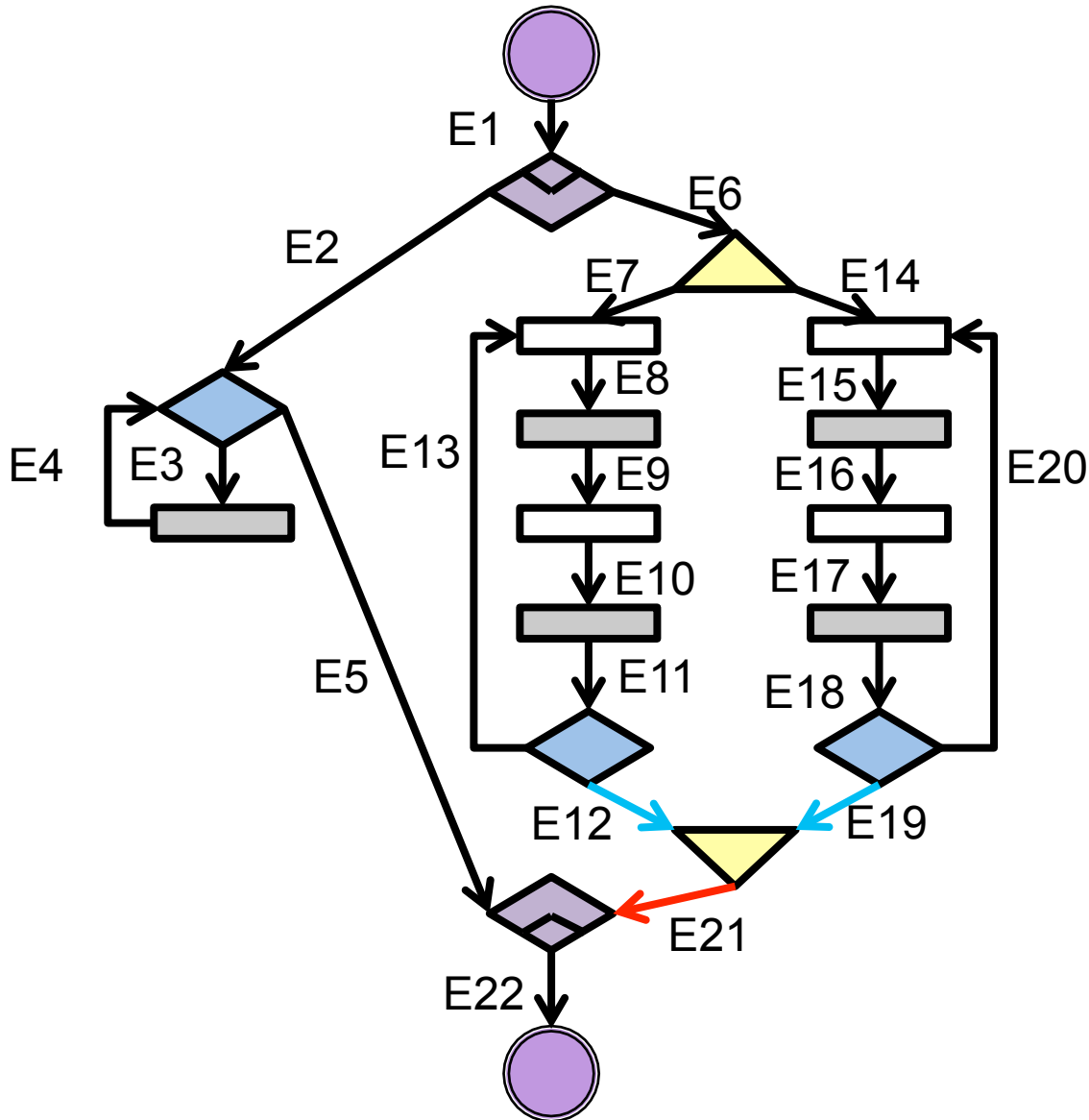
Fork:

$$E7 = E6$$

$$E14 = E6$$

Join:

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

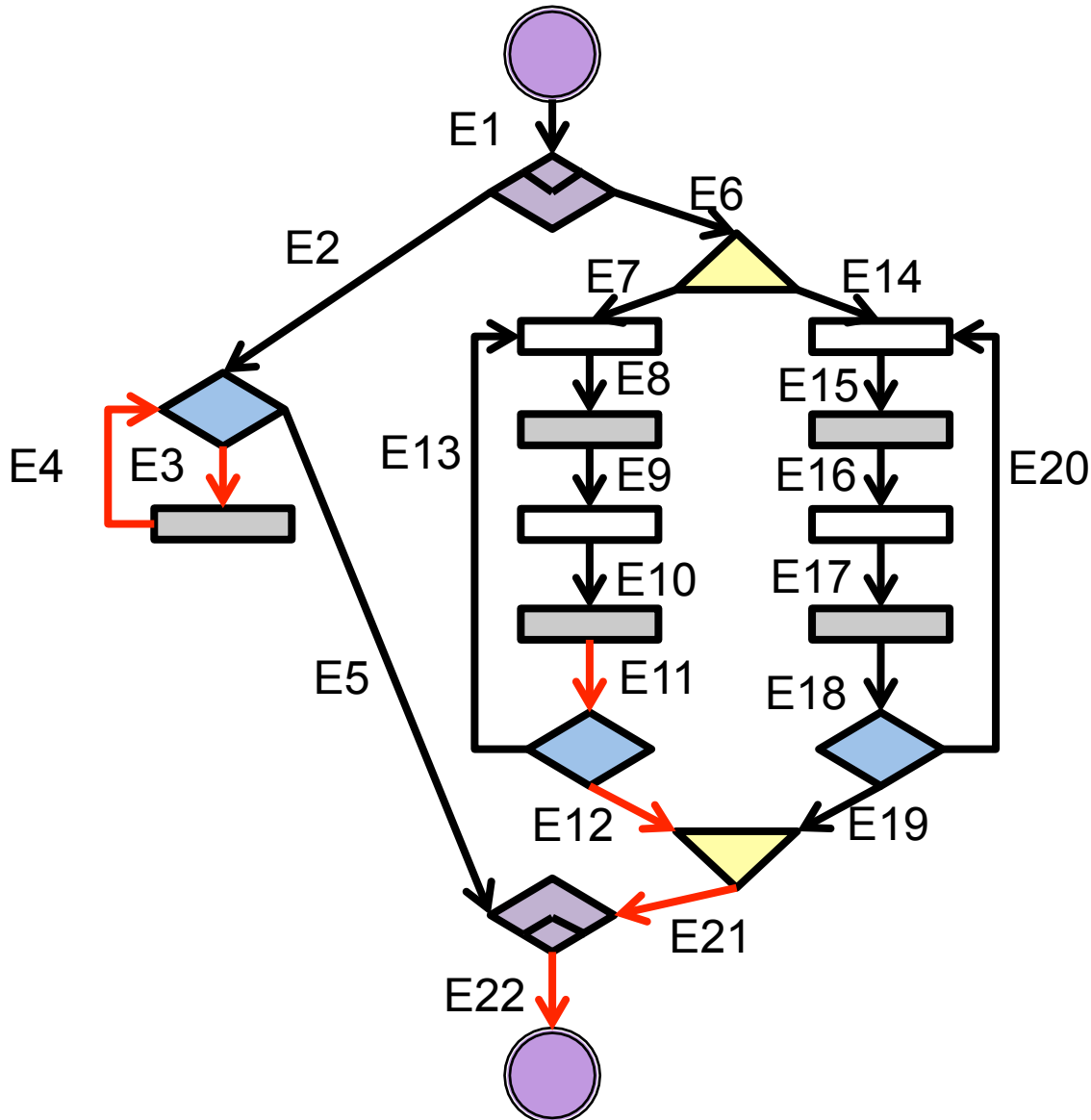
$$E7 = E6$$

$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

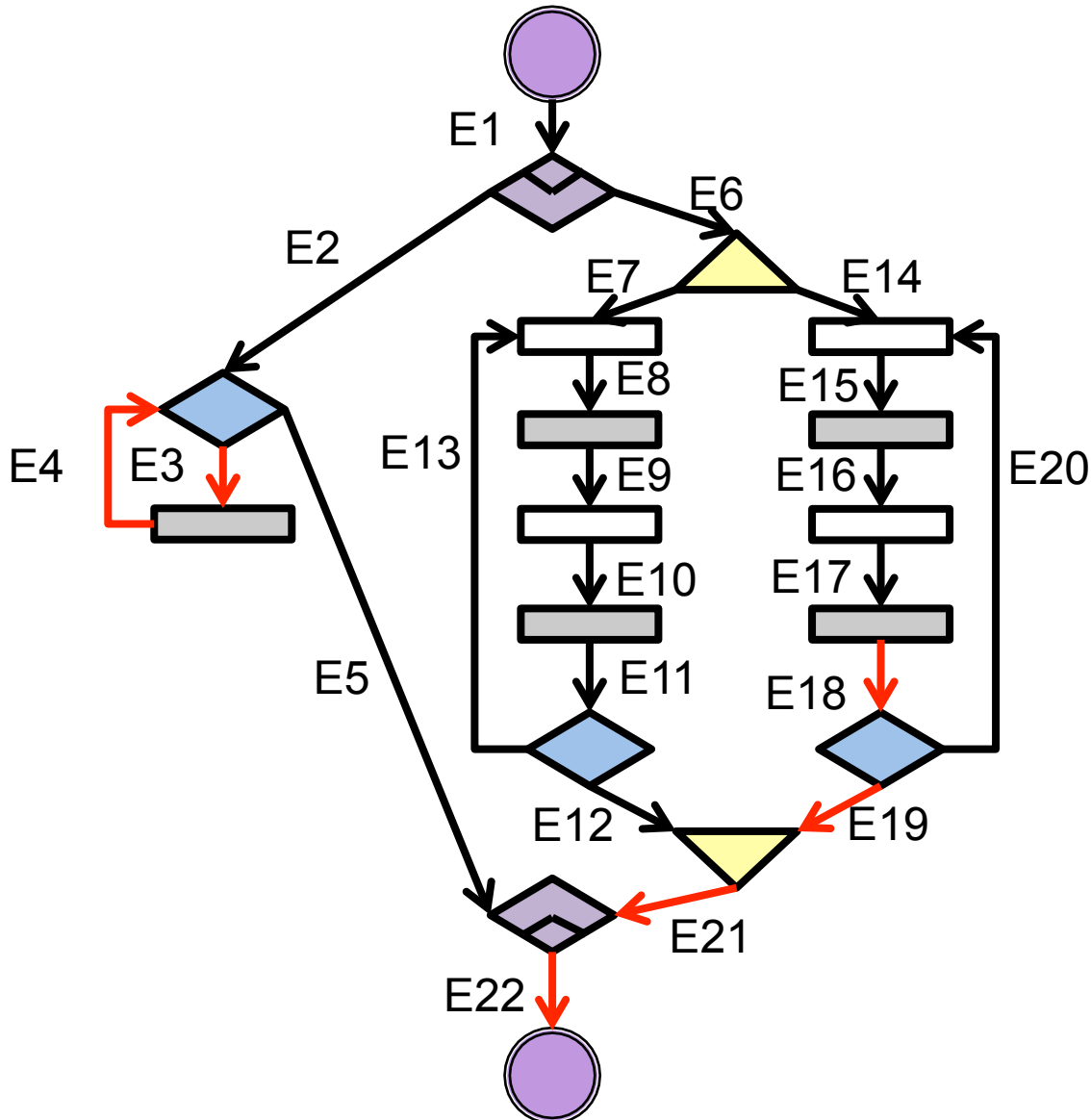
$$E7 = E6$$

$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

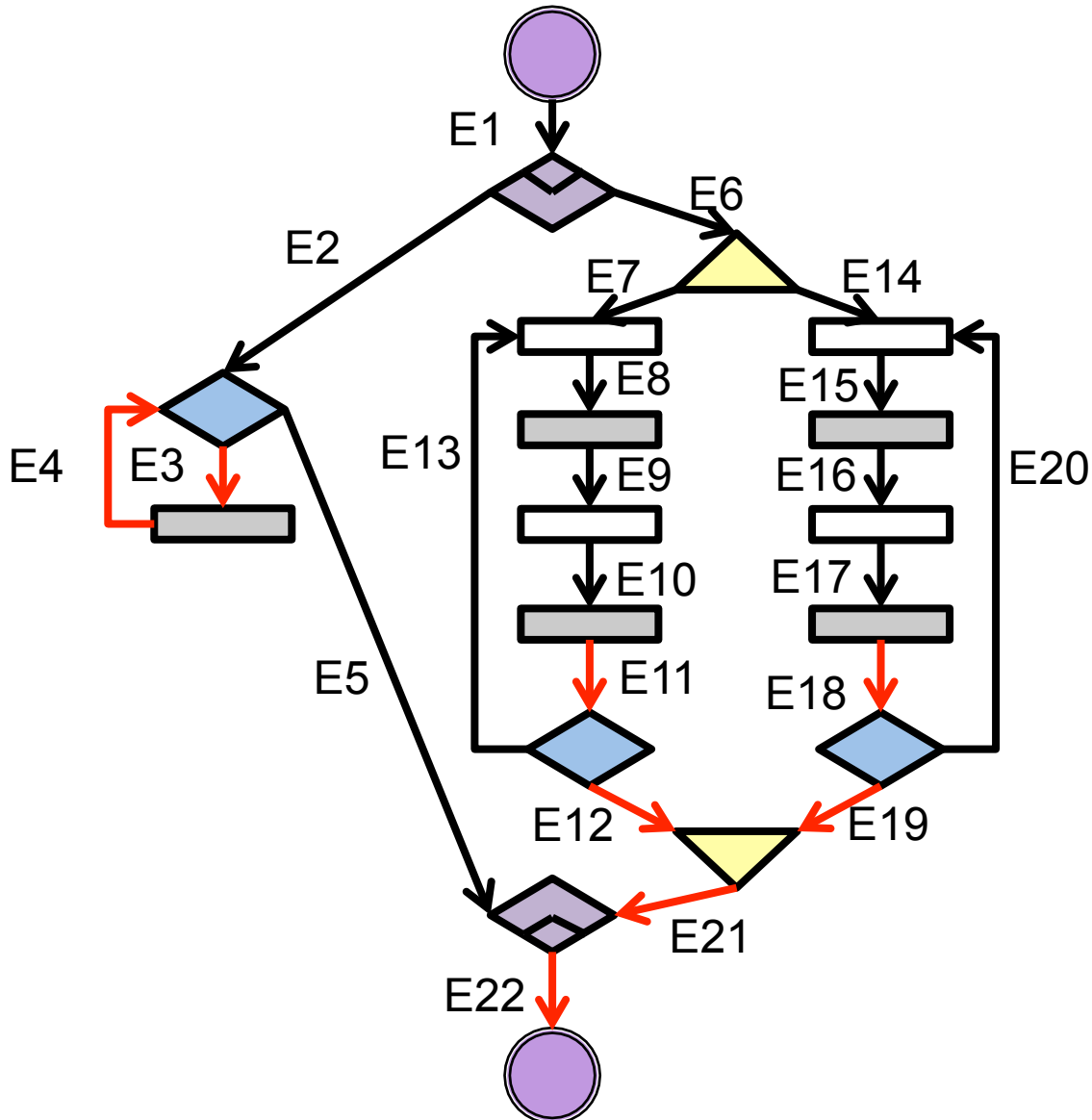
$$E7 = E6$$

$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

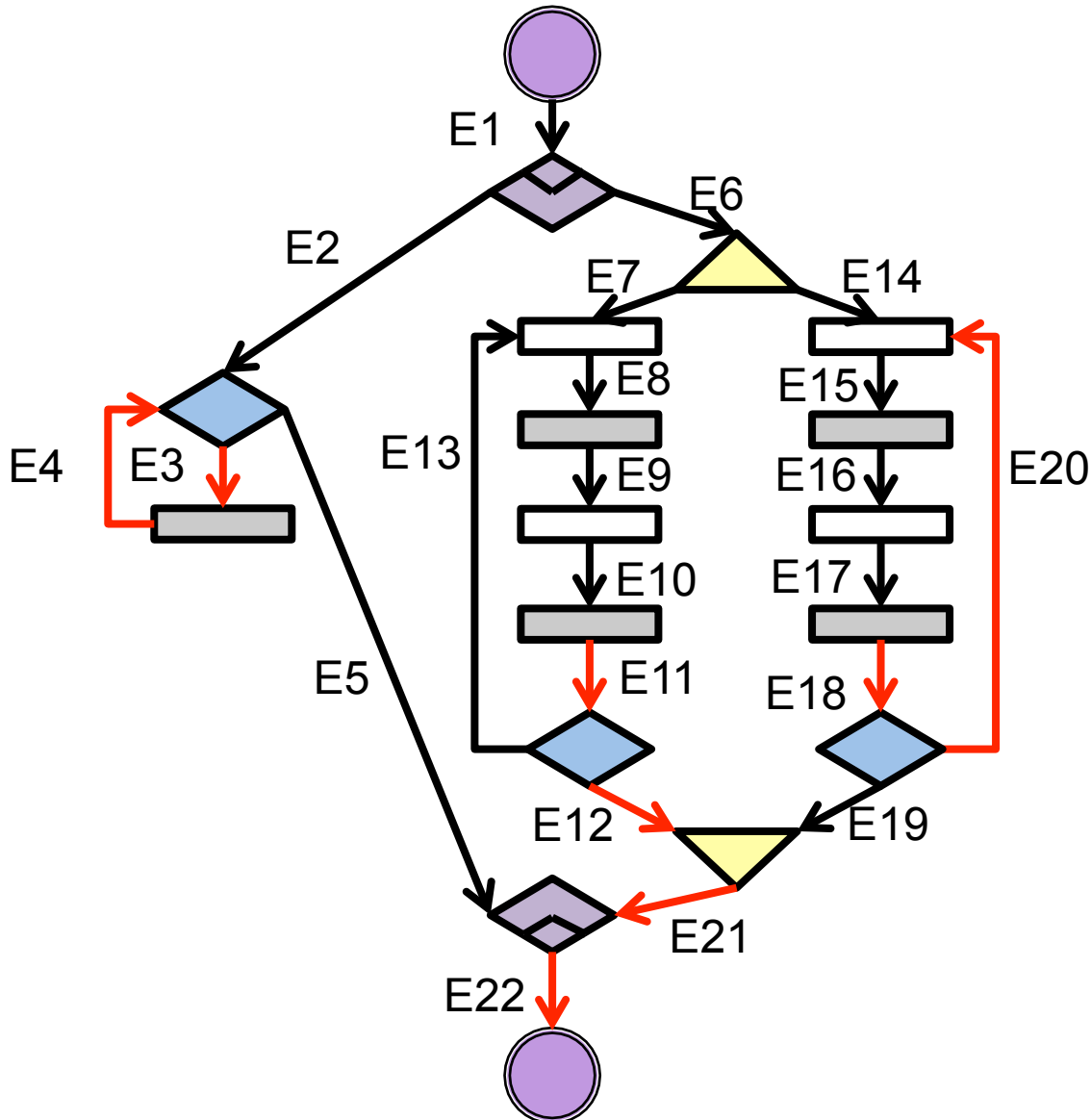
$$E7 = E6$$

$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

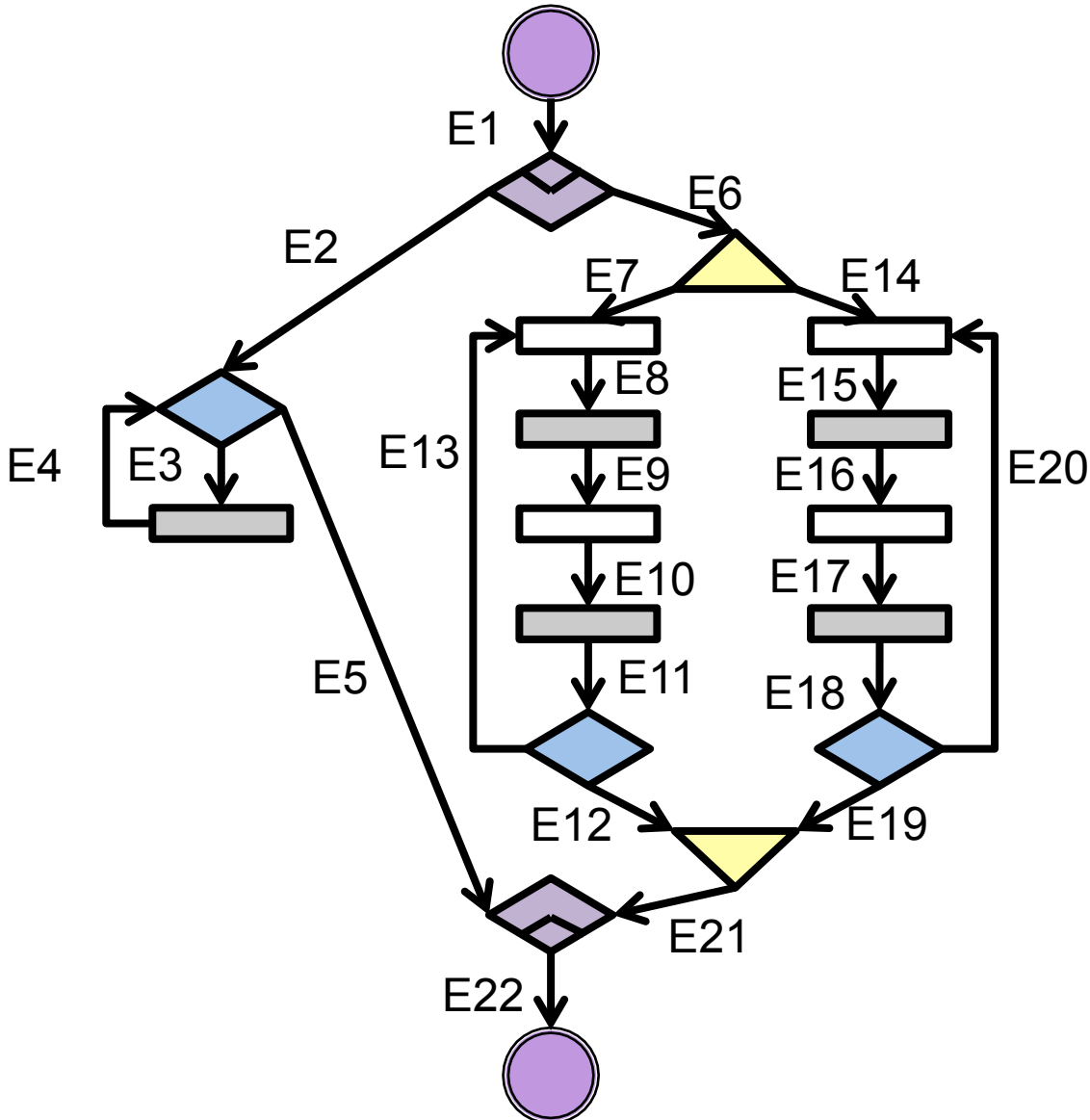
$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

Exception

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

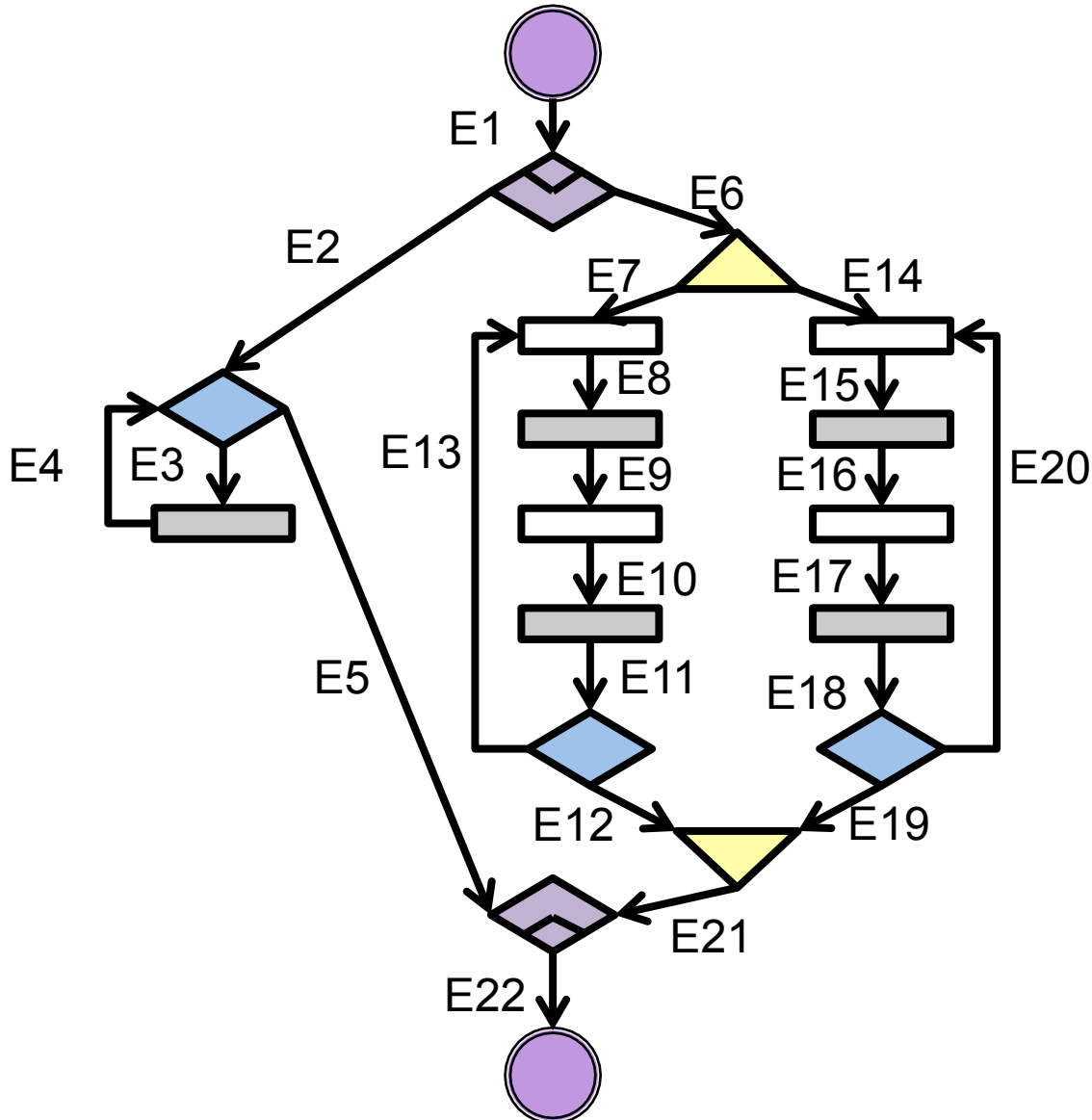
$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

$$E21 \leq (1 - E6 - E9 - E11) + E12$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

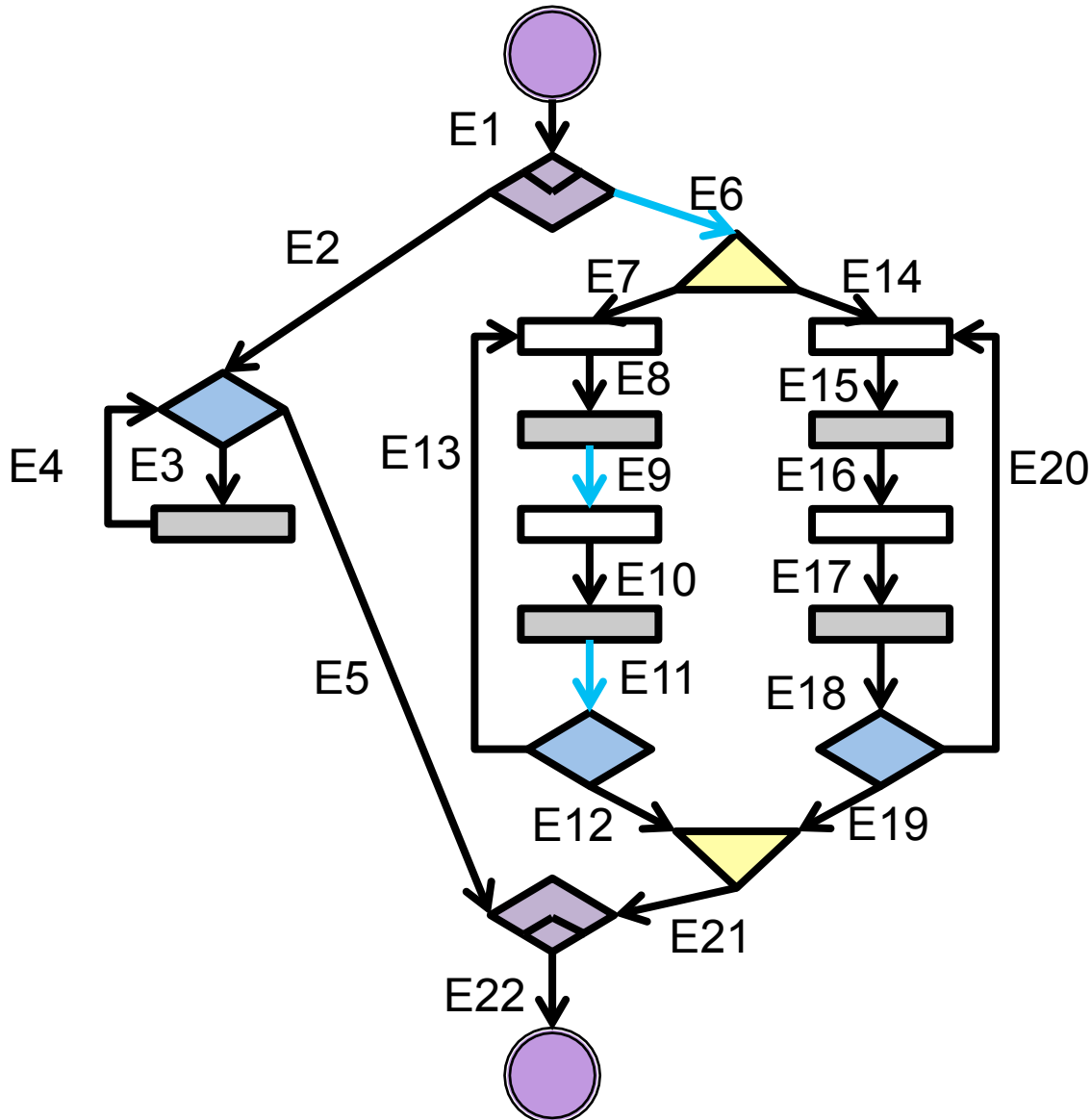
$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

$$E21 \leq (1 - E6 - E9 - E11) + E12$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

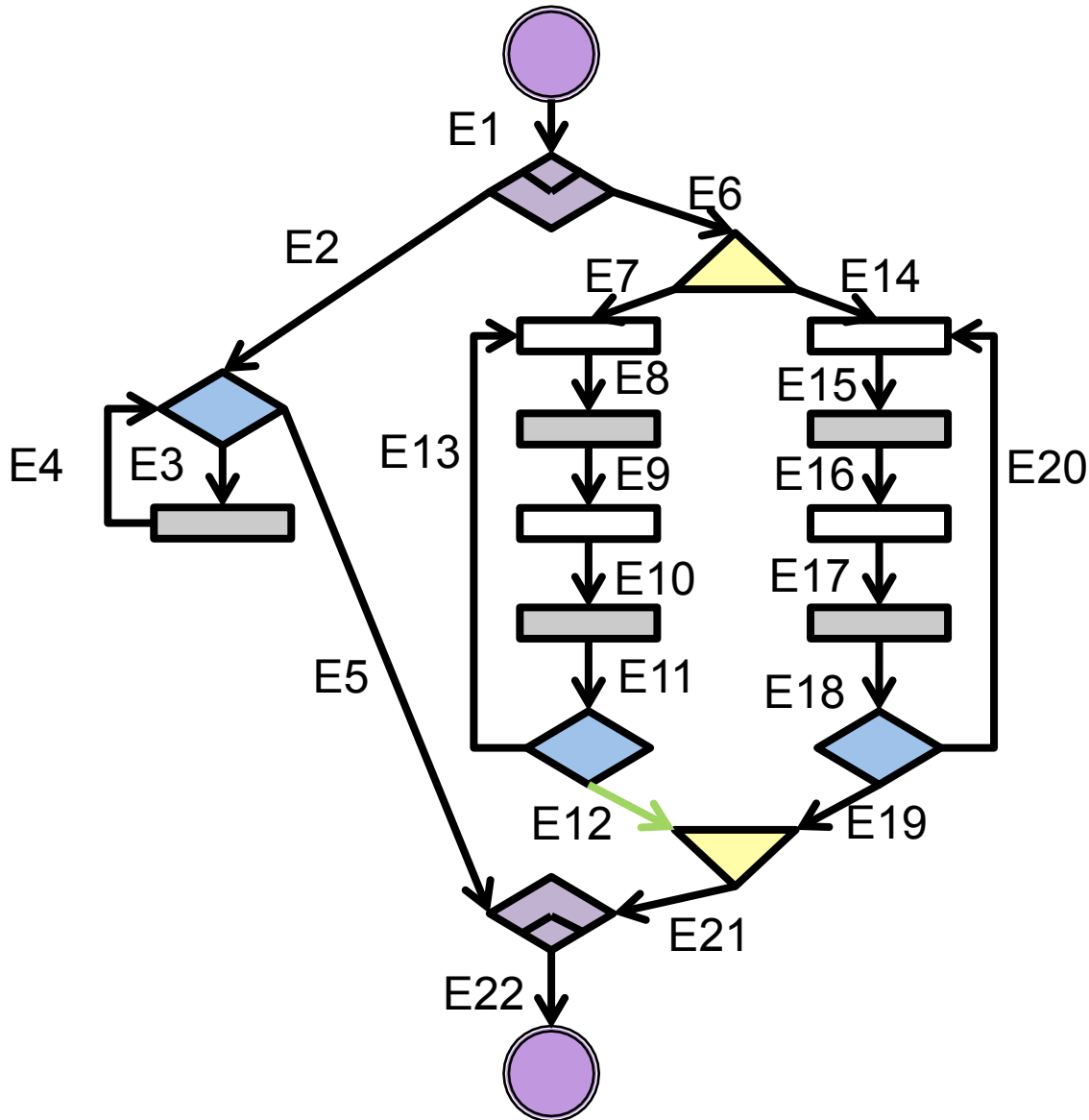
$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

$$E21 \leq (1 - E6 - E9 - E11) + E12$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

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$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

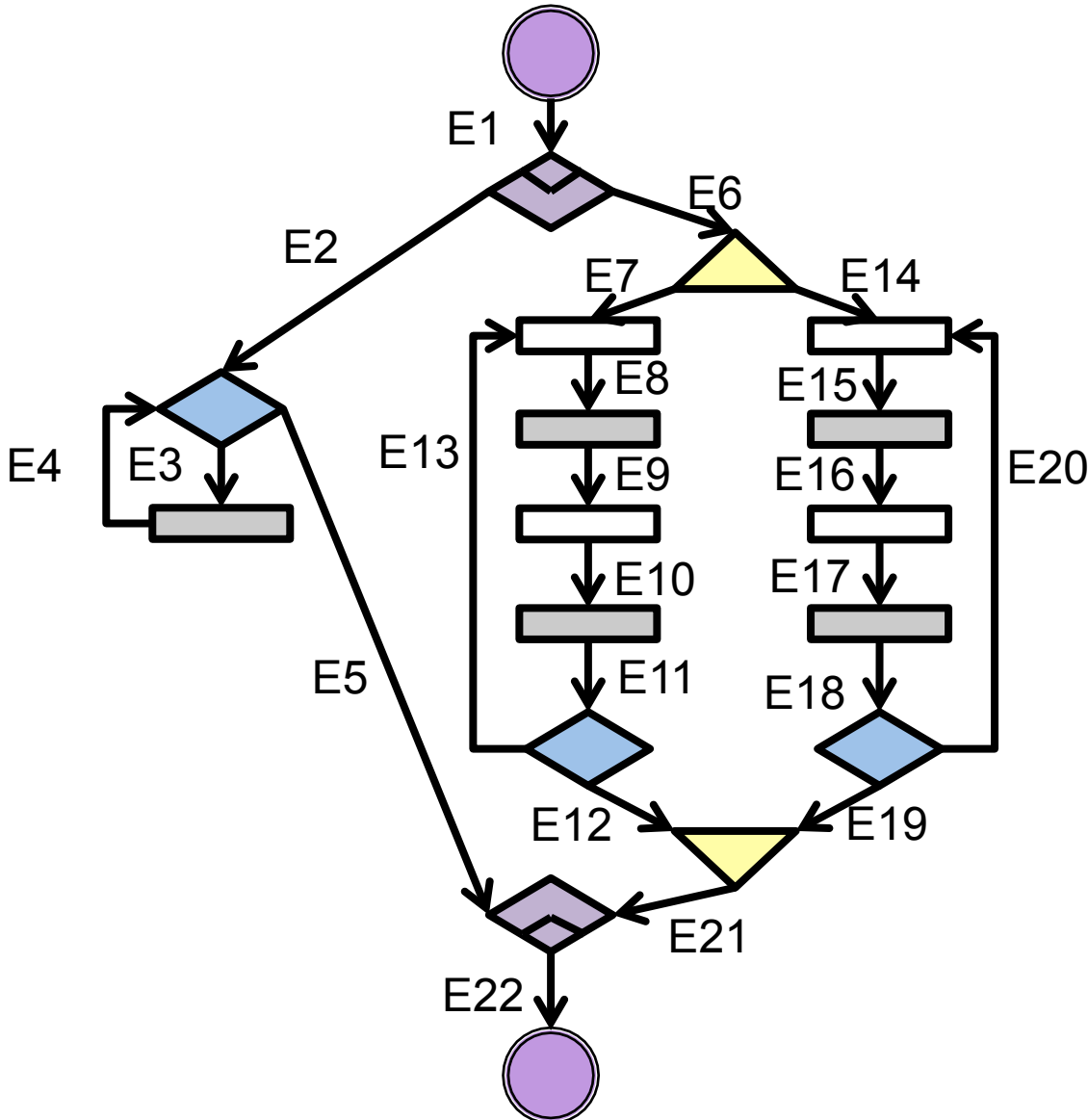
$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

$$E21 \leq (1 - E6 - E9 - E11) + E12$$

ILP model



EOT:

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$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

$$E14 = E6$$

Join:

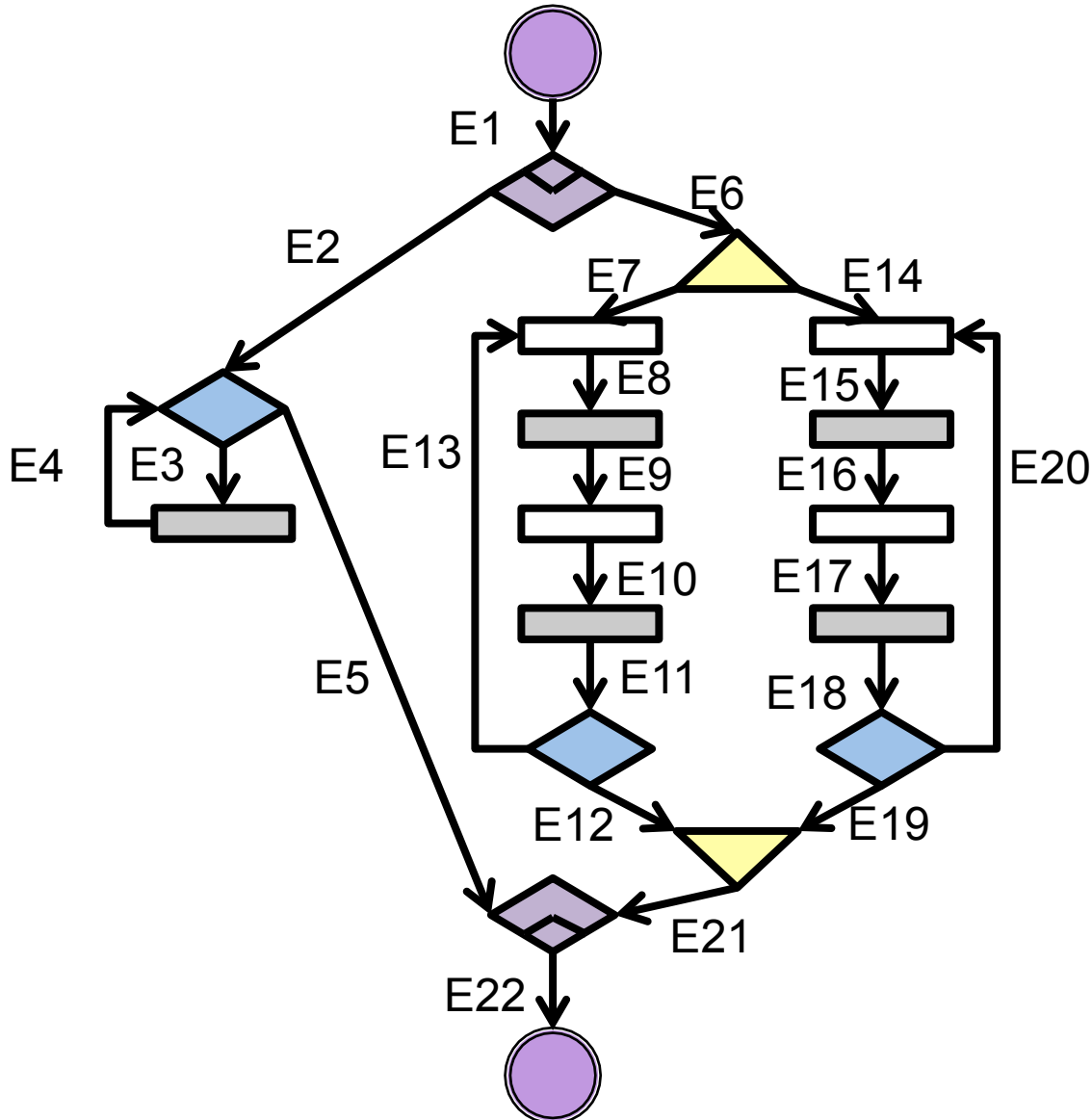
$$E21 \leq E12 + E19$$

$$E21 \leq (1 - E6 - E9 - E11) + E12$$

Using EOT edges:

- Enough to represent all edges in a thread

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

$$E14 = E6$$

Join:

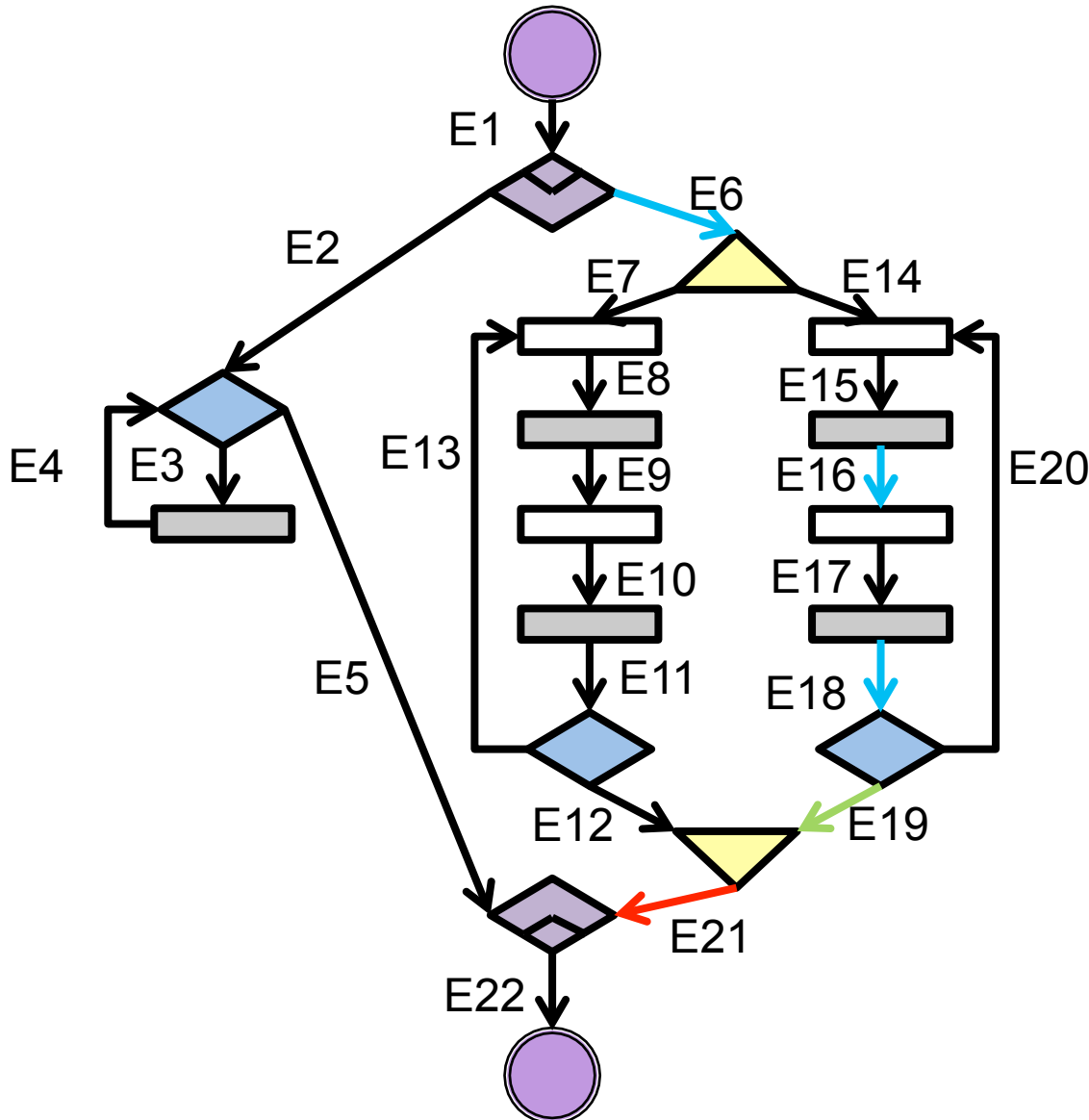
$$E21 \leq E12 + E19$$

$$E21 \leq (1 - E6 - E9 - E11) + E12$$

Using EOT edges:

- Enough to represent all edges in a thread
- Re-use EOT constraints

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

$$E14 = E6$$

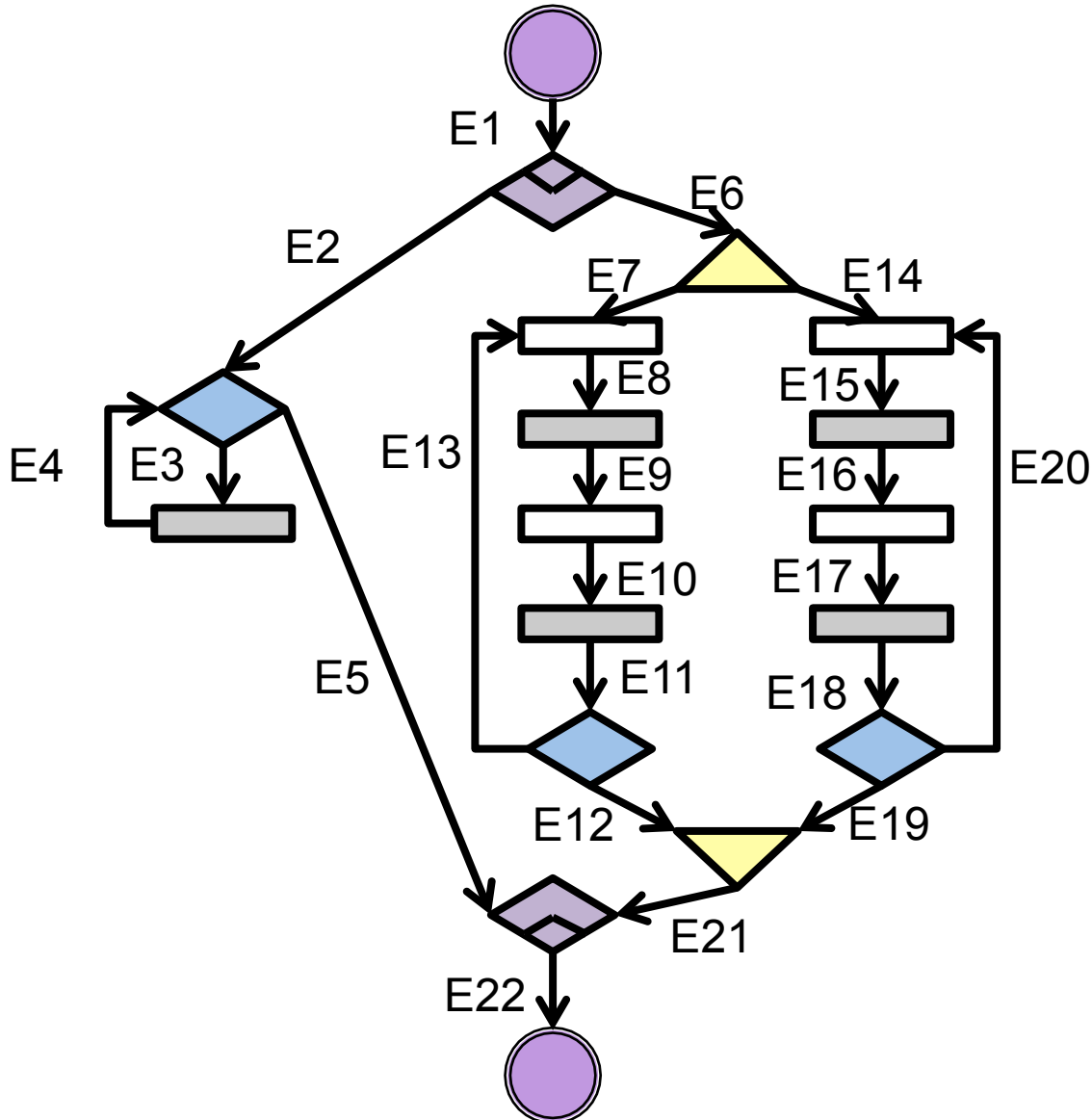
Join:

$$E21 \leq E12 + E19$$

$$E21 \leq (1 - E6 - E9 - E11) + E12$$

$$E21 \leq (1 - E6 - E16 - E18) + E19$$

ILP model



EOT:

$$E1 + E4 \leq 1$$

$$E1 + E9 + E11 \leq 1$$

$$E1 + E16 + E18 \leq 1$$

Fork:

$$E7 = E6$$

$$E14 = E6$$

Join:

$$E21 \leq E12 + E19$$

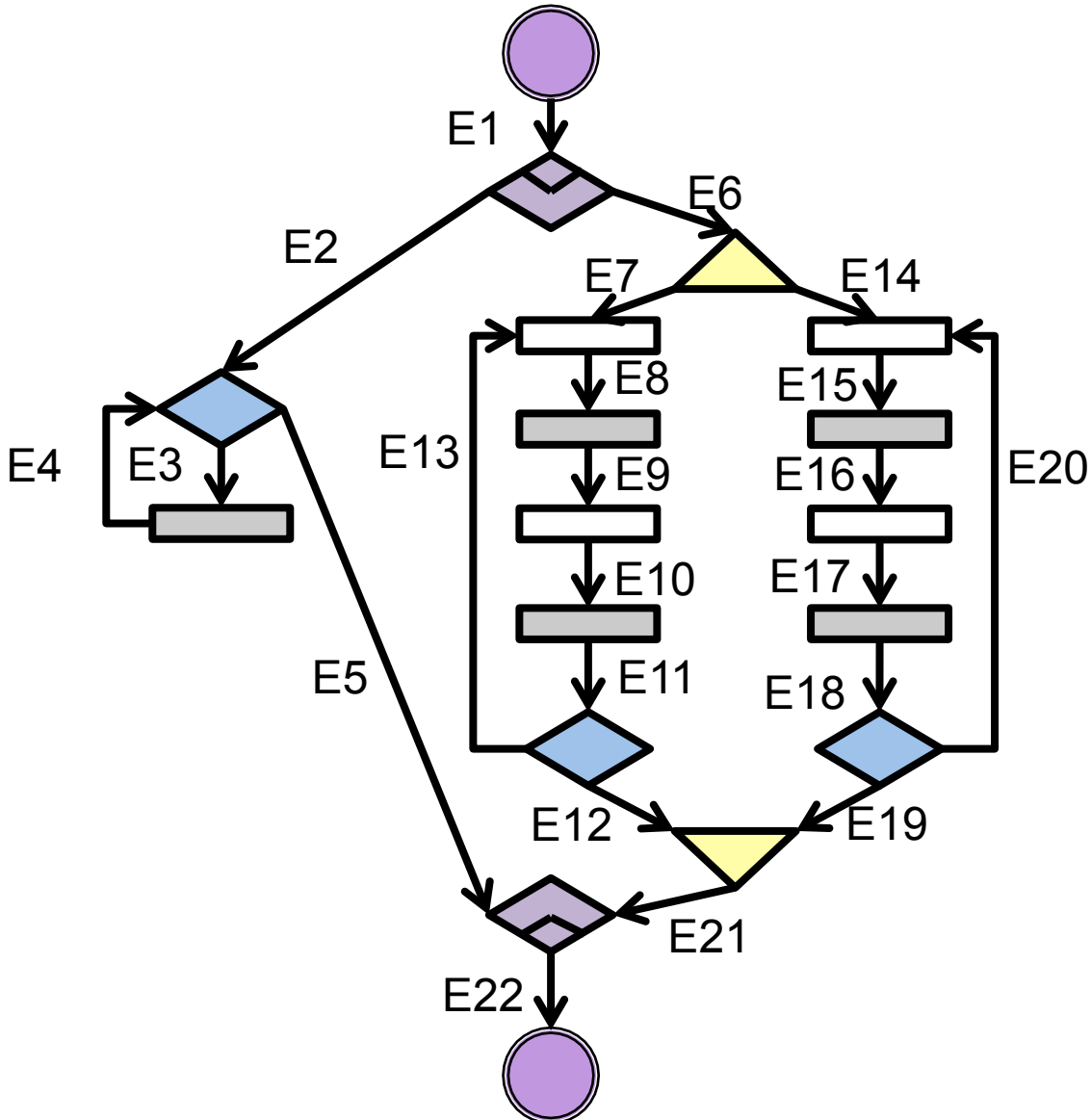
$$E21 \leq (1 - E6 - E9 - E11) + E12$$

$$E21 \leq (1 - E6 - E16 - E18) + E19$$

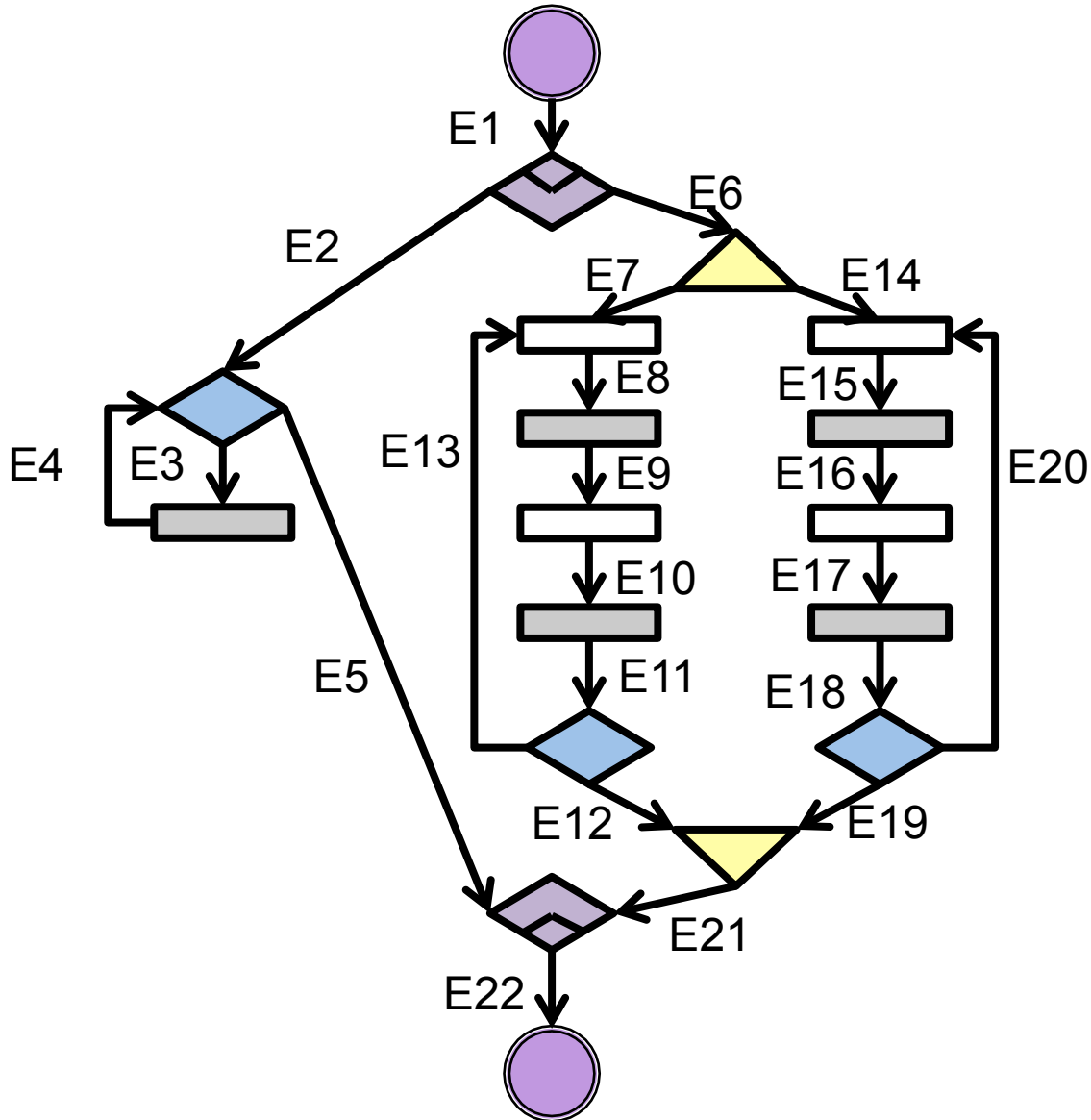
E21 is '1' if the right hand side of all the constraints are greater than '0'

ILP model

Abort start:



ILP model

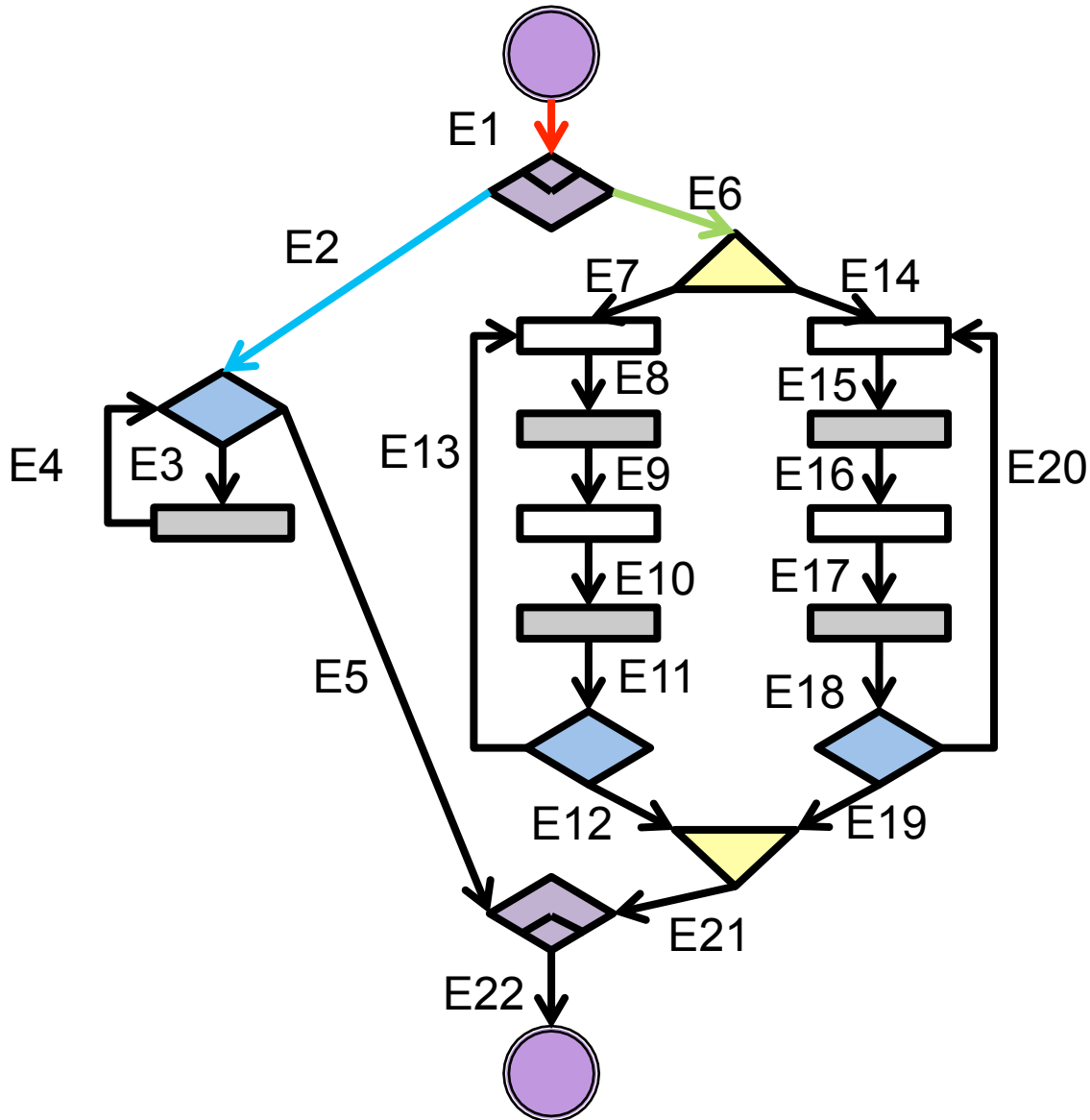


Abort start:

$$E1 = E2$$

$$E1 \geq E6$$

ILP model

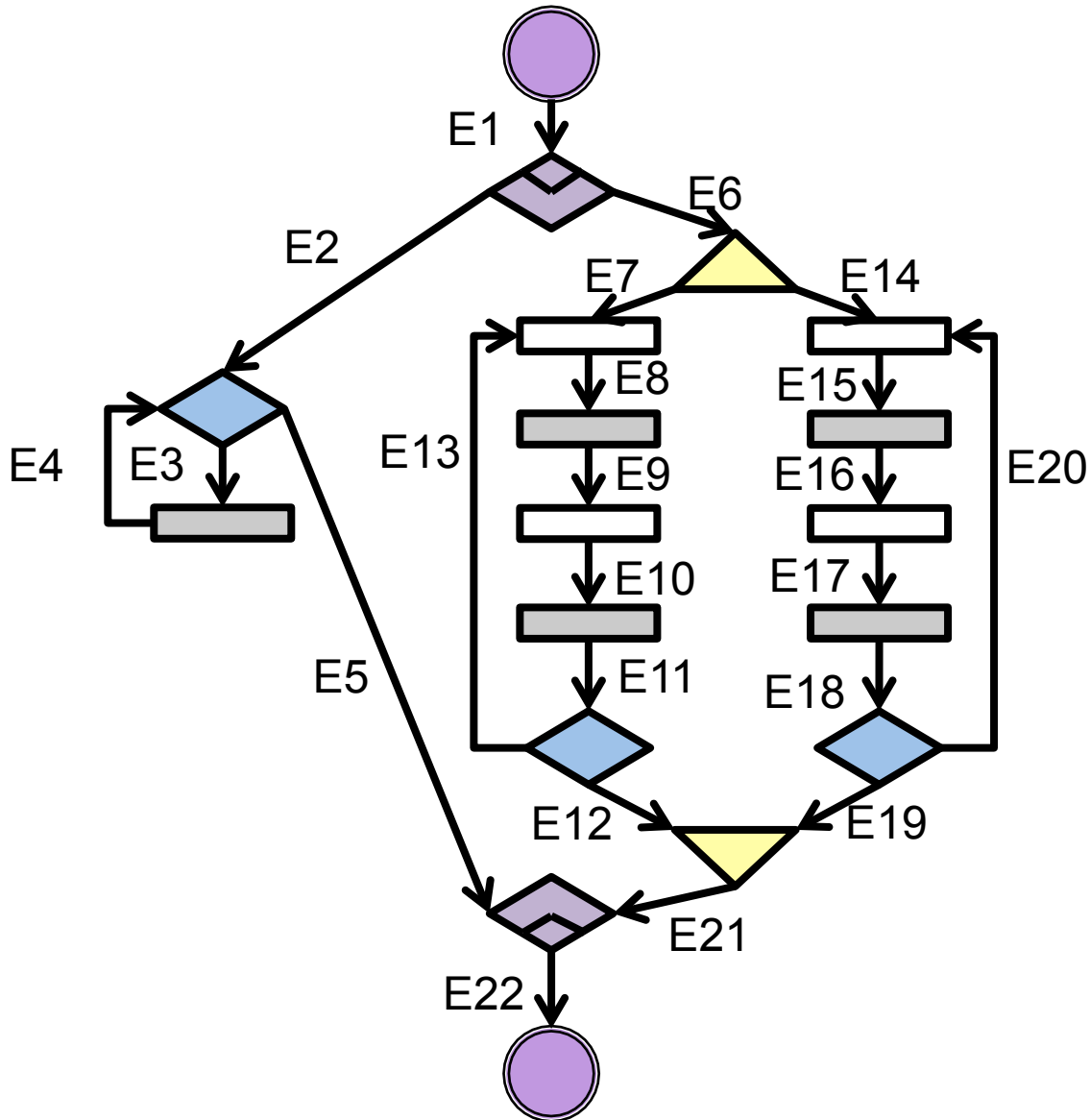


Abort start:

$$E1 = E2$$

$$E1 \geq E6$$

ILP model



Abort start:

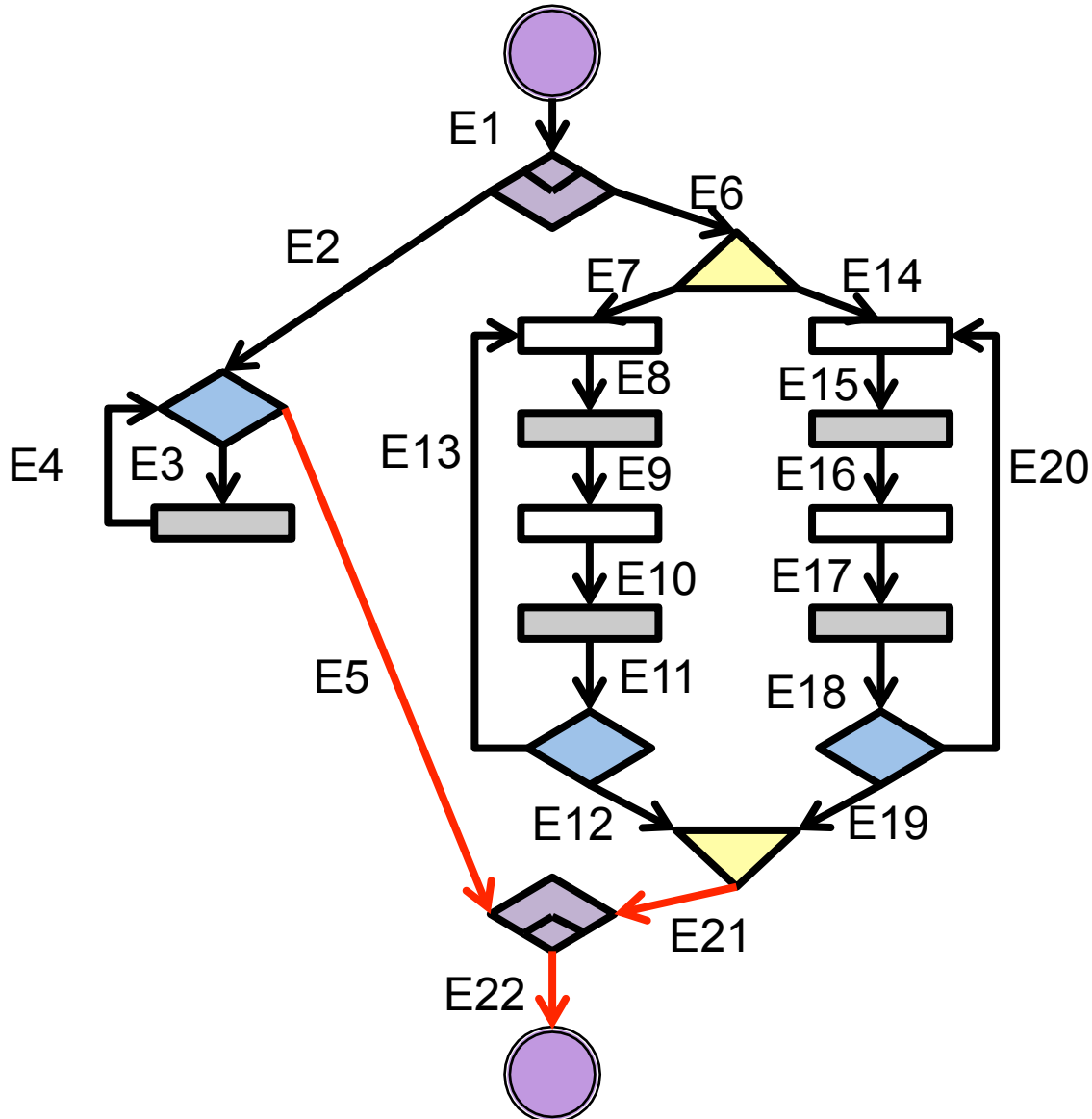
$$E1 = E2$$

$$E1 \geq E6$$

Abort End:

$$E22 = E5 + E21$$

ILP model



Abort start:

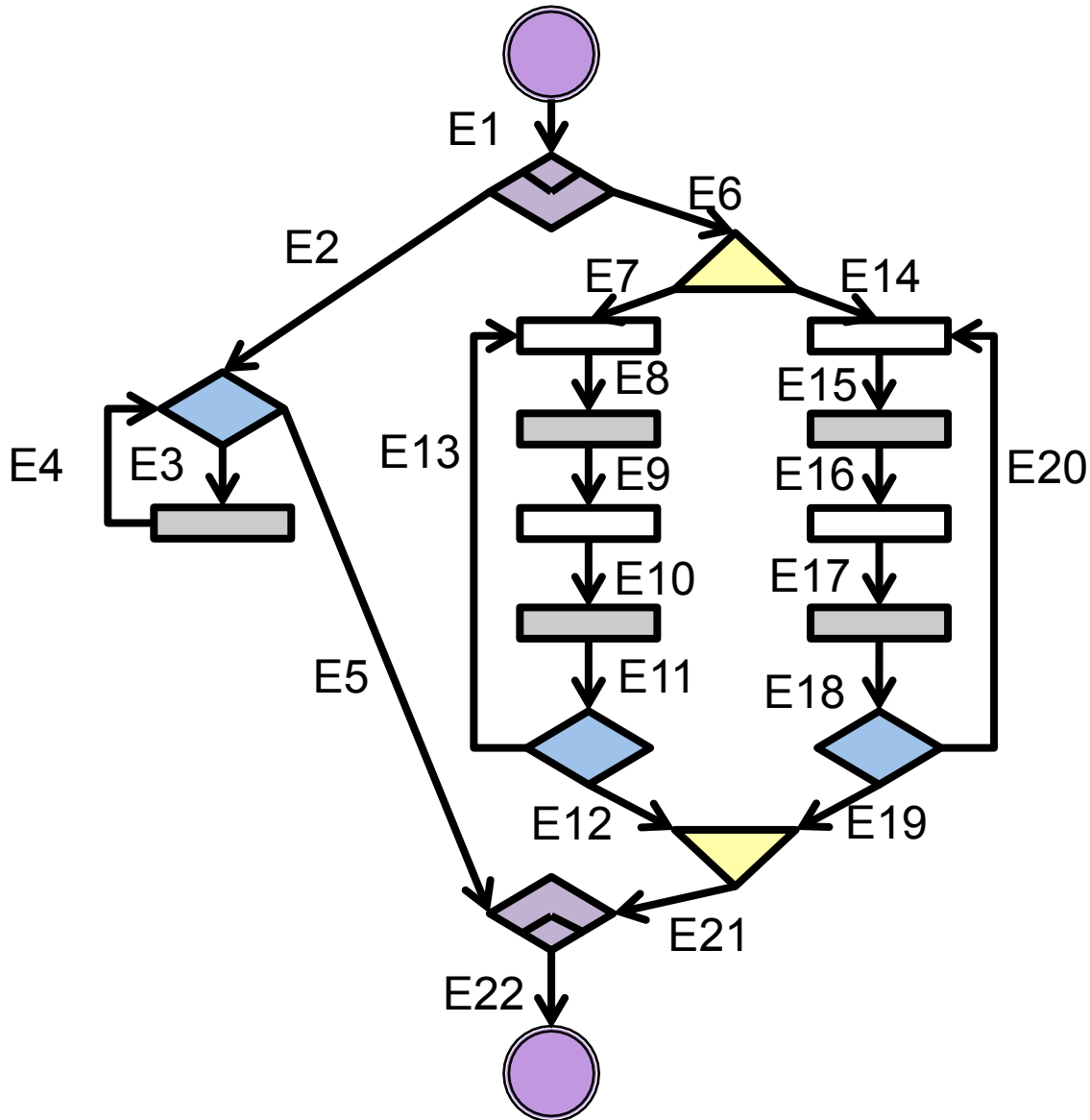
$$E1 = E2$$

$$E1 \geq E6$$

Abort End:

$$E22 = E5 + E21$$

ILP model



Abort start:

$$E1 = E2$$

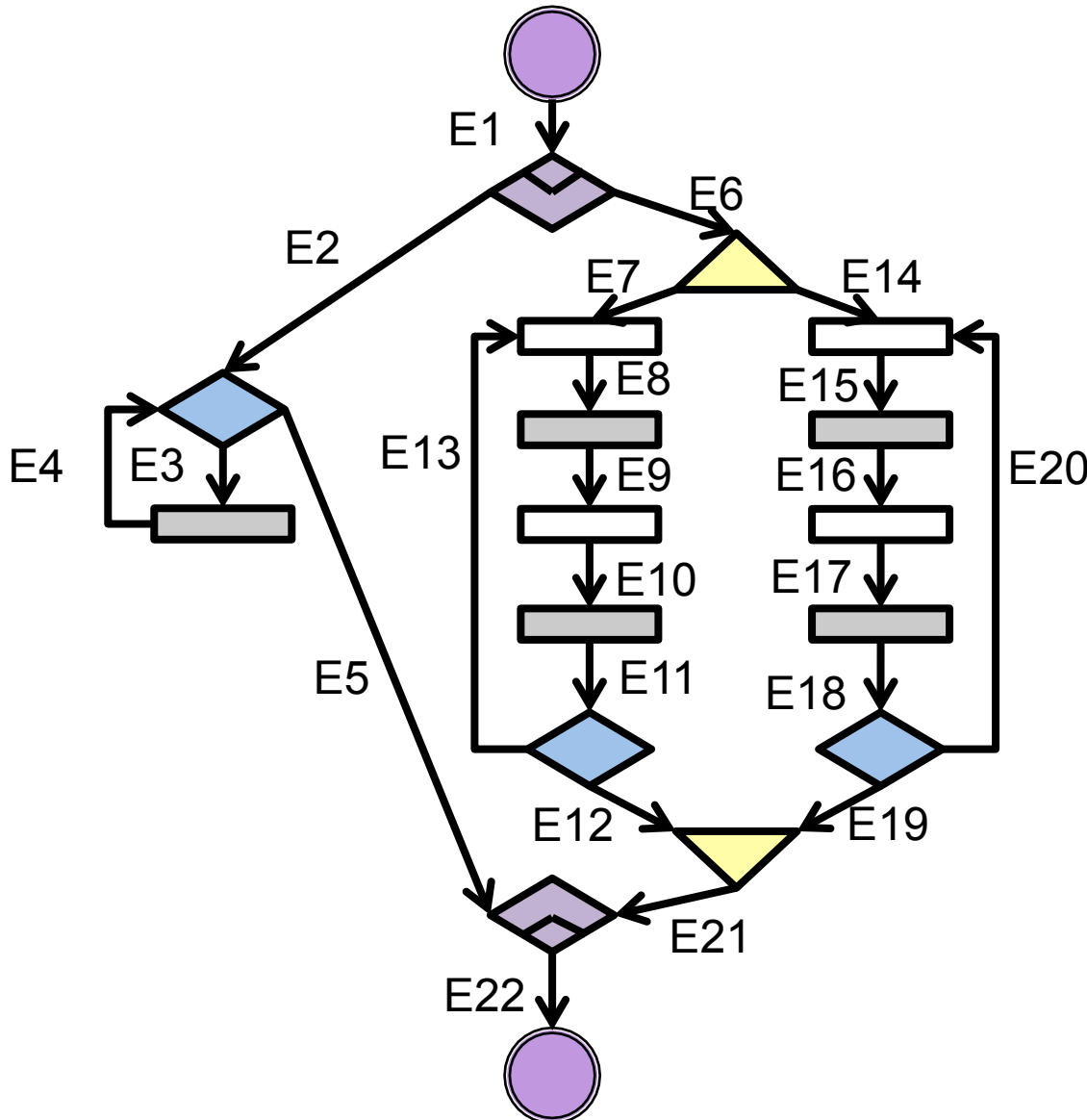
$$E1 \geq E6$$

Abort End:

$$E22 = E5 + E21$$

Preemption:

ILP model



Abort start:

$$E1 = E2$$

$$E1 \geq E6$$

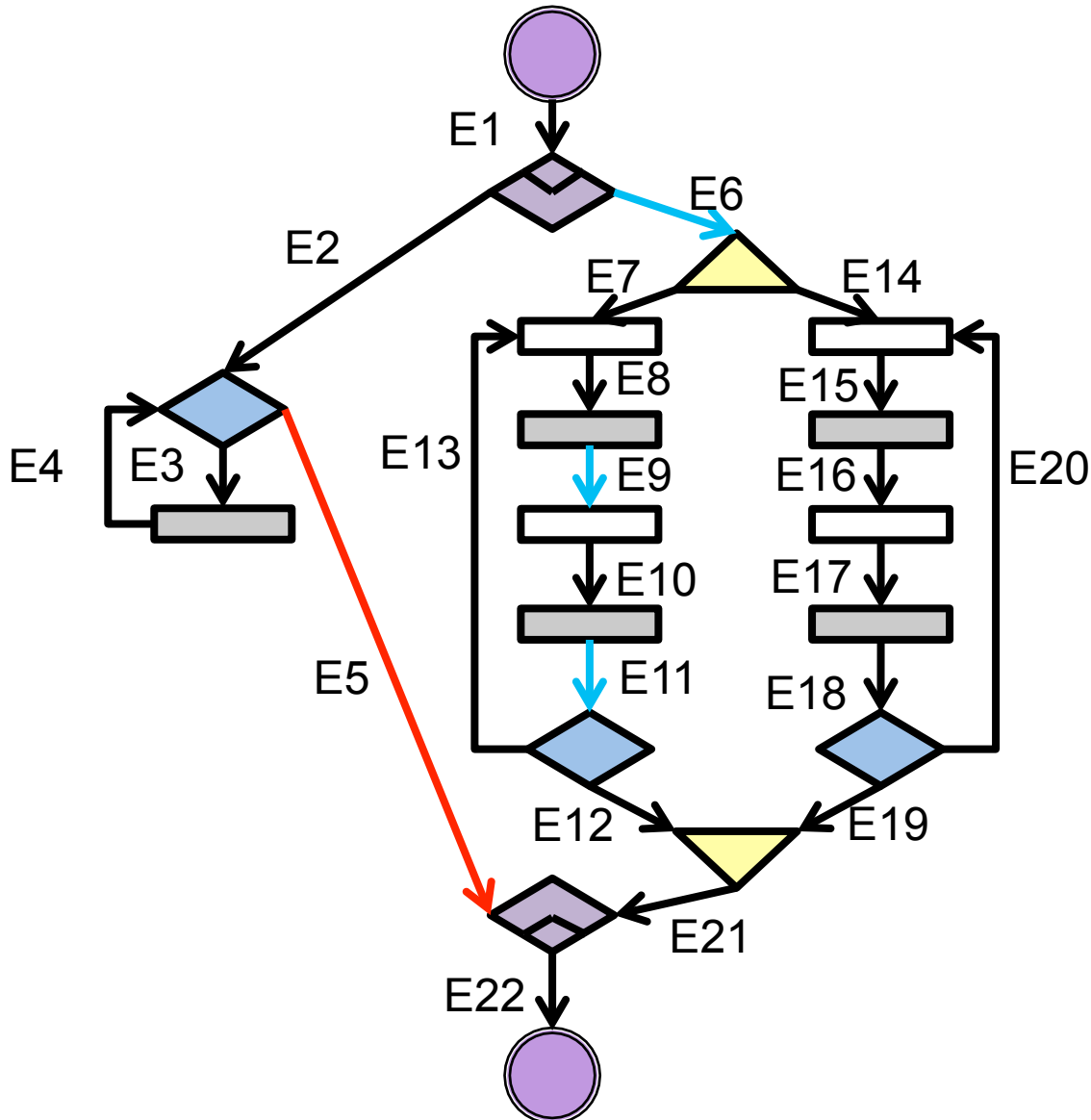
Abort End:

$$E22 = E5 + E21$$

Preemption:

$$E6 + E9 + E11 \leq 1 - E5$$

ILP model



Abort start:

$$E1 = E2$$

$$E1 \geq E6$$

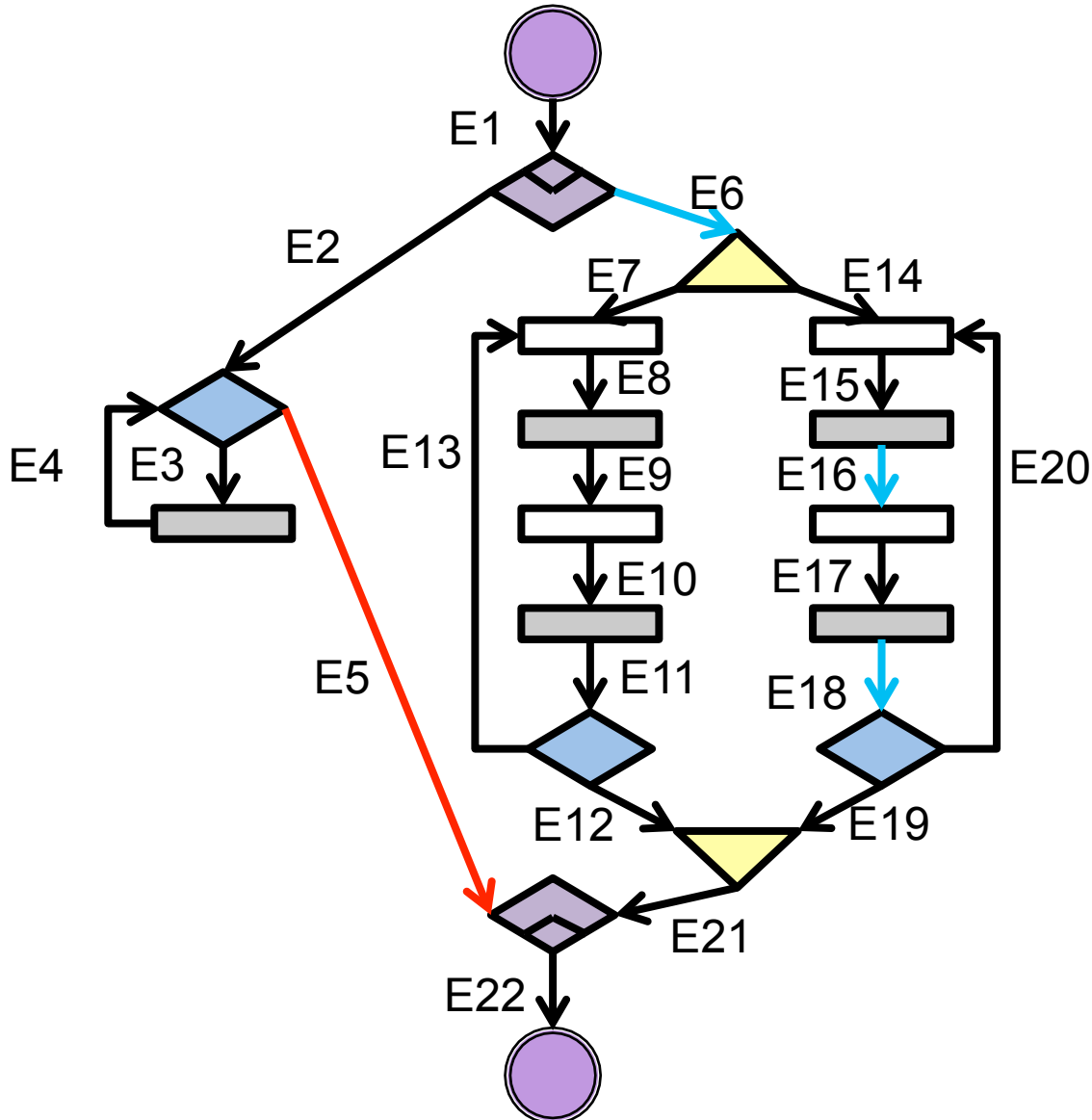
Abort End:

$$E22 = E5 + E21$$

Preemption:

$$E6 + E9 + E11 \leq 1 - E5$$

ILP model



Abort start:

$$E1 = E2$$

$$E1 \geq E6$$

Abort End:

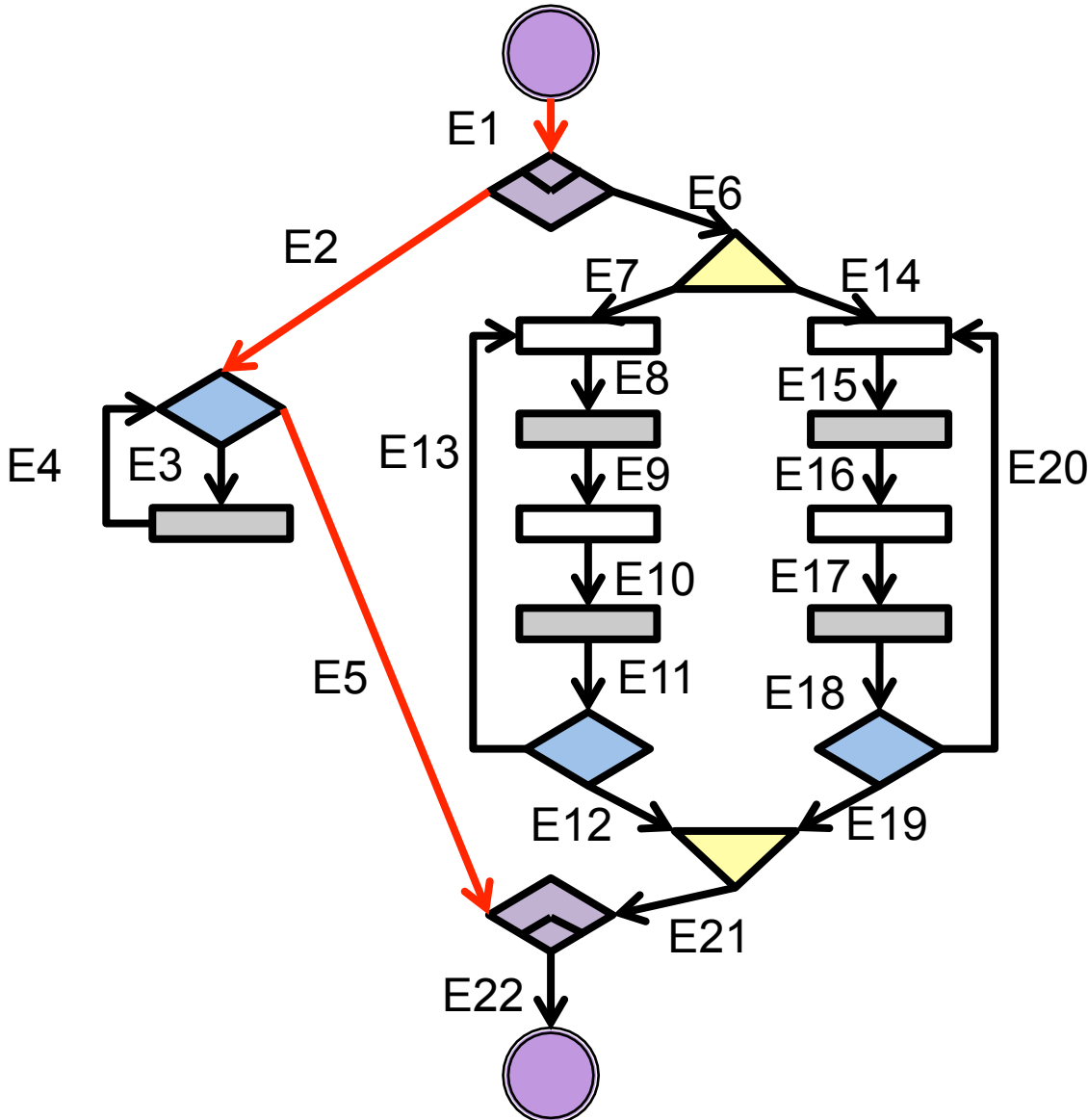
$$E22 = E5 + E21$$

Preemption:

$$E6 + E9 + E11 \leq 1 - E5$$

$$E6 + E16 + E18 \leq 1 - E5$$

ILP model



Abort start:

$$E1 = E2$$

$$E1 \geq E6$$

Abort End:

$$E22 = E5 + E21$$

Preemption:

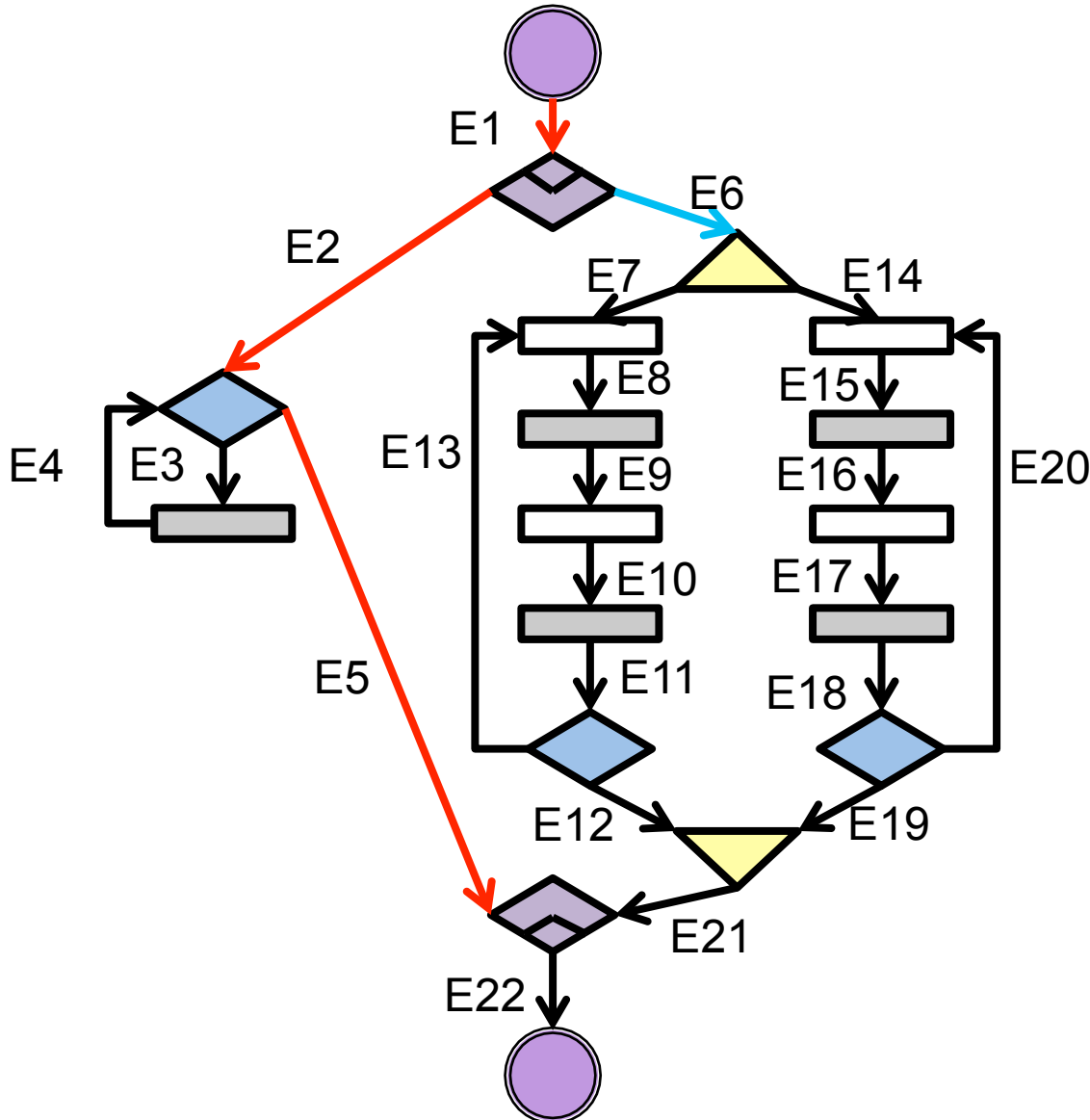
$$E6 + E9 + E11 \leq 1 - E5$$

$$E6 + E16 + E18 \leq 1 - E5$$

0 0 0 0

Preemption

ILP model



Abort start:

$$E1 = E2$$

$$E1 \geq E6$$

Abort End:

$$E22 = E5 + E21$$

Preemption:

$$E6 + E9 + E11 \leq 1 - E5$$

$$E6 + E16 + E18 \leq 1 - E5$$

0 0 0 0

Preemption

Benchmarking

- Compared with 3 existing approaches [1,2,3]
- Conducted in 2 phases
 - Phase 1: Theoretical performance
 - Phase 2: Real-world applications
- Benchmark computer
 - Windows based
 - Quad-core 1.6 GHz CPU
 - 8 GB memory

[1] L. Ju, B. K. Huynh, S. Chakraborty, and A. Roychoudhury. *Context-sensitive timing analysis of Esterel programs*, DAC, 2009.

[2] S. Andalam, P. S. Roop, and A. Girault. *Pruning infeasible paths for tight WCRT analysis of synchronous programs*, DATE 2011.

[3] M. Kuo, R. Sinha, and P. S. Roop. *Efficient WCRT analysis of synchronous programs using reachability*, DAC, 2011.

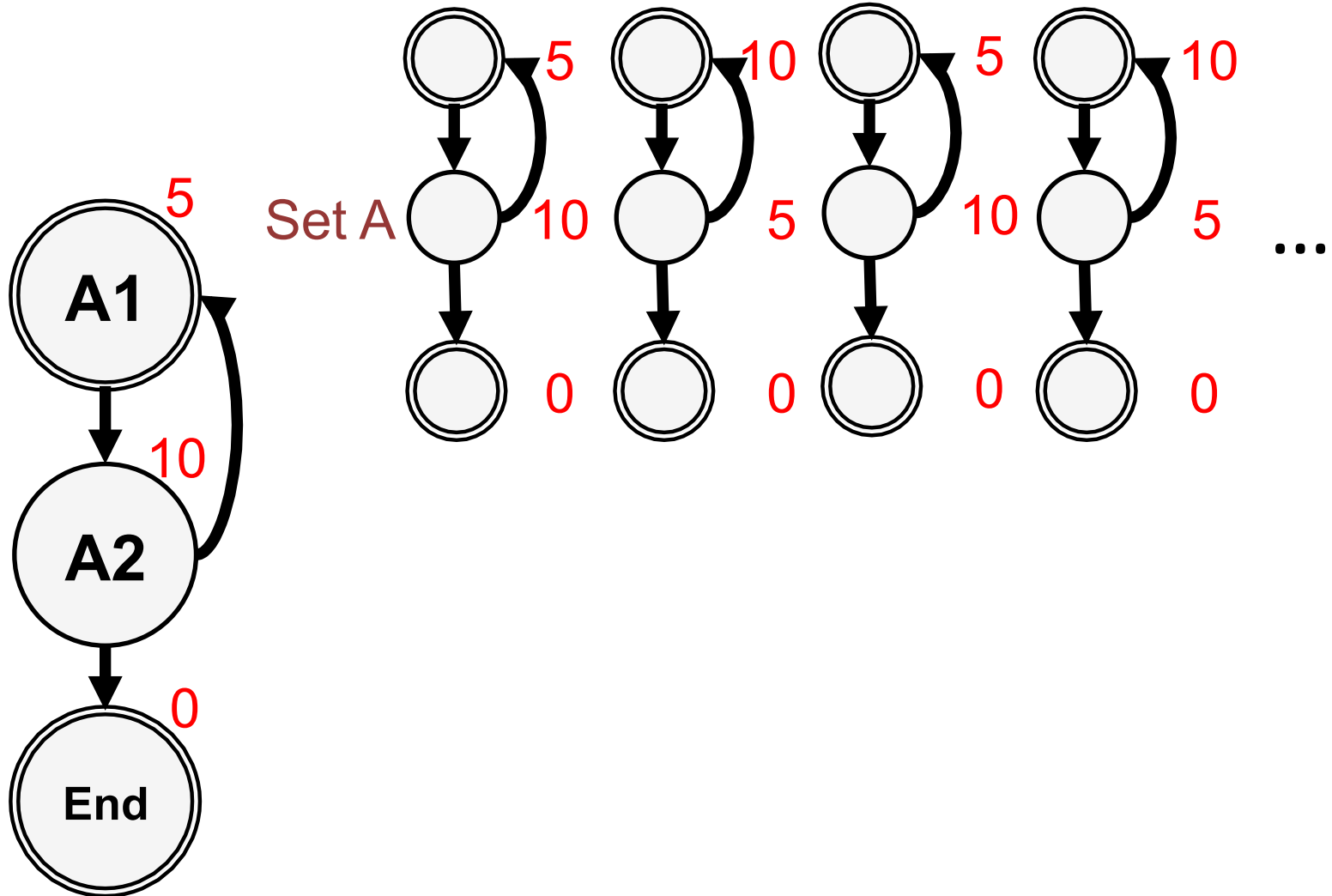
Scalability

- Analysis time V.S. program states.
- Scalability of ILPc
 - Time taken for each iteration.
 - Depend on number of program states.
 - The number of iteration.
 - Depend on structure and cost distribution.

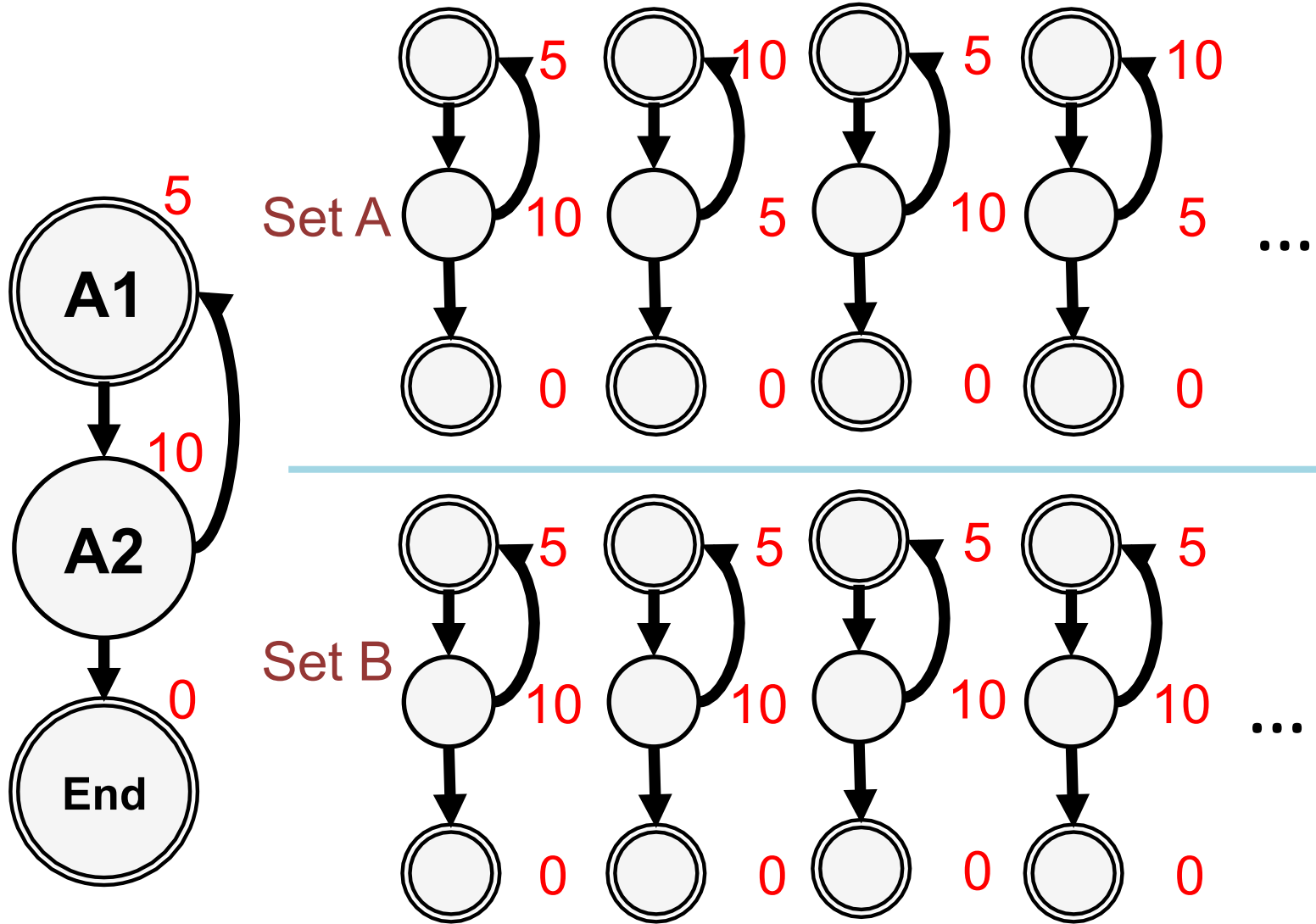
Benchmarking: Phase 1

- Two sets of benchmarks
 - Set A - **Maximize** the number of required iterations for a given number of program states.
 - Set B - **Minimize** the number of required iterations for a given number of program states.
 - Iteration = 1

Benchmarking: Phase 1

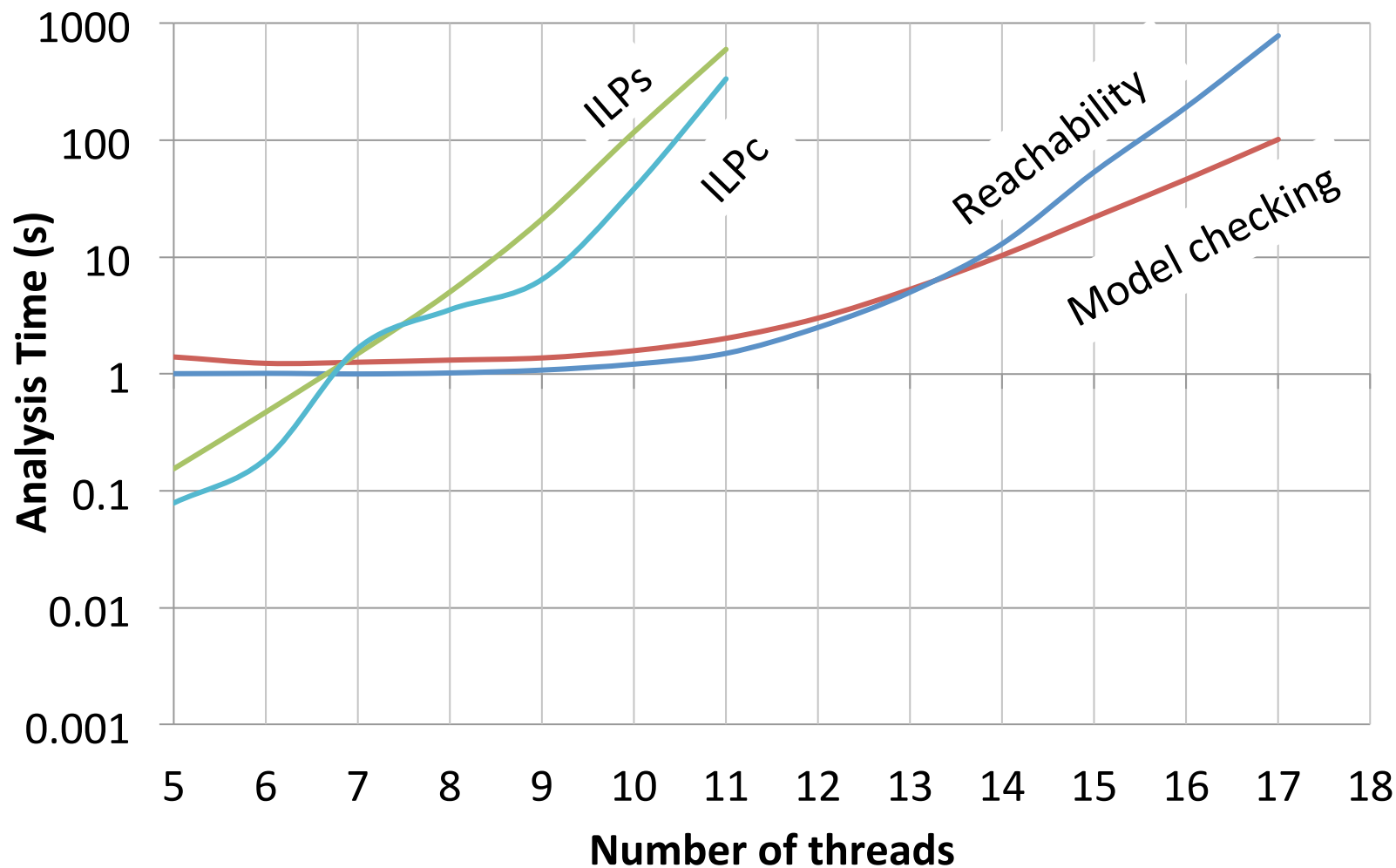


Benchmarking: Phase 1



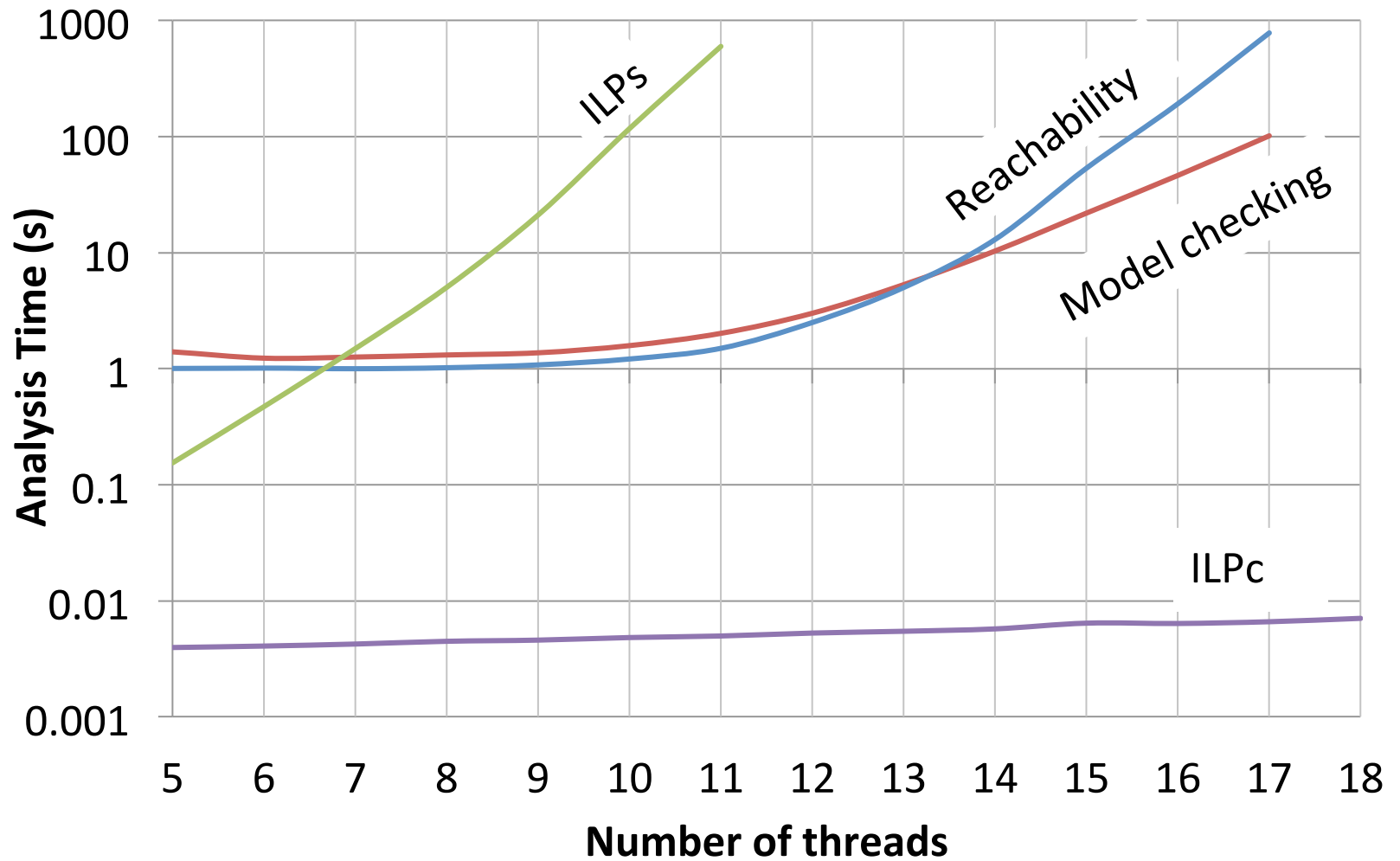
Benchmarking: Phase 1

Set A



Benchmarking: Phase 1

Set B



Benchmarking: Phase 1

- Same precision.
- Analysis time of ILPc heavily depends on number of iterations, but not number of program states.
- On average, analysis time of ILPc should be between the worst case and best case scenarios.

Benchmarking: Phase2

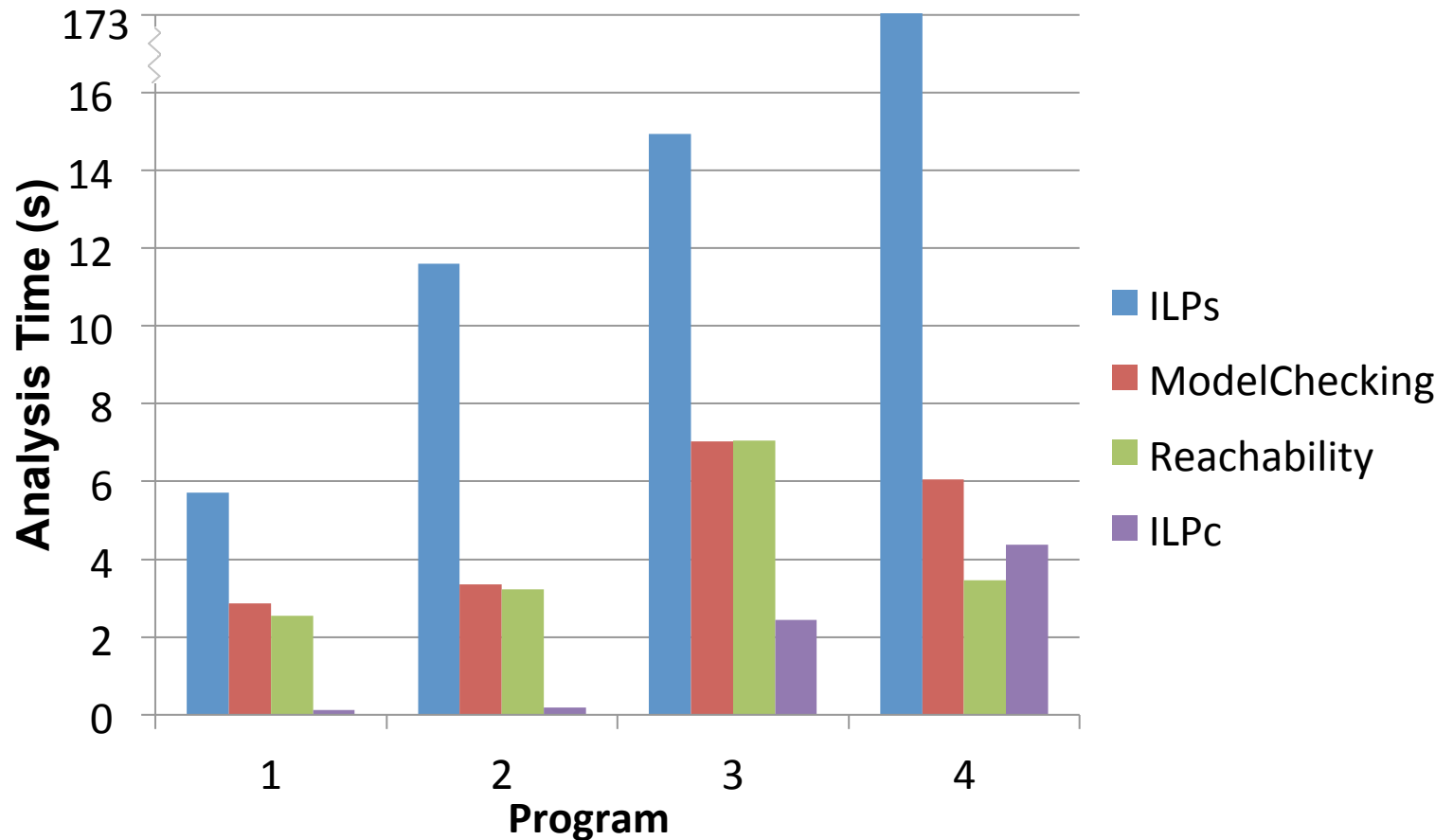
	Name	WCRT	Threads	
1	ChannelProtocol	997	7	Small
2	Flasher	617	7	
3	RobotSonar	1874	7	
4	DrillStation	2751	15	Large
5	CruiseControl	1931	25	
6	RailroadCrossing	4472	30	
7	WaterMonitor	4631	40	

L. H. Yoong and G. D. Shaw. *Auckland function block benchmark*. University of Auckland, 2010.

www.ece.auckland.ac.nz/~pretzel/Auckland_FB_Benchmark.zip

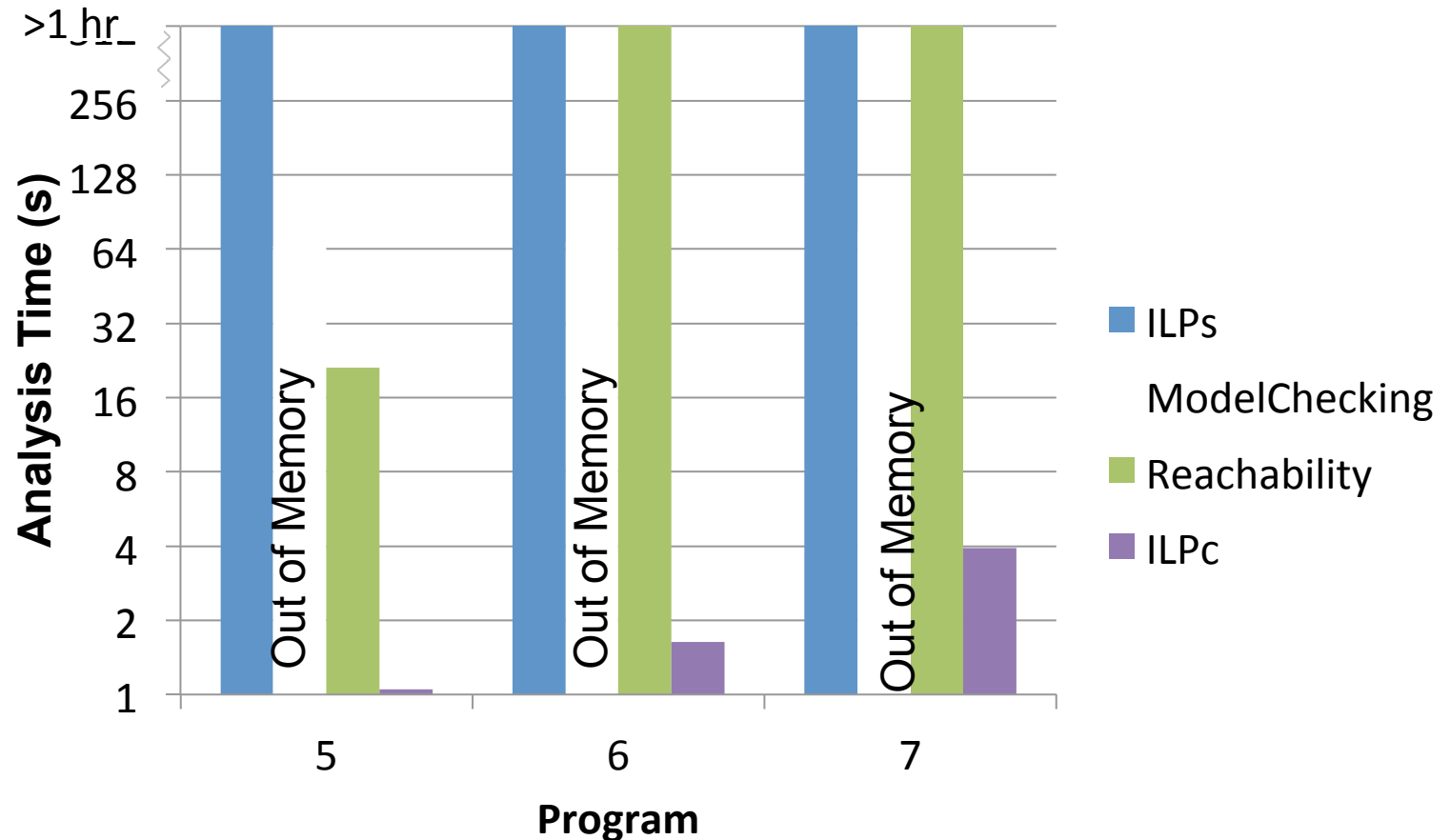
Benchmarking: Phase2

Benchmarks 1-4 (less than 20 threads)



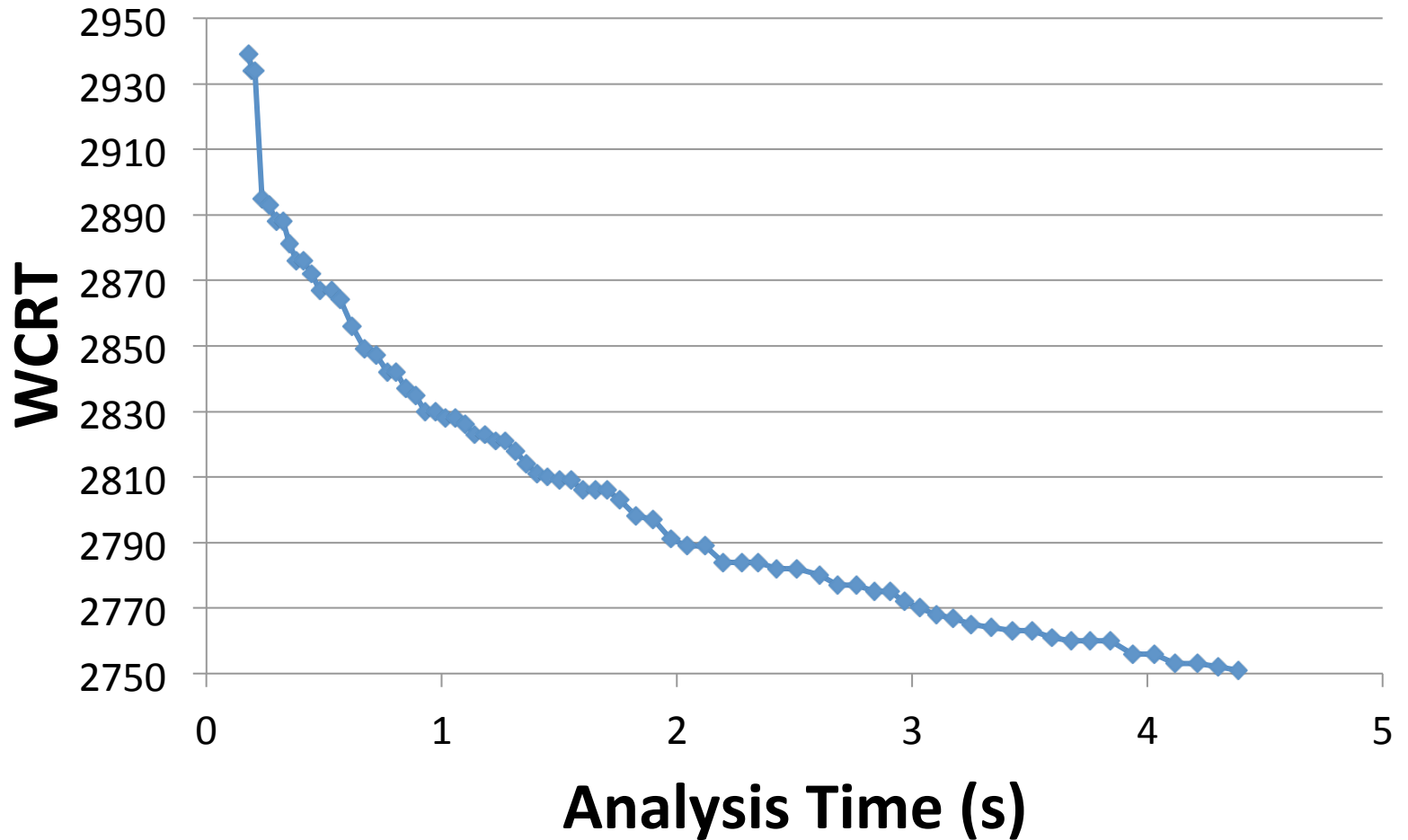
Benchmarking: Phase2

Benchmarks 5-7 (more than 20 threads)



Benchmarking: Phase2

DrillStation



Results summary

- Same precision as state exploration approaches
- Orders of magnitude faster compared to state exploration approaches for synchronous benchmarks for industrial automation applications

Conclusions

- We proposed ILPc that is tailored for timing analysis of concurrent programs with scalable performance.
- Precision improves with the number of iterations.
- Safe over-approximation in any iteration. If the user's precision requirement is met, analysis can be stopped.
- Compositional: adding further analysis components such as DVFS module / caches etc easier.
- Outlook:
 - User guided path infeasibility constraints through model checking.
 - Bicriteria optimization techniques for (WCRT, Energy)